

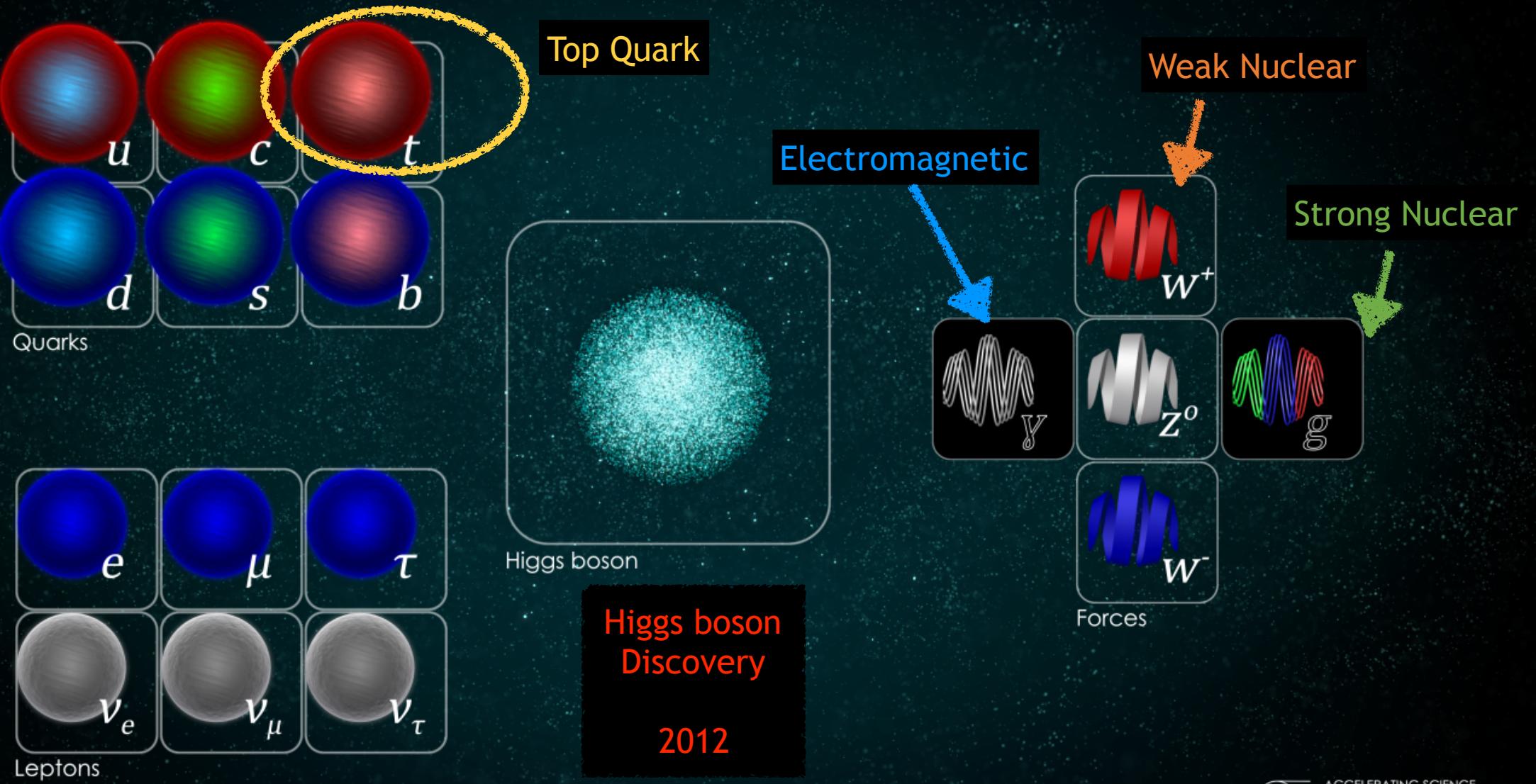
Understanding the Top quark

At the LHC and beyond

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Department of Physics, IIT Guwahati

The Standard Model



ACCELERATING SCIENCE

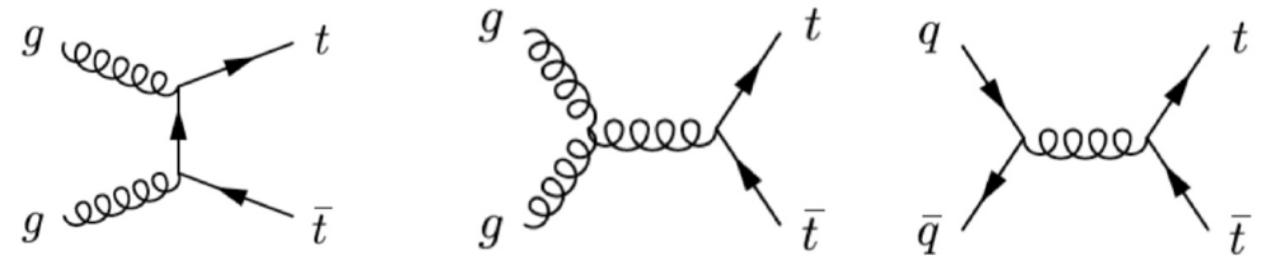
Top quark (discovery in 1995):

An elementary particle about 180 times heavier than the proton !
The only bare quark that decays before forming bound states, and therefore exposes its interactions with the other SM particles in a direct way.

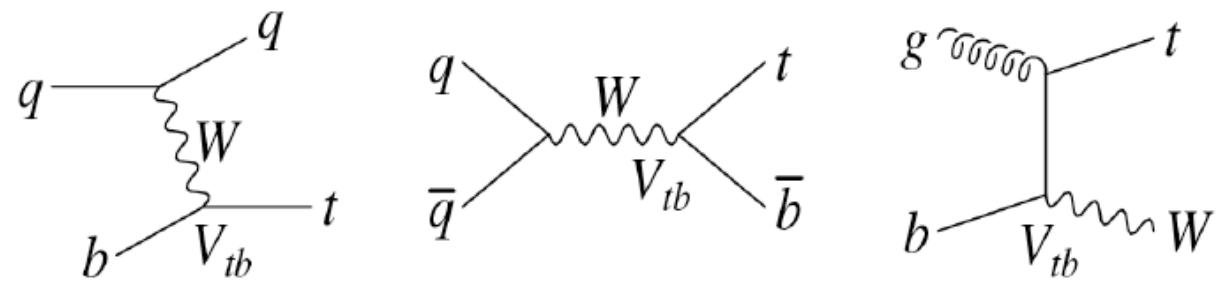
**Top quark being the heaviest elementary particle (so far)
has the strongest interaction with the Higgs boson**

It is crucial to know the top quark couplings precisely to know the details of Higgs couplings and thus to understand the Electroweak Symmetry Breaking

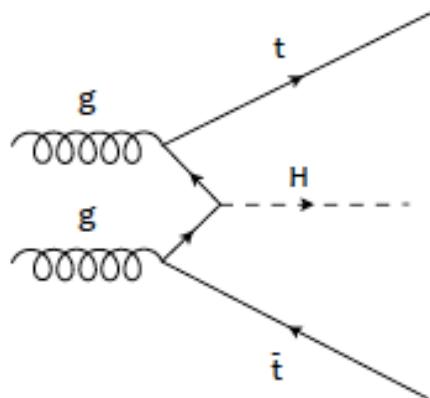
Top quark is produced at LCH in many processes



pair production

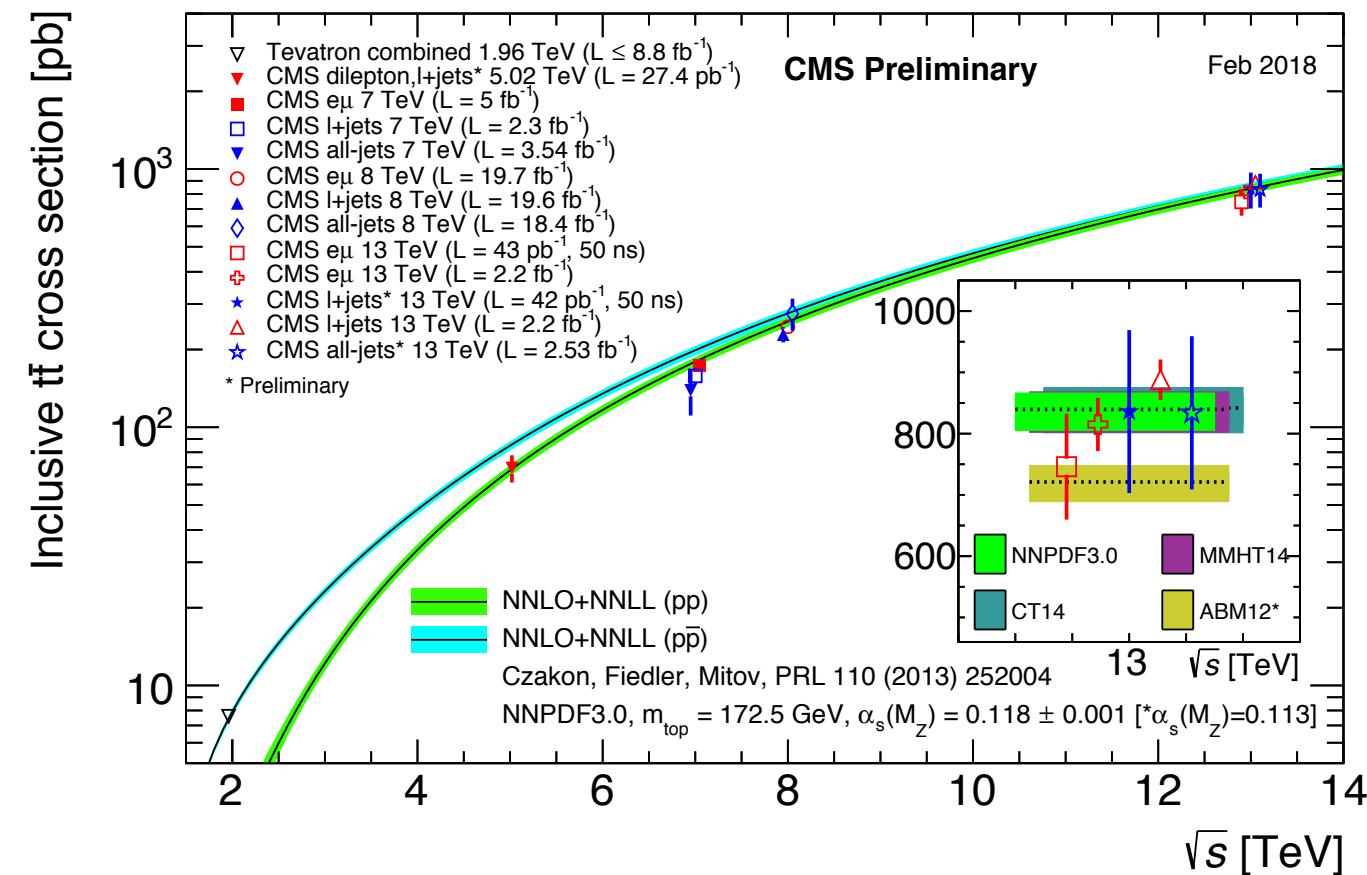
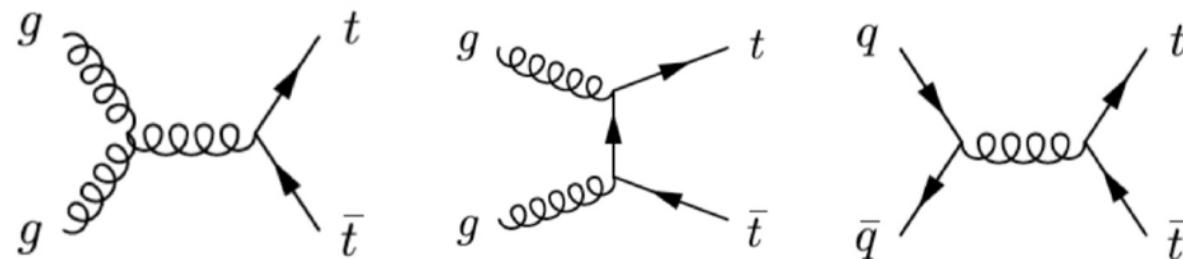


single top with a light jet / W/Z and jet

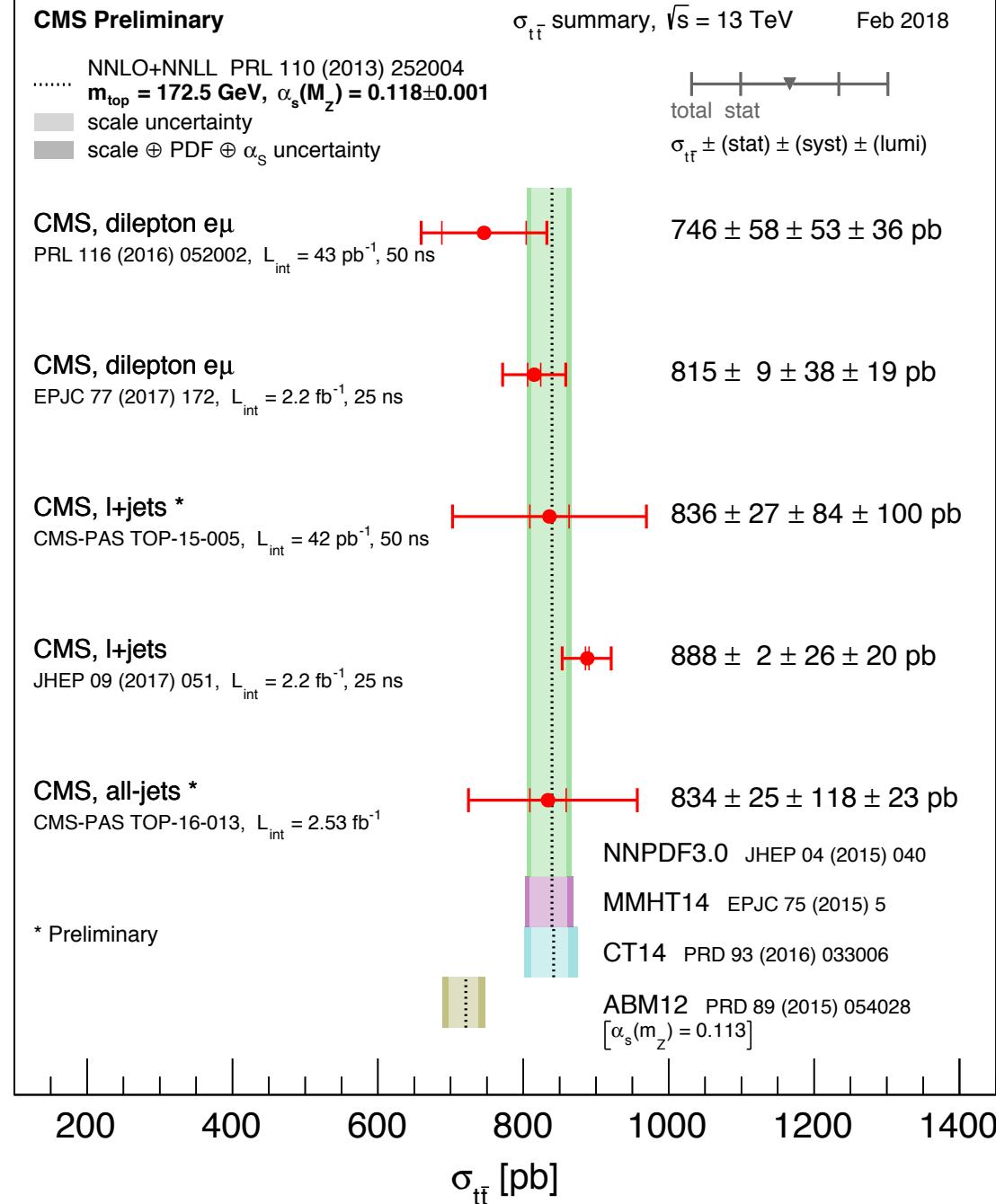


pair production along with H/Z

Top quark pair production at the LHC



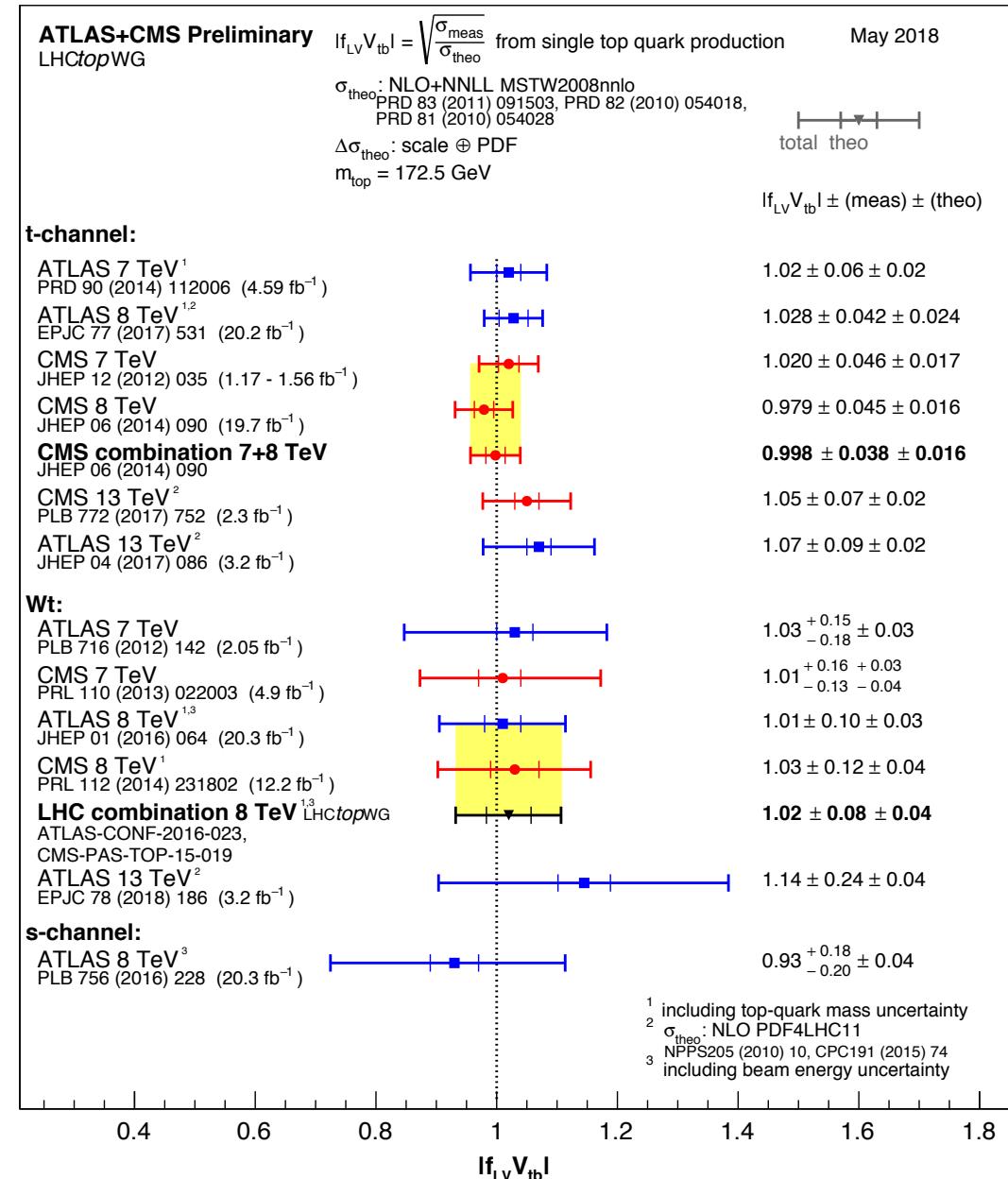
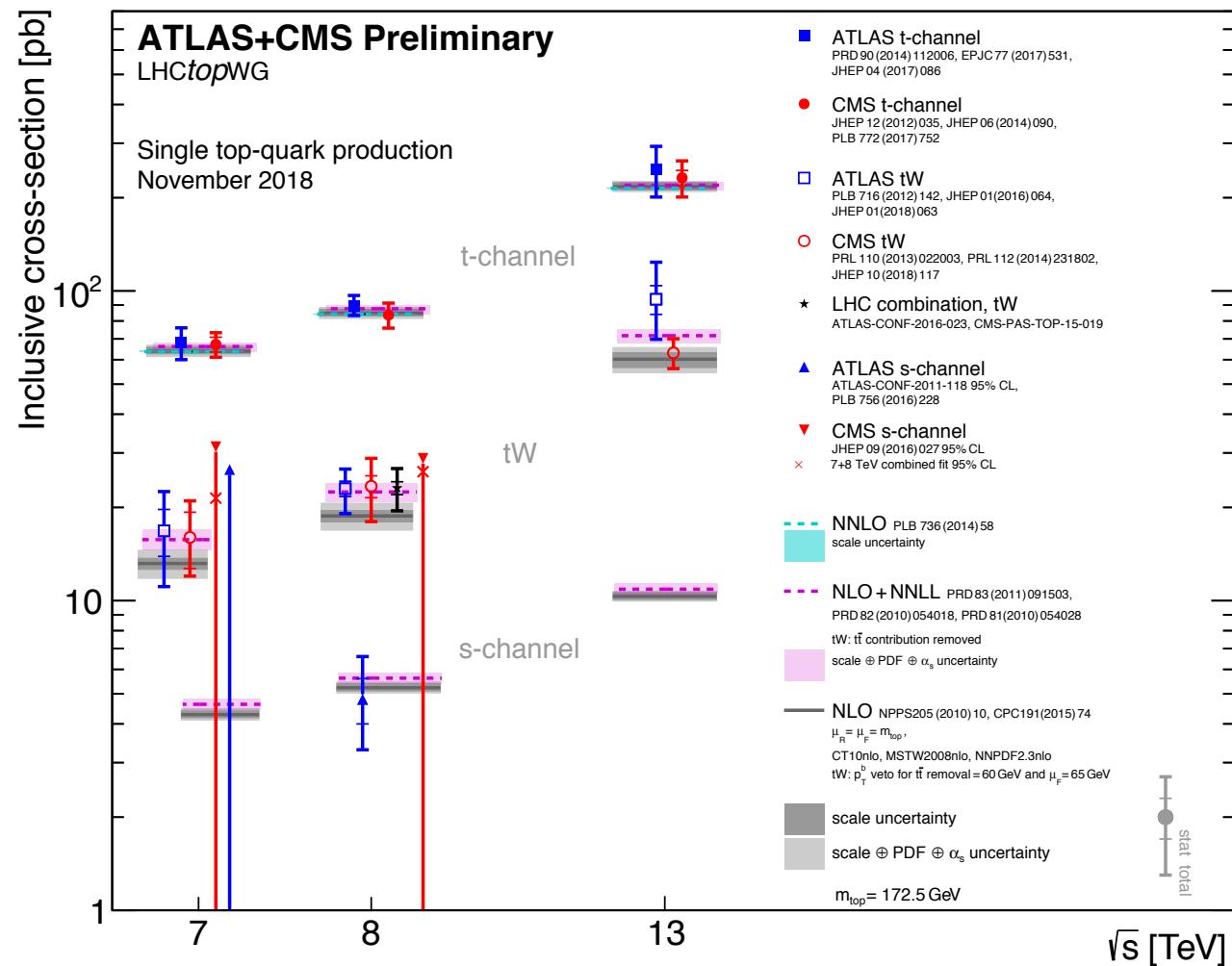
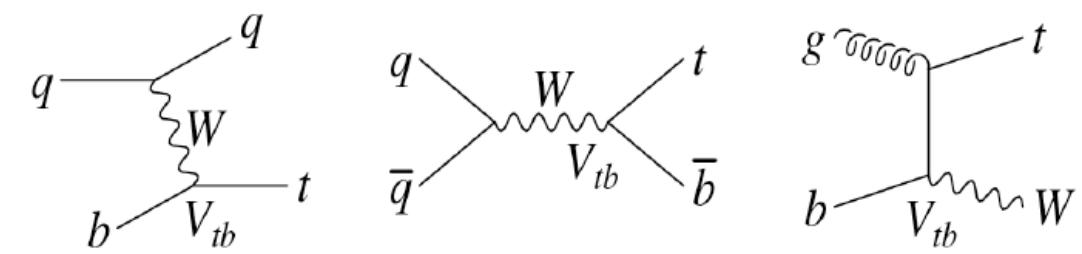
More than 80×10^6 top pairs
 @ 13 TeV, 100 /fb (approx. one year)



Single Top quark production at the LHC

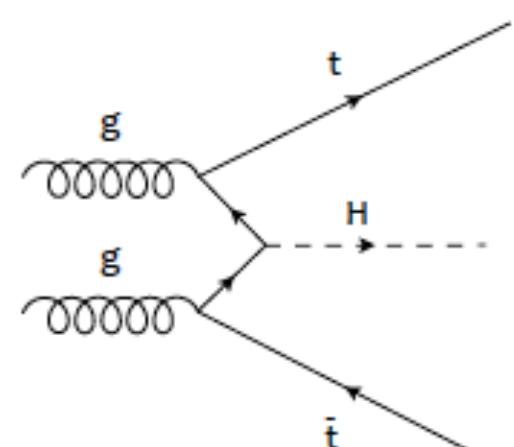
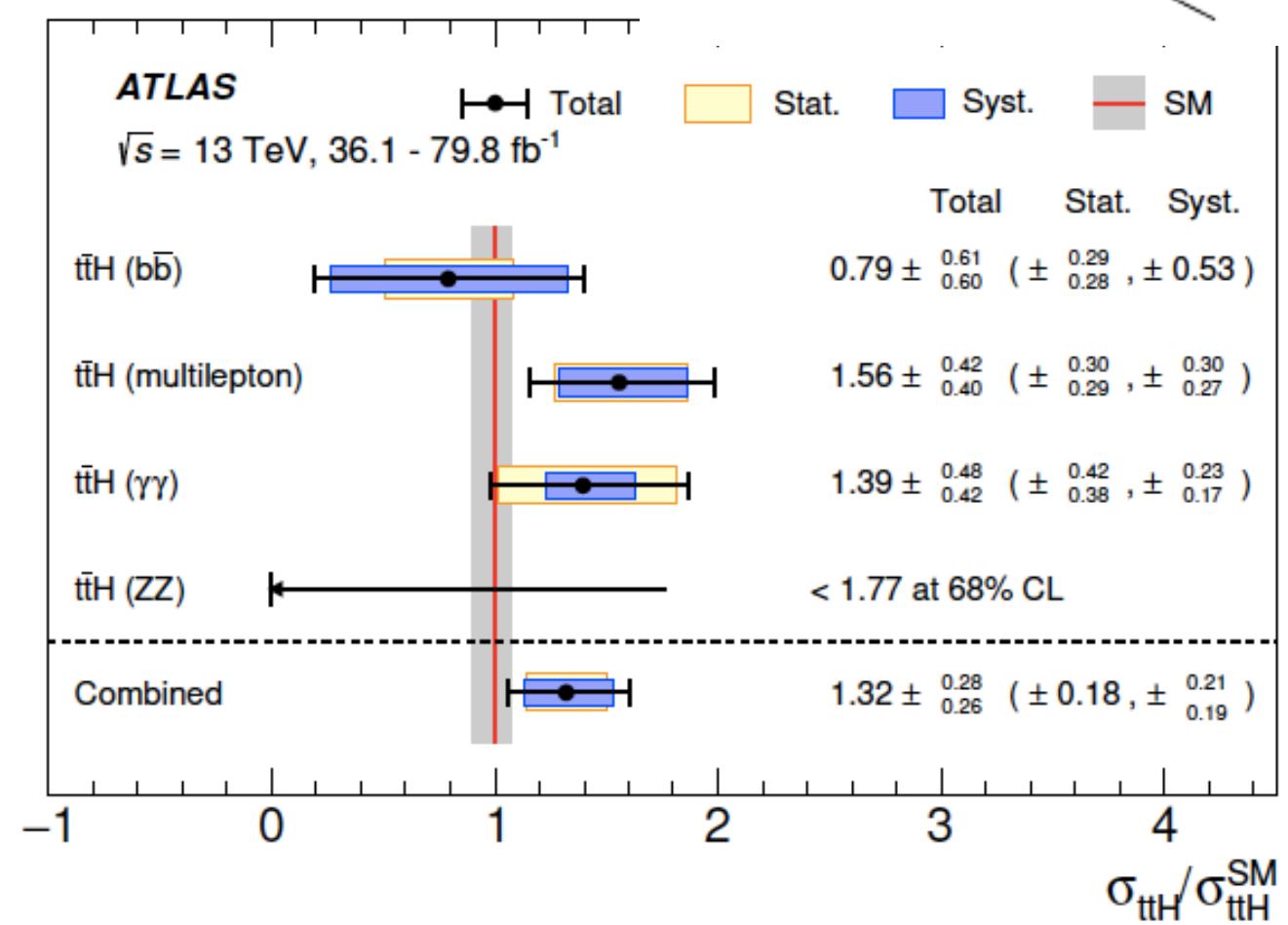
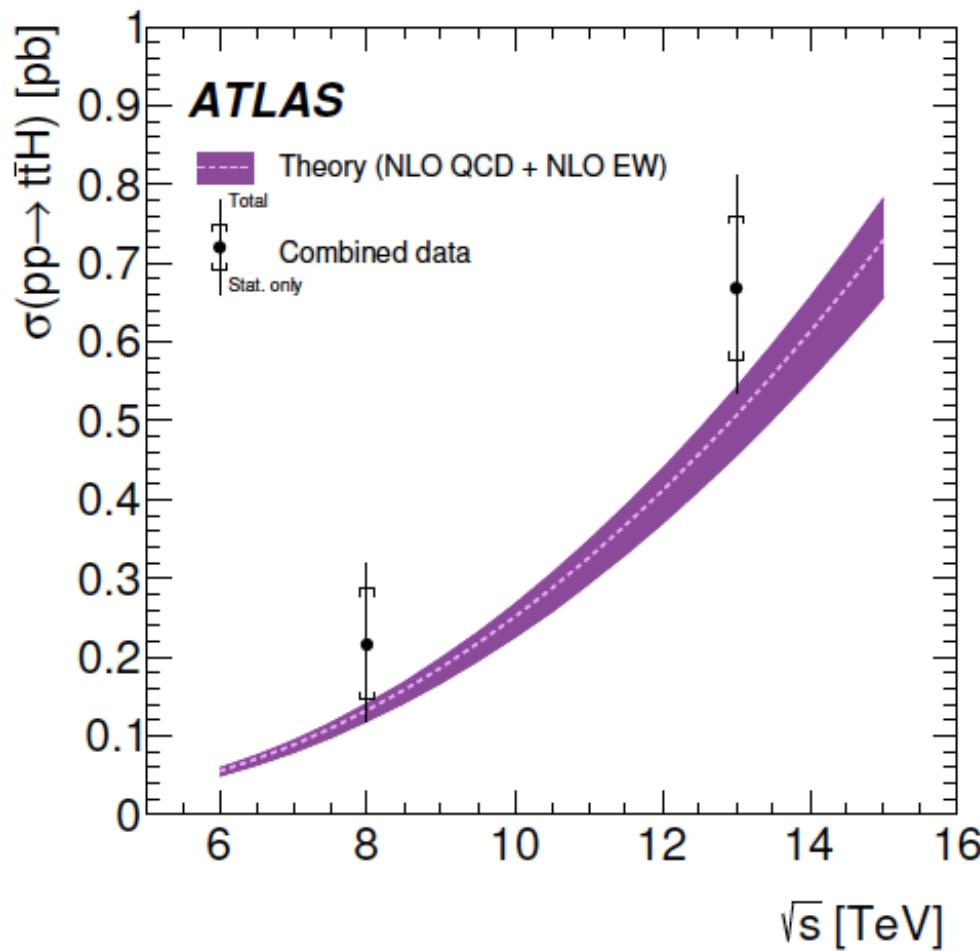
direct measurement of V_{tb}

**More than 30×10^6 single top
@ 13 TeV, 100 /fb**



ATLAS, Phys. Lett. B 784 (2018) 173

About 60000 top pairs along with H
@ 13 TeV, 100 /fb



Top quark mass

Need to know precisely
to understand evolution of
Higgs coupling.

ATLAS+CMS Preliminary
LHCtopWG

..... World comb. (Mar 2014) [2]
stat
total uncertainty

LHC comb. (Sep 2013) ^{LHCtopWG}

World comb. (Mar 2014)

ATLAS, I+jets

ATLAS, dilepton

ATLAS, all jets

ATLAS, single top

ATLAS, dilepton

ATLAS, all jets

ATLAS, I+jets

ATLAS comb. (Oct 2018)

CMS, I+jets

CMS, dilepton

CMS, all jets

CMS, I+jets

CMS, dilepton

CMS, all jets

CMS, single top

CMS comb. (Sep 2015)

CMS, I+jets

CMS, dilepton

CMS, all jets

m_{top} summary, $\sqrt{s} = 7\text{-}13 \text{ TeV}$ November 2018

total stat

$m_{\text{top}} \pm \text{total (stat} \pm \text{syst)}$	\sqrt{s}	Ref.
$173.29 \pm 0.95 (0.35 \pm 0.88)$	7 TeV	[1]
$173.34 \pm 0.76 (0.36 \pm 0.67)$	1.96-7 TeV	[2]
$172.33 \pm 1.27 (0.75 \pm 1.02)$	7 TeV	[3]
$173.79 \pm 1.41 (0.54 \pm 1.30)$	7 TeV	[3]
$175.1 \pm 1.8 (1.4 \pm 1.2)$	7 TeV	[4]
$172.2 \pm 2.1 (0.7 \pm 2.0)$	8 TeV	[5]
$172.99 \pm 0.85 (0.41 \pm 0.74)$	8 TeV	[6]
$173.72 \pm 1.15 (0.55 \pm 1.01)$	8 TeV	[7]
$172.08 \pm 0.91 (0.39 \pm 0.82)$	8 TeV	[8]
$172.69 \pm 0.48 (0.25 \pm 0.41)$	7+8 TeV	[8]
$173.49 \pm 1.06 (0.43 \pm 0.97)$	7 TeV	[9]
$172.50 \pm 1.52 (0.43 \pm 1.46)$	7 TeV	[10]
$173.49 \pm 1.41 (0.69 \pm 1.23)$	7 TeV	[11]
$172.35 \pm 0.51 (0.16 \pm 0.48)$	8 TeV	[12]
$172.82 \pm 1.23 (0.19 \pm 1.22)$	8 TeV	[12]
$172.32 \pm 0.64 (0.25 \pm 0.59)$	8 TeV	[12]
$172.95 \pm 1.22 (0.77 \pm 0.95)$	8 TeV	[13]
$172.44 \pm 0.48 (0.13 \pm 0.47)$	7+8 TeV	[12]
$172.25 \pm 0.63 (0.08 \pm 0.62)$	13 TeV	[14]
$172.33 \pm 0.70 (0.14 \pm 0.69)$	13 TeV	[15]
$172.34 \pm 0.79 (0.20 \pm 0.76)$	13 TeV	[16]

[1] ATLAS-CONF-2013-102

[7] JHEP 09 (2017) 118

[2] arXiv:1403.4427

[8] arXiv:1810.01772

[3] Eur.Phys.J.C75 (2015) 330

[9] JHEP 12 (2012) 105

[4] Eur.Phys.J.C75 (2015) 158

[10] Eur.Phys.J.C72 (2012) 2202

[5] ATLAS-CONF-2014-055

[11] Eur.Phys.J.C74 (2014) 2758

[6] Phys.Lett.B761 (2016) 350

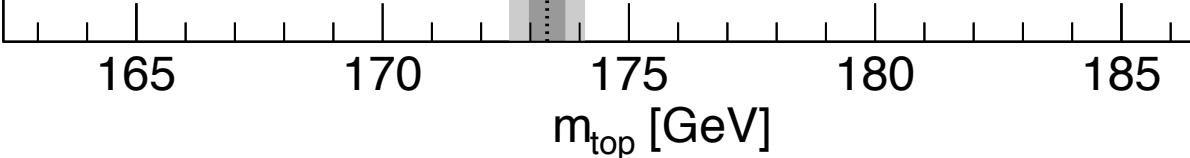
[12] Phys.Rev.D93 (2016) 072004

[13] EPJC 77 (2017) 354

[14] arXiv:1805.01428

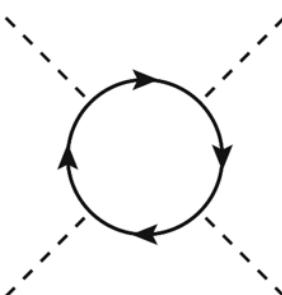
[15] CMS PAS TOP-17-001

[16] CMS PAS TOP-17-008



Why is it important

$$V(\phi) = \mu^2 \phi^\dagger \phi + \lambda (\phi^\dagger \phi)^2$$



Running of Higgs self coupling

$$16\pi^2 \frac{d\lambda}{d \log \mu} = 24\lambda^2 + 12\lambda g_{htt}^2 - 9\lambda \left(g^2 + \frac{g'^2}{3} \right) - 6g_{htt}^4 + \frac{9g^4}{8} + \frac{3g'^4}{8} + \frac{3g^2 g'^2}{4}$$

In the SM, at tree level

$$g_{htt}^{SM} = \frac{\sqrt{2} m_t}{v} = \frac{\sqrt{2} \cdot (173.34 \pm 0.76)}{246} = 0.996 \pm 0.004$$

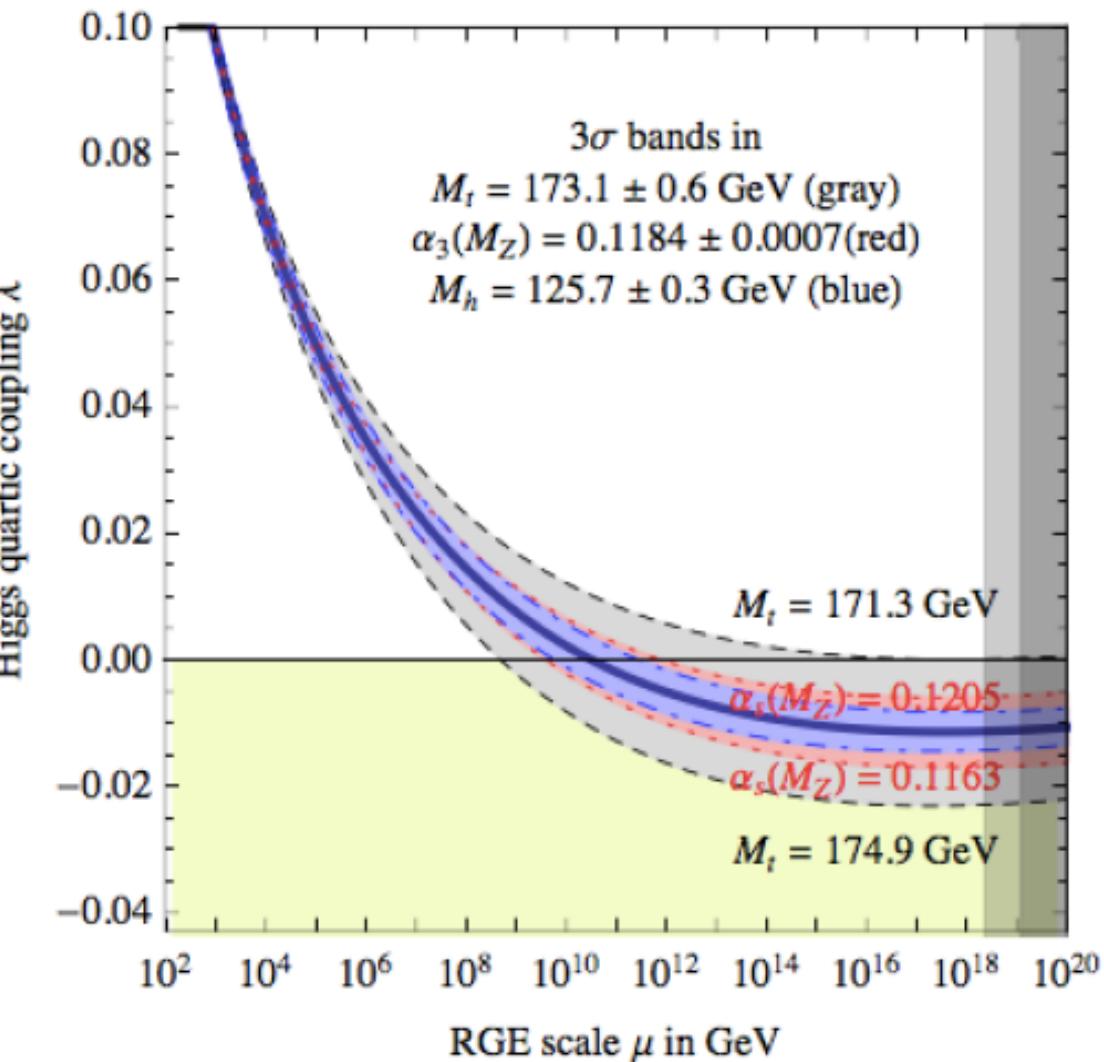
In 2HDM / MSSM

$$g_{htt} = \frac{\sqrt{2} m_t}{v} \frac{\cos \alpha}{\sin \beta}$$

In general

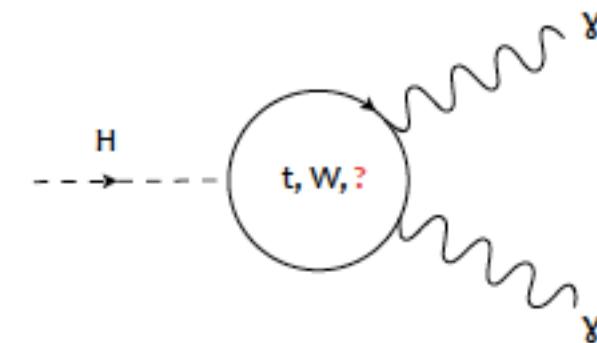
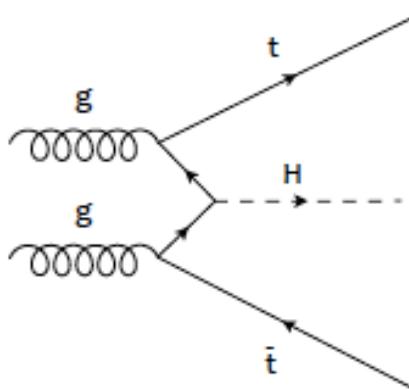
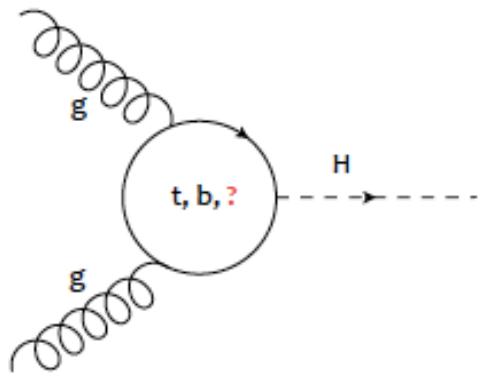
$$g_{htt} = c_t g_{htt}^{SM}$$

$$Y_d \bar{Q}_L \phi d_R - Y_u \bar{Q}_L \tilde{\phi} u_R \quad y_t = g_{htt}$$

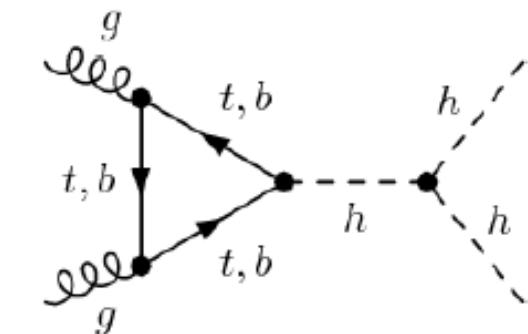
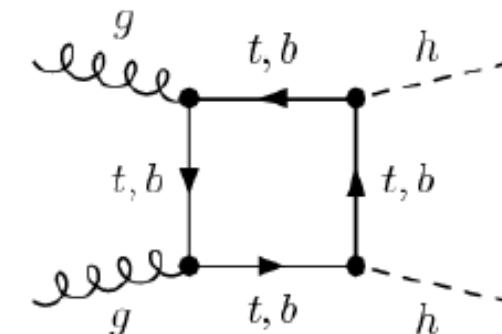
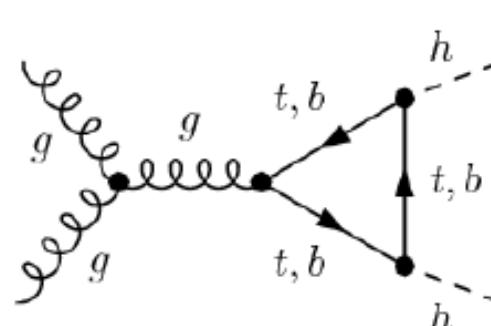
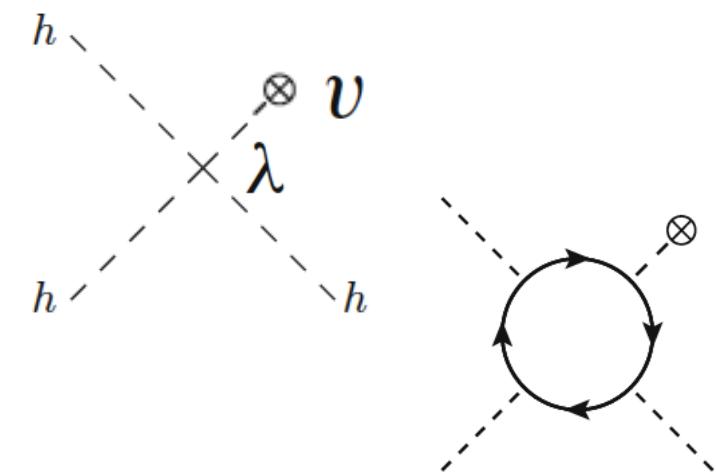


Degassi, et al., JHEP08(2012)098 [1205.6497]

Top quark Yukawa influencing the production and decay of the Higgs boson at the LHC



Also the measurement of
Higgs trilinear coupling



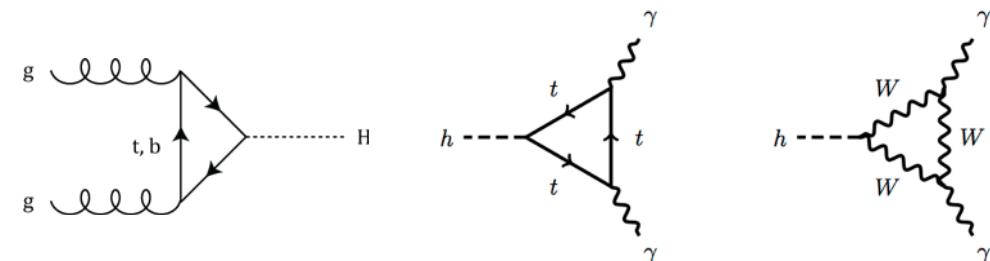
$$\mathcal{L}_{t\bar{t}H} = -\frac{m_t}{v} \bar{\psi}_t (\kappa_t + \tilde{\kappa}_t i\gamma_5) H \psi_t \quad \text{SM} \Rightarrow \kappa_t = 1 \quad \tilde{\kappa}_t = 0$$

Indirect measurements

$pp(gg) \rightarrow H \rightarrow \gamma\gamma$

$$\sigma \cdot \text{BR}(gg \rightarrow H \rightarrow \gamma\gamma) = \sigma_{\text{SM}}(gg \rightarrow H) \cdot \text{BR}_{\text{SM}}(H \rightarrow \gamma\gamma) \cdot \frac{\kappa_g^2 \cdot \kappa_\gamma^2}{\kappa_H^2}$$

$$\sigma(gg \rightarrow H) * \text{BR}(H \rightarrow \gamma\gamma) \sim \frac{\kappa_F^2 \cdot \kappa_\gamma^2(\kappa_F, \kappa_V)}{0.75 \cdot \kappa_F^2 + 0.25 \cdot \kappa_V^2}$$



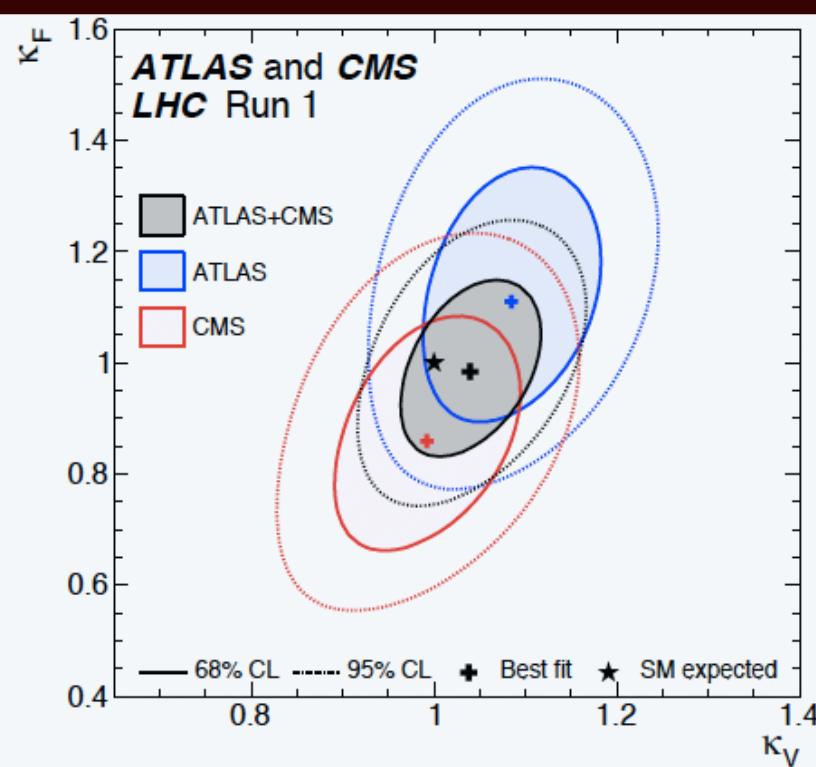
$$\kappa_V = \kappa_W = \kappa_Z$$

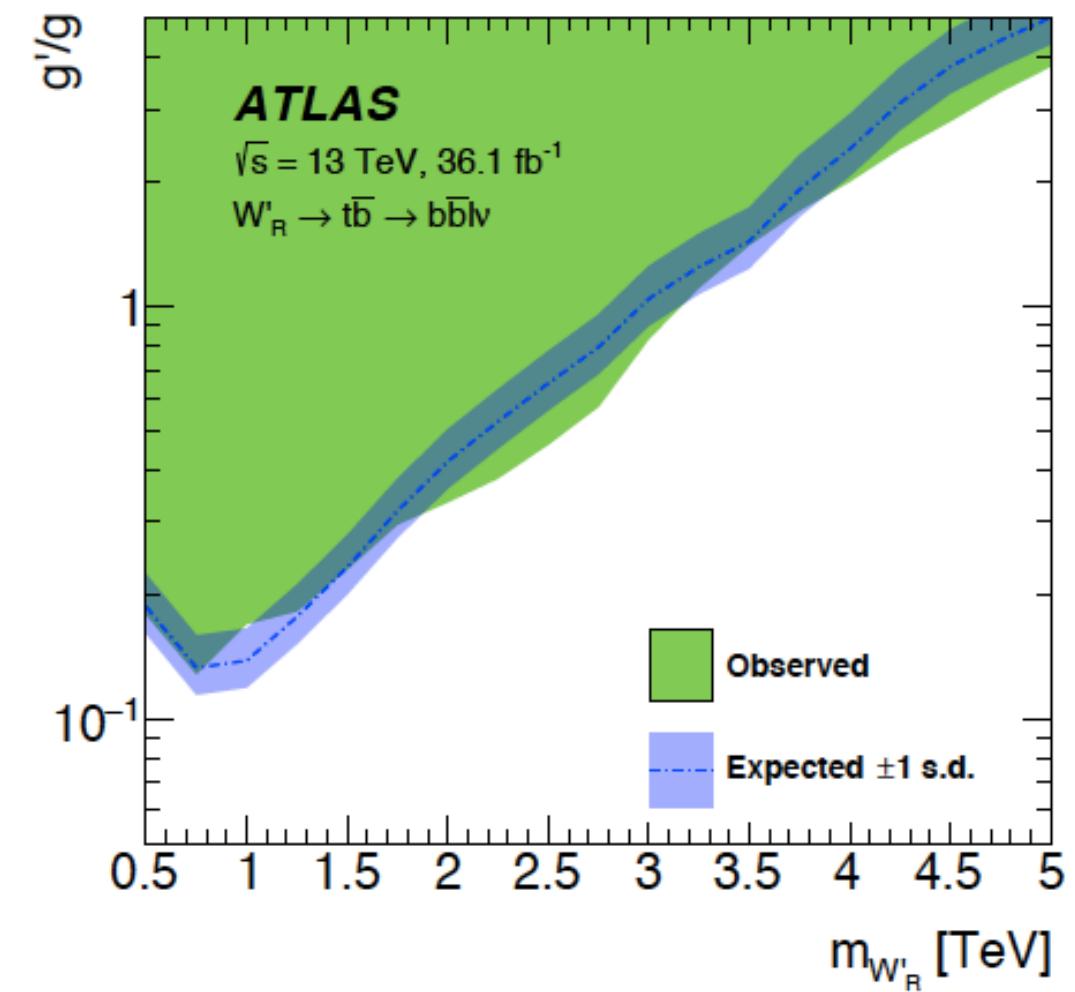
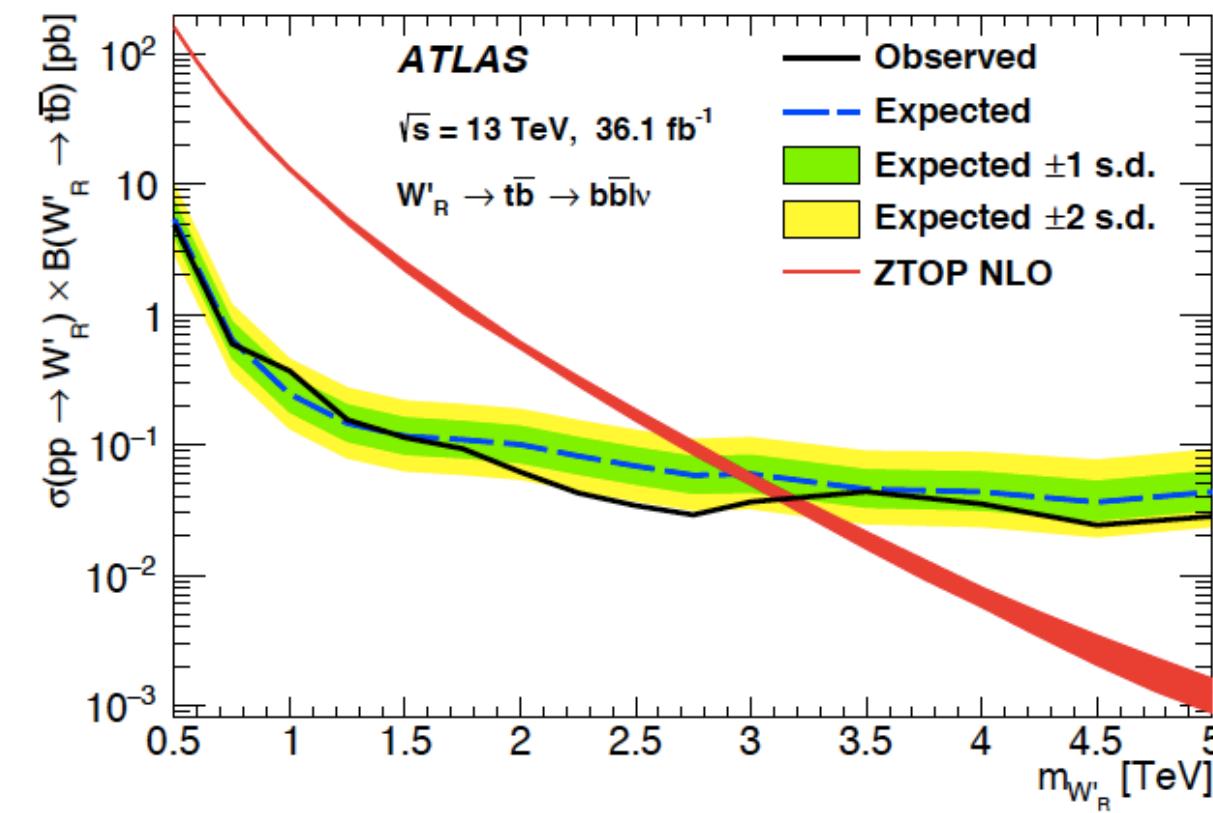
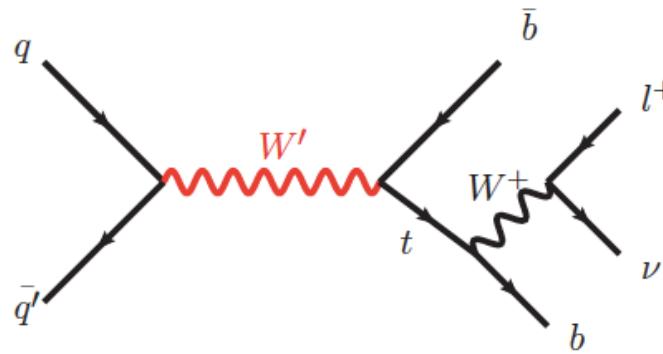
$$\kappa_F = \kappa_t = \kappa_b = \kappa_\tau = \kappa_g$$

$$\kappa_j^2 = \sigma_j / \sigma_j^{\text{SM}} \quad \text{or} \quad \kappa_j^2 = \Gamma_j / \Gamma_{\text{SM}}^j$$

$$\kappa_\gamma^2(\kappa_F, \kappa_V) = 1.59 \cdot \kappa_V^2 - 0.66 \cdot \kappa_V \kappa_F + 0.07 \cdot \kappa_F^2$$

$$\begin{aligned} \kappa_H^2 = & 0.57 \cdot \kappa_b^2 + 0.22 \cdot \kappa_W^2 + 0.09 \cdot \kappa_g^2 + \\ & 0.06 \cdot \kappa_\tau^2 + 0.03 \cdot \kappa_Z^2 + 0.03 \cdot \kappa_c^2 + \\ & 0.0023 \cdot \kappa_\gamma^2 + 0.0016 \cdot \kappa_{(Z\gamma)}^2 + \\ & 0.0001 \cdot \kappa_s^2 + 0.00022 \cdot \kappa_\mu^2 \end{aligned}$$



$W'^+ \rightarrow t\bar{b}$ and $W'^- \rightarrow \bar{t}b$


This can be relaxed considering

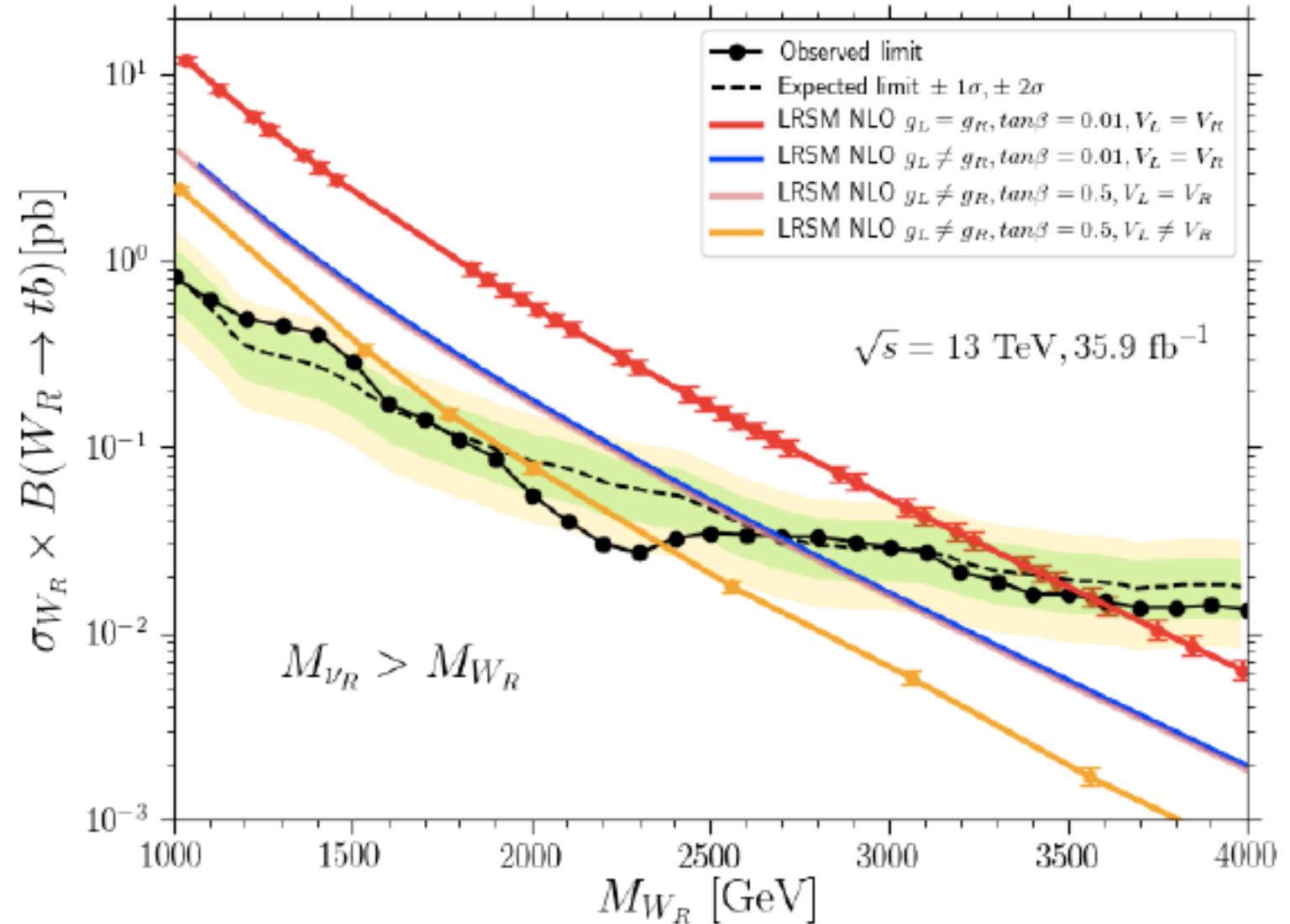
$$g_R \neq g_L$$

$$V_{\text{CKM}}^L \neq V_{\text{CKM}}^R$$

(respecting all constraints
including those from Flavour Sector)

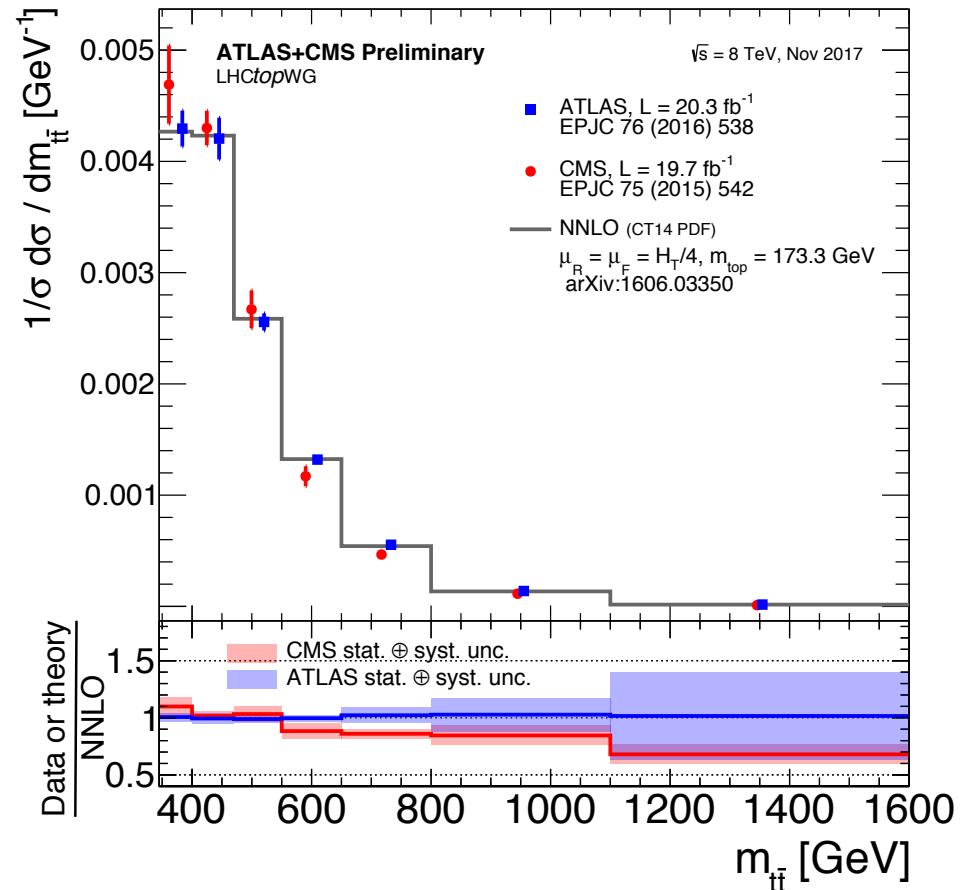
Frank, Ozdel, PP: [arXiv:1812.05681](https://arxiv.org/abs/1812.05681)

Phys. Rev. D99 (2019) no.3, 035001

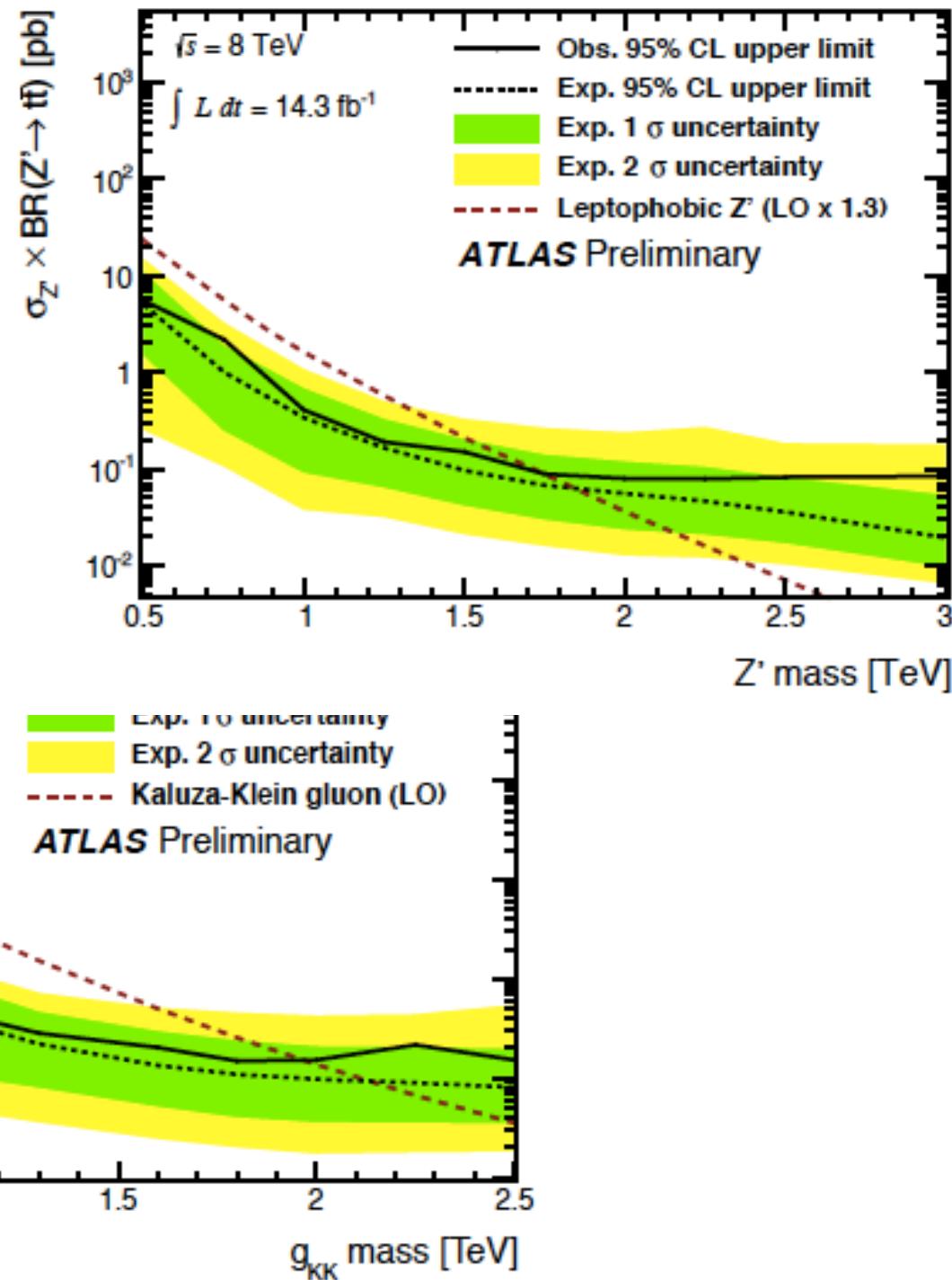


$Z' \rightarrow t\bar{t}$

$G \rightarrow t\bar{t}$

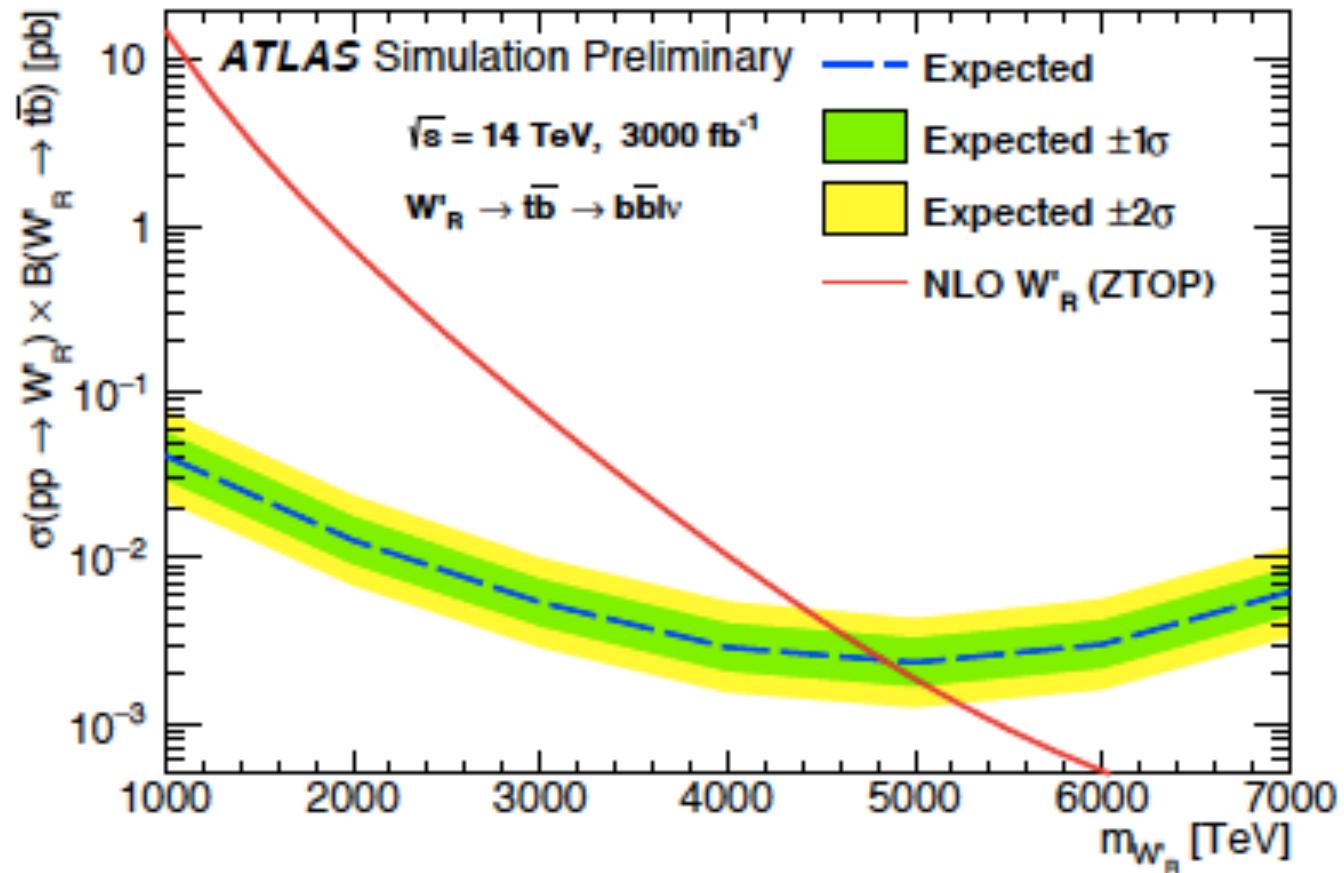
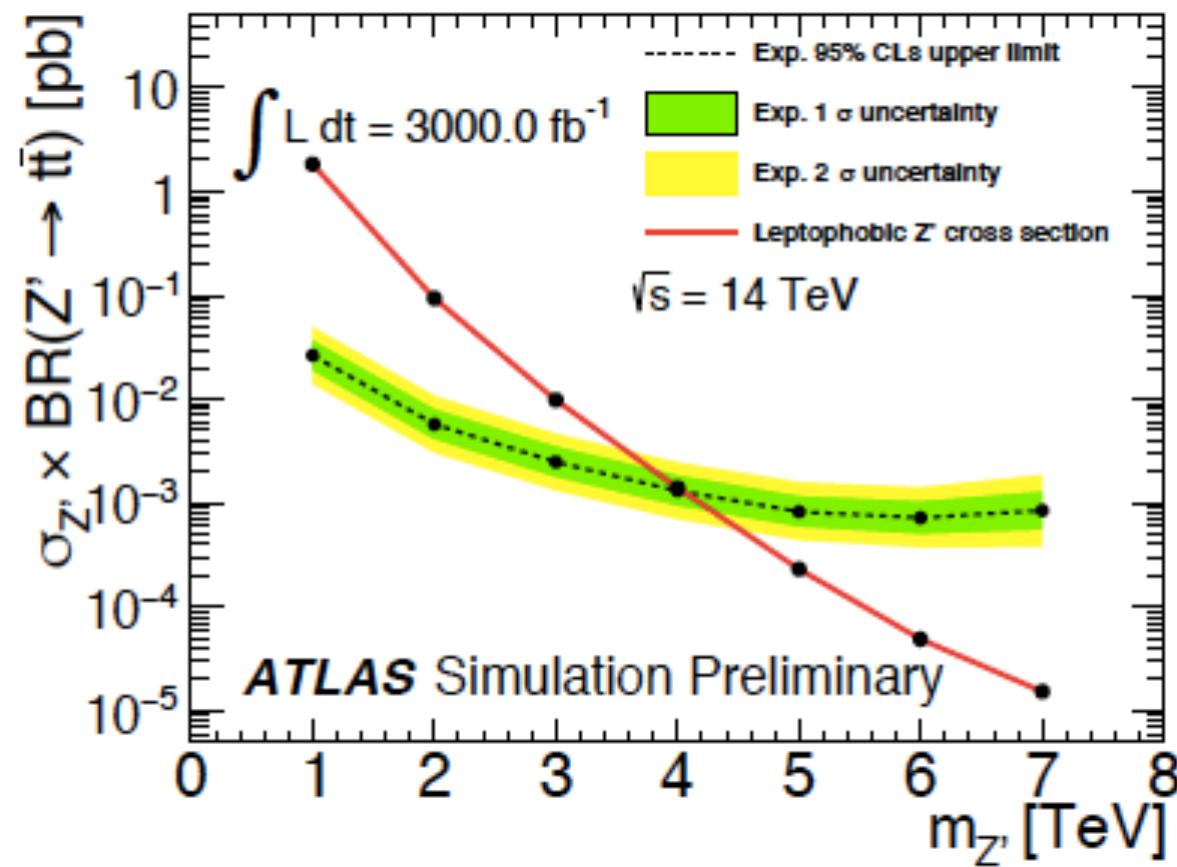


Limits are much weaker compared to di-jet and di-lepton channels

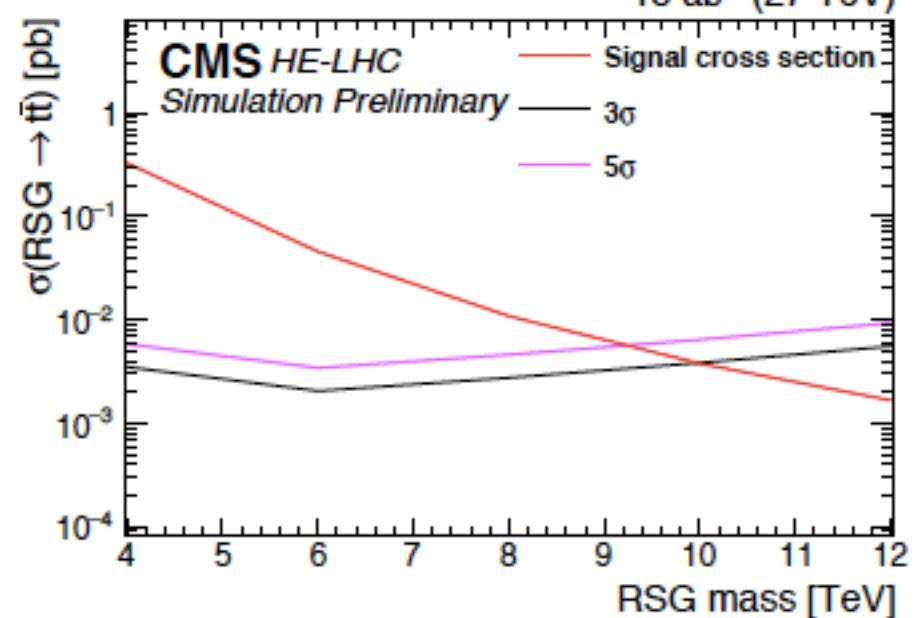
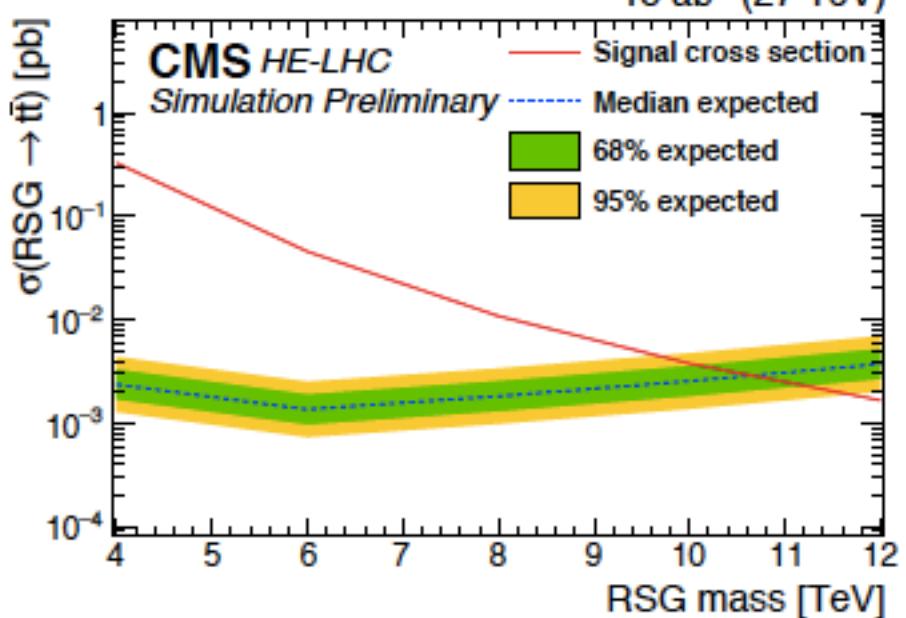
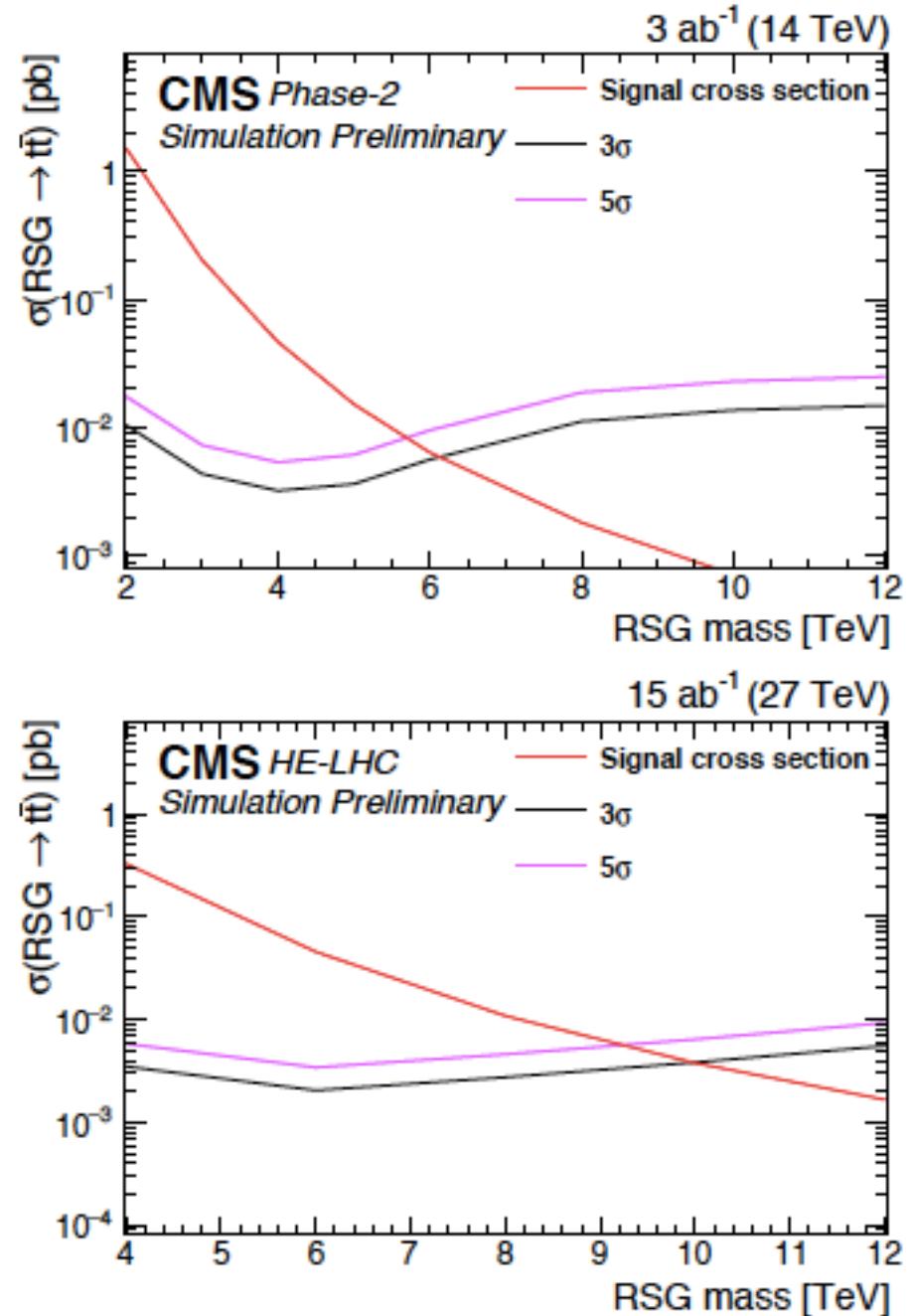
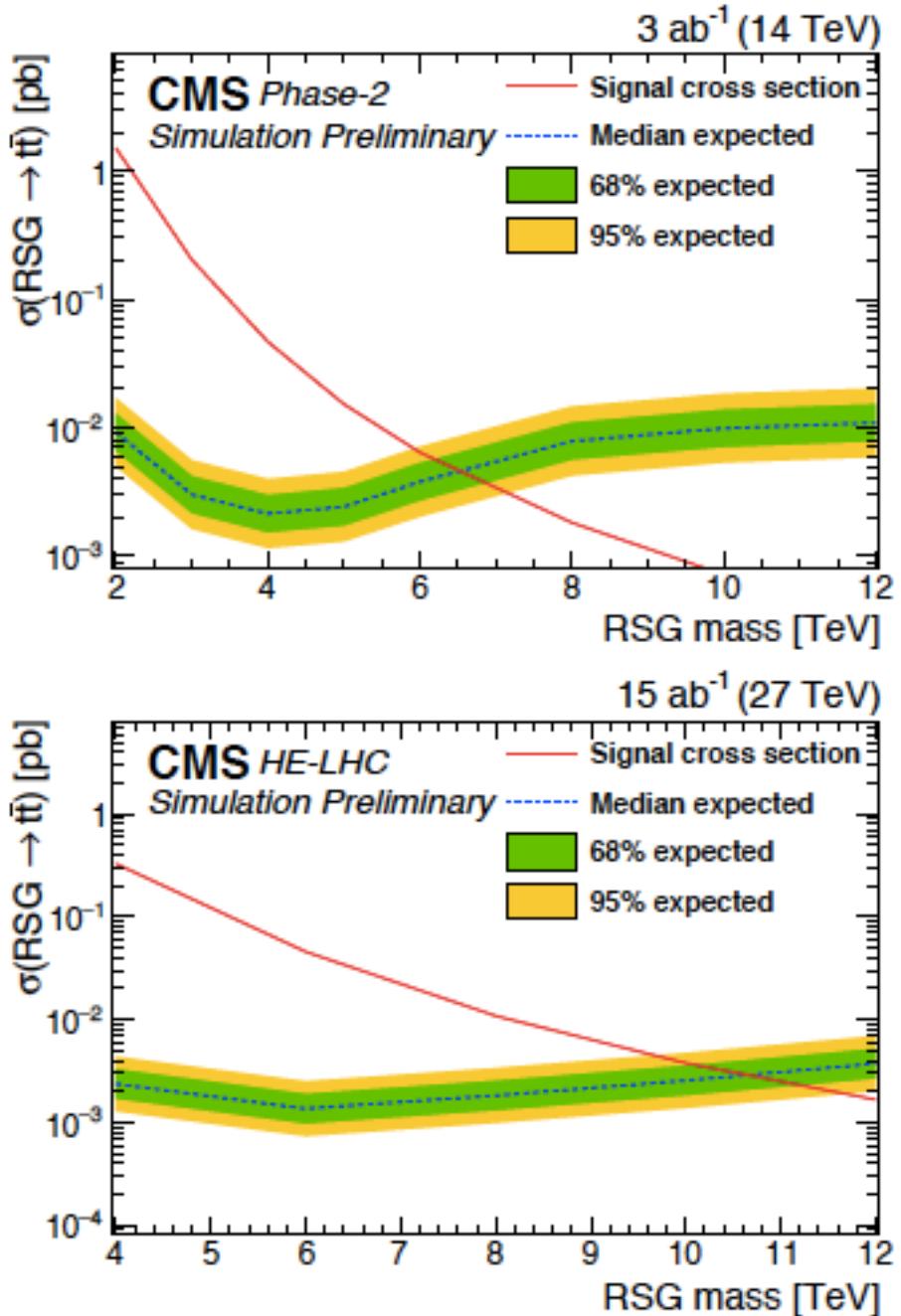


High Luminosity LHC expectations

arXiv: 1812.07831

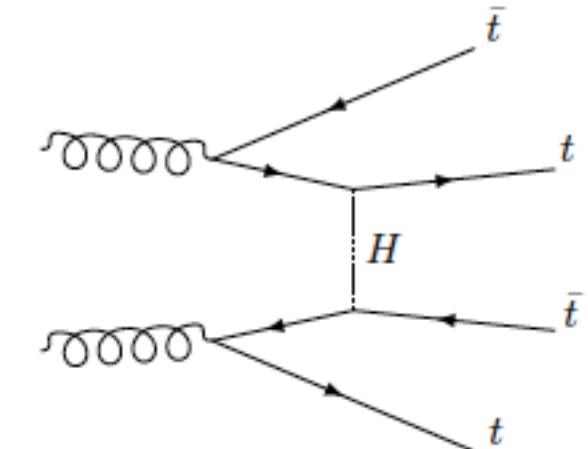
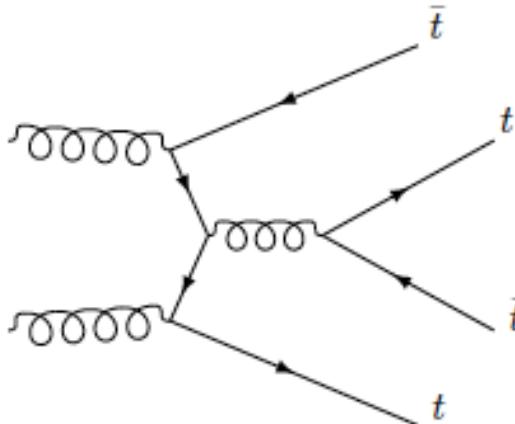


Spin-2 Resonance at HL-LHC and HE-LHC



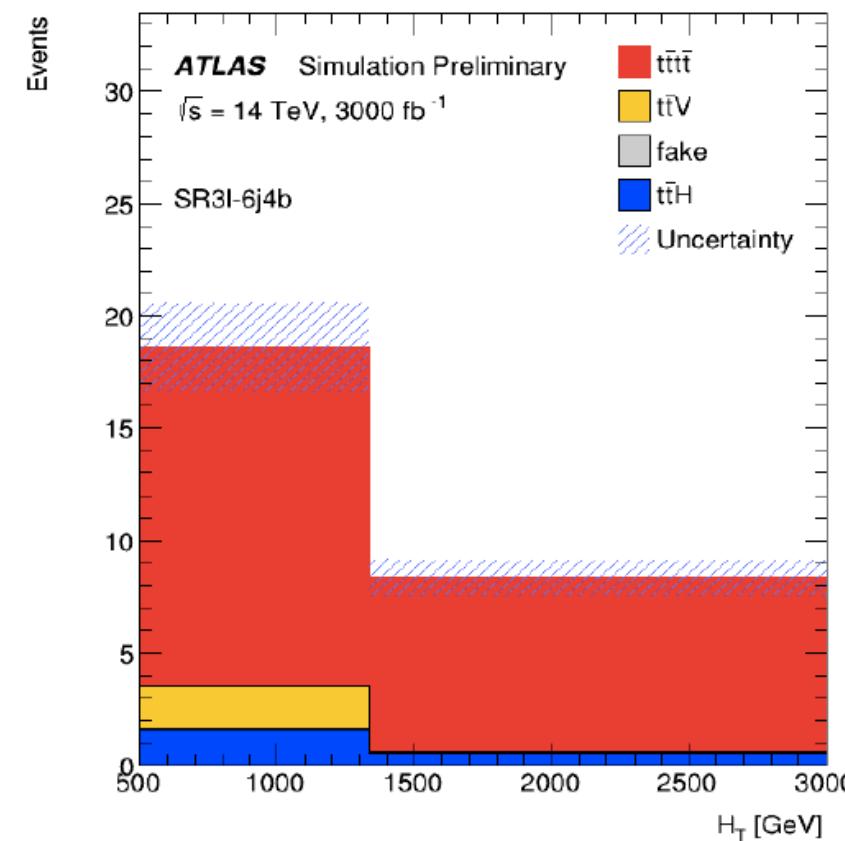
Four Top production at the LHC

$$\sigma(pp \rightarrow t\bar{t}t\bar{t}) = 15.83^{+18\%}_{-21\%} \text{ fb at 14 TeV}$$

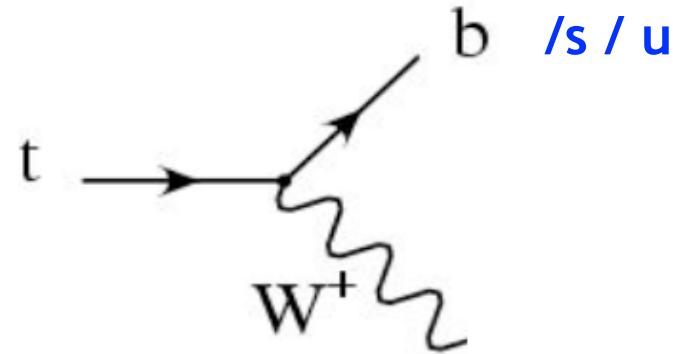


Explores top-top scattering

New physics possibilities not studied well.



Standard Decays of Top quark



$$\Gamma_t = \frac{G_F M_{\text{top}}^3}{8 \pi \sqrt{2}} |V_{tb}|^2 \left(1 - \frac{M_W^2}{M_{\text{top}}^2}\right)^2 \left(1 + 2 \frac{M_W^2}{M_{\text{top}}^2}\right)$$

$$|V_{tb}| = 1.019 \pm 0.028$$

$$|V_{ts}| = (39.4 \pm 2.3) \times 10^{-3}$$

$$|V_{td}| = (8.1 \pm 0.5) \times 10^{-3}$$

PDG, Phys.Rev. D98 (2018) no.3, 030001

Almost 100% decay to bW

Rare top decays

1) rare top decays (flavor changing neutral currents)

2 body decays: $t \rightarrow c\gamma$, $t \rightarrow cg$, $t \rightarrow cZ$, $t \rightarrow ch$
 $t \rightarrow u\gamma$, $t \rightarrow ug$, $t \rightarrow uZ$, $t \rightarrow uh$

3 body decays: $t \rightarrow c\gamma h$, $t \rightarrow cgh$, $t \rightarrow cl^+l^-$, ...
 $t \rightarrow u\gamma h$, $t \rightarrow ugh$, $t \rightarrow ul^+l^-$, ...

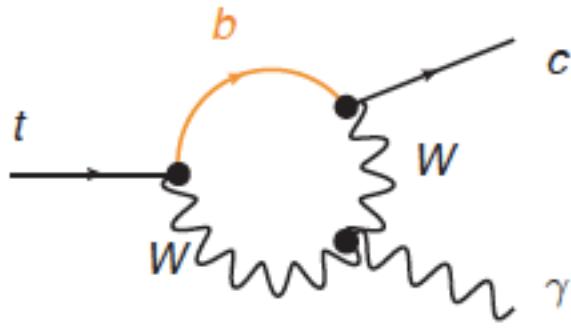
2) exotic top decays (into new physics particles)

light charged Higgs: $t \rightarrow H^\pm b$, $t \rightarrow H^\pm s$, $t \rightarrow H^\pm d$
light neutral gauge boson: $t \rightarrow Z'c$, $t \rightarrow Z'u$
dark matter: $t \rightarrow \chi\chi c$, $t \rightarrow \chi\chi u$

$$\Gamma_t \simeq \frac{g_2^2}{64\pi} \left(\frac{m_t}{m_W} \right)^2 |V_{tb}|^2 m_t$$

top FCNCs are 1-loop suppressed, CKM suppressed
and strongly GIM suppressed

Standard channel



$$\mathcal{A}_{t \rightarrow c\gamma} \propto \frac{e}{16\pi^2} \frac{G_F}{\sqrt{2}} \frac{m_b^2}{m_W^2} V_{tb} V_{cb}^*$$

$$\rightarrow \text{BR}(t \rightarrow c\gamma)_{\text{SM}} \simeq 5 \times 10^{-14}$$

(Aguilar-Saavedra hep-ph/0409342)

$$\text{BR}(t \rightarrow c\gamma) \simeq 5 \times 10^{-14} , \quad \text{BR}(t \rightarrow u\gamma) \simeq 4 \times 10^{-16}$$

$$\text{BR}(t \rightarrow cg) \simeq 5 \times 10^{-12} , \quad \text{BR}(t \rightarrow ug) \simeq 4 \times 10^{-14}$$

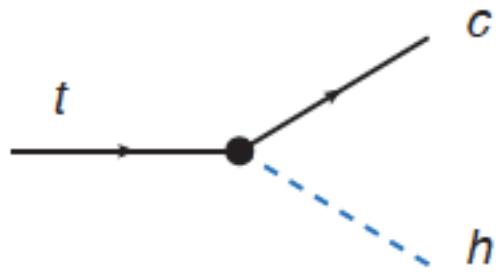
$$\text{BR}(t \rightarrow cZ) \simeq 1 \times 10^{-14} , \quad \text{BR}(t \rightarrow uZ) \simeq 8 \times 10^{-17}$$

$$\text{BR}(t \rightarrow ch) \simeq 3 \times 10^{-15} , \quad \text{BR}(t \rightarrow uh) \simeq 2 \times 10^{-17}$$

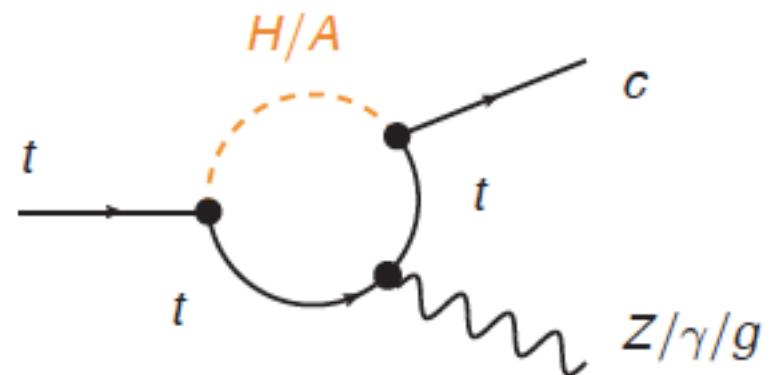
SM predictions

Beyond the SM

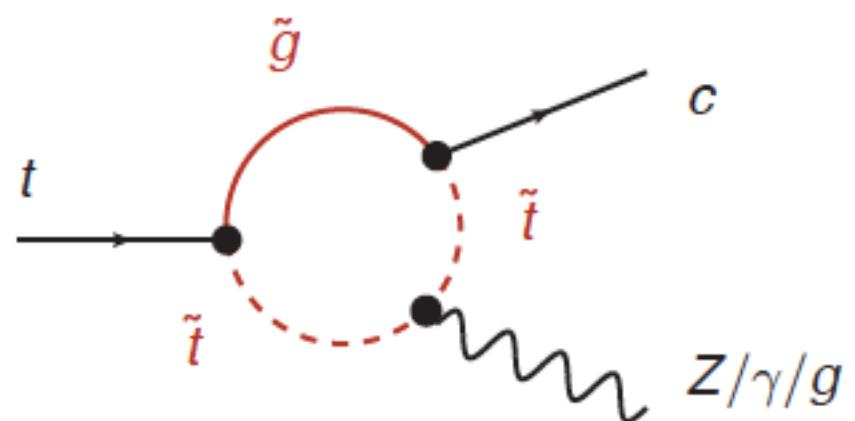
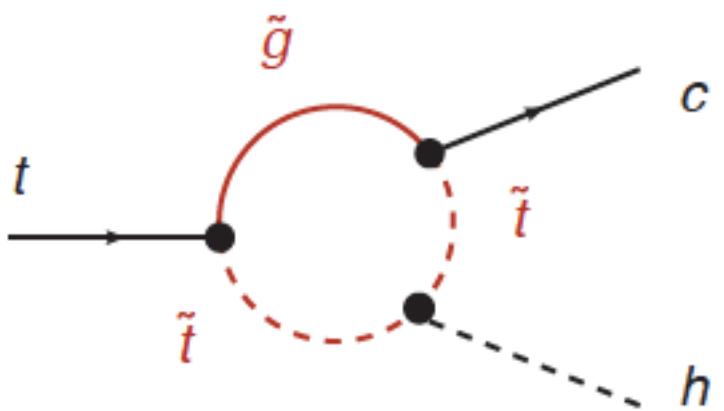
2HDM



$t \rightarrow c \ Z/\gamma/g$ at the 1 loop level



MSSM

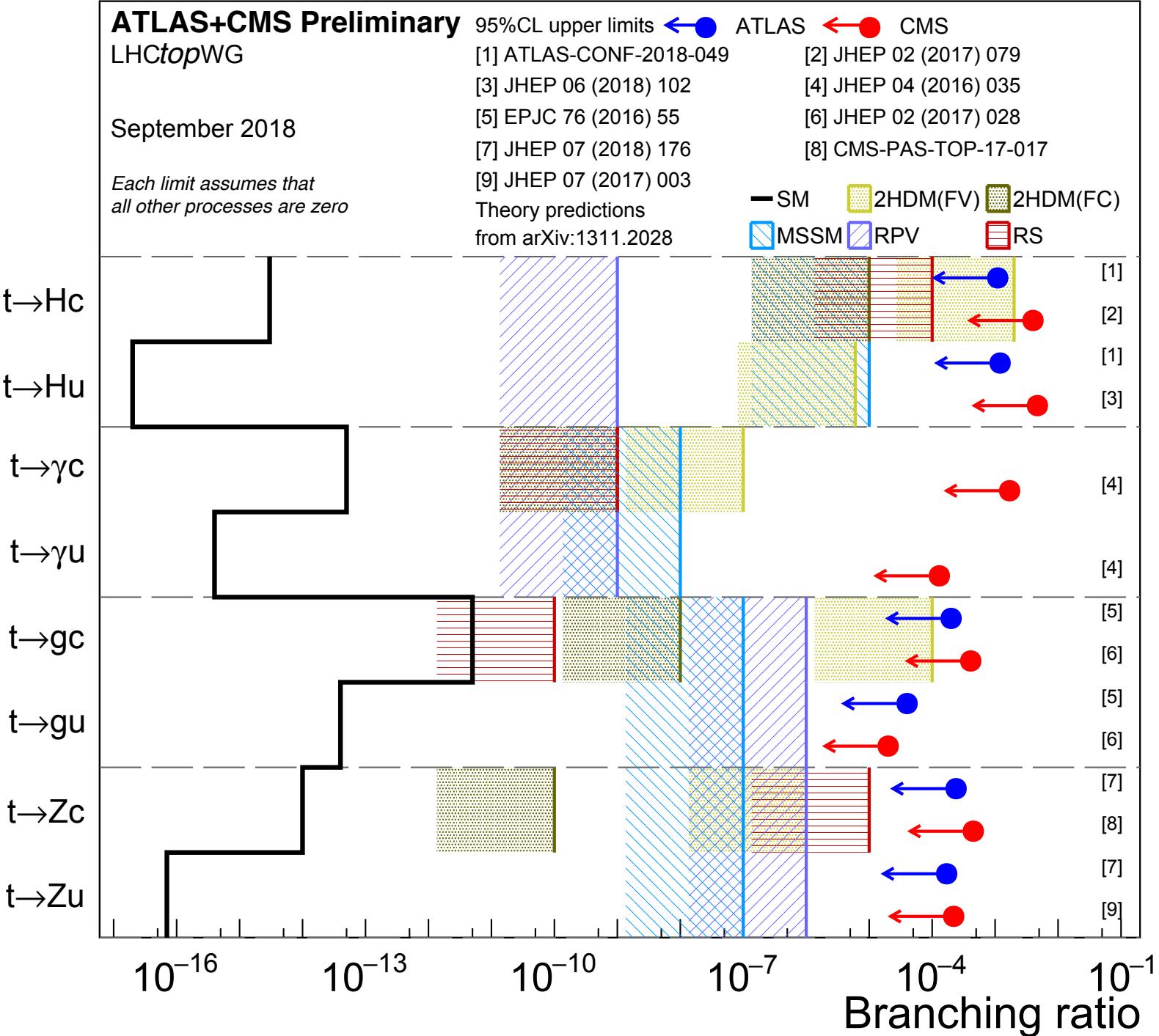


Present Experimental status and comparison with model predictions

Assuming only one
such coupling present at a time

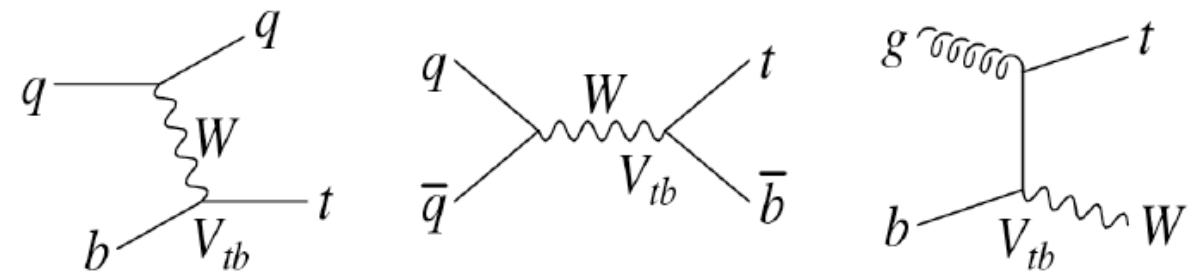
Top Working Group Summary Plots

ATL-PHYS-PUB-2018-034

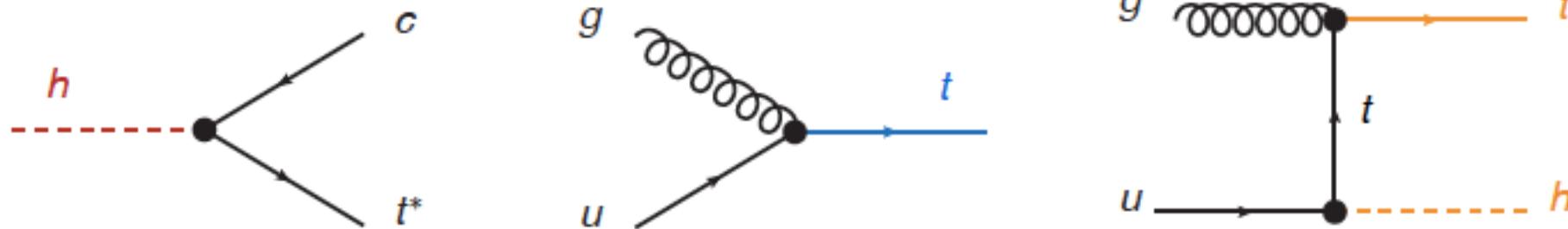


Apart from non-standard decays, large FCNC can invoke rare production channels

Standard Single top productions



Non-Standard Single top productions include

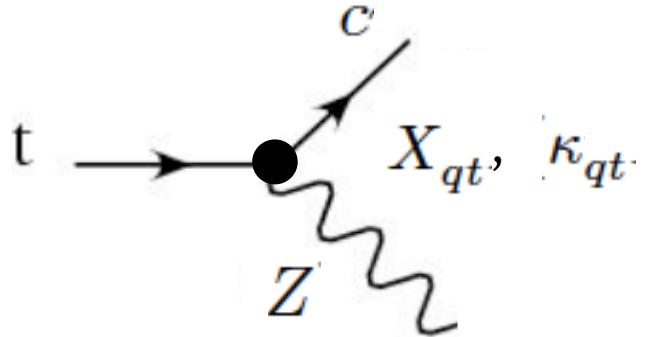


Chen, Hou, Kao, Kohda 1304.8037; Atwood, Gupta, Soni 1305.2427

Greljo, Kamenik, Kopp 1404.1278; ...

Model Independent - Effective couplings

$$\begin{aligned} -\mathcal{L}_{tqZ(\gamma)} = & \frac{g}{2c_W} \bar{q} \gamma^\mu (X_{qt}^L P_L + X_{qt}^R P_R) t Z_\mu + \frac{g}{2c_W} \bar{q} \frac{i\sigma^{\mu\nu} q_\nu}{m_t} (\kappa_{qt}^L P_L + \kappa_{qt}^R P_R) t Z_\mu \\ & + e \bar{q} \frac{i\sigma^{\mu\nu} q_\nu}{m_t} (\kappa_{qt}^L(\gamma) P_L + \kappa_{qt}^R(\gamma) P_R) t A_\mu + \text{H.c.} \end{aligned}$$



$$\Gamma(t \rightarrow qZ)_\gamma = \frac{\alpha}{32 s_W^2 c_W^2} |X_{qt}|^2 \frac{m_t^3}{M_Z^2} \left[1 - \frac{M_Z^2}{m_t^2} \right]^2 \left[1 + 2 \frac{M_Z^2}{m_t^2} \right],$$

$$\Gamma(t \rightarrow qZ)_\sigma = \frac{\alpha}{16 s_W^2 c_W^2} |\kappa_{qt}|^2 m_t \left[1 - \frac{M_Z^2}{m_t^2} \right]^2 \left[2 + \frac{M_Z^2}{m_t^2} \right],$$

$$\Gamma(t \rightarrow q\gamma) = \frac{\alpha}{2} |\lambda_{qt}|^2 m_t,$$

$$\Gamma(t \rightarrow qg) = \frac{2\alpha_s}{3} |\zeta_{qt}|^2 m_t,$$

$$\Gamma(t \rightarrow qH) = \frac{\alpha}{32 s_W^2} |g_{qt}|^2 m_t \left[1 - \frac{M_H^2}{m_t^2} \right]^2.$$

$$\begin{aligned} \text{Br}(t \rightarrow qZ)_\gamma &= 0.472 X_{qt}^2, \\ \text{Br}(t \rightarrow qZ)_\sigma &= 0.367 \kappa_{qt}^2, \\ \text{Br}(t \rightarrow q\gamma) &= 0.428 \lambda_{qt}^2, \\ \text{Br}(t \rightarrow qg) &= 7.93 \zeta_{qt}^2, \\ \text{Br}(t \rightarrow qH) &= 3.88 \times 10^{-2} g_{qt}^2 \end{aligned}$$

Current Limits:

$Br(t \rightarrow Zu(c)) < 1.7(2.4) \times 10^{-4}$	$\Rightarrow X_{qt}, \kappa_{qt}^L < 0.02$	ATLAS	JHEP 07 (2018) 176
$BR(t \rightarrow ug) \leq 4.0 \times 10^{-5}$	< 0.002	ATLAS	Eur.Phys. J.C. 76 (2016) 55
$BR(t \rightarrow cg) \leq 2.0 \times 10^{-4}$	< 0.005		
$BR(t \rightarrow u\gamma) \leq 1.3 \times 10^{-4}$	< 0.017	ATLAS	JHEP 04 (2016) 35
$BR(t \rightarrow c\gamma) \leq 1.7 \times 10^{-3}$	< 0.063		
$BR(t \rightarrow uH) \leq 2.4 \times 10^{-3}$	< 0.025	ATLAS	JHEP 1710 (2017) 120
$BR(t \rightarrow cH) \leq 2.2 \times 10^{-3}$	< 0.024		

Expectations at HL-LHC (3 /ab)

$$BR(t \rightarrow cZ) \leq 5.8 \times 10^{-5} \quad BR(t \rightarrow uZ) \leq 4.3 \times 10^{-5} \quad BR(t \rightarrow q\gamma) \leq 2.5 \times 10^{-5}$$

$$t \rightarrow Hq \leq 1.2 \times 10^{-4}$$

ATL-PHYS-PUB-2016-019

ATL-PHYS-PUB-2013-007

Process	Br Limit	Search	Dataset	Reference
$t \rightarrow Zq$	2.2×10^{-4}	ATLAS $t\bar{t} \rightarrow Wb + Zq \rightarrow \ell\nu b + \ell\ell q$	$300 \text{ fb}^{-1}, 14 \text{ TeV}$	[140]
$t \rightarrow Zq$	7×10^{-5}	ATLAS $t\bar{t} \rightarrow Wb + Zq \rightarrow \ell\nu b + \ell\ell q$	$3000 \text{ fb}^{-1}, 14 \text{ TeV}$	[140]
$t \rightarrow Zq$	$5(2) \times 10^{-4}$	ILC single top, $\gamma_\mu (\sigma_{\mu\nu})$	$500 \text{ fb}^{-1}, 250 \text{ GeV}$	Extrap.
$t \rightarrow Zq$	$1.5(1.1) \times 10^{-4(-5)}$	ILC single top, $\gamma_\mu (\sigma_{\mu\nu})$	$500 \text{ fb}^{-1}, 500 \text{ GeV}$	[141]
$t \rightarrow Zq$	$1.6(1.7) \times 10^{-3}$	ILC $t\bar{t}, \gamma_\mu (\sigma_{\mu\nu})$	$500 \text{ fb}^{-1}, 500 \text{ GeV}$	[141]
$t \rightarrow \gamma q$	8×10^{-5}	ATLAS $t\bar{t} \rightarrow Wb + \gamma q$	$300 \text{ fb}^{-1}, 14 \text{ TeV}$	[140]
$t \rightarrow \gamma q$	2.5×10^{-5}	ATLAS $t\bar{t} \rightarrow Wb + \gamma q$	$3000 \text{ fb}^{-1}, 14 \text{ TeV}$	[140]
$t \rightarrow \gamma q$	6×10^{-5}	ILC single top	$500 \text{ fb}^{-1}, 250 \text{ GeV}$	Extrap.
$t \rightarrow \gamma q$	6.4×10^{-6}	ILC single top	$500 \text{ fb}^{-1}, 500 \text{ GeV}$	[141]
$t \rightarrow \gamma q$	1.0×10^{-4}	ILC $t\bar{t}$	$500 \text{ fb}^{-1}, 500 \text{ GeV}$	[141]
$t \rightarrow gu$	4×10^{-6}	ATLAS $qg \rightarrow t \rightarrow Wb$	$300 \text{ fb}^{-1}, 14 \text{ TeV}$	Extrap.
$t \rightarrow gu$	1×10^{-6}	ATLAS $qg \rightarrow t \rightarrow Wb$	$3000 \text{ fb}^{-1}, 14 \text{ TeV}$	Extrap.
$t \rightarrow gc$	1×10^{-5}	ATLAS $qg \rightarrow t \rightarrow Wb$	$300 \text{ fb}^{-1}, 14 \text{ TeV}$	Extrap.
$t \rightarrow gc$	4×10^{-6}	ATLAS $qg \rightarrow t \rightarrow Wb$	$3000 \text{ fb}^{-1}, 14 \text{ TeV}$	Extrap.
$t \rightarrow hq$	2×10^{-3}	LHC $t\bar{t} \rightarrow Wb + hq \rightarrow \ell\nu b + \ell\ell q X$	$300 \text{ fb}^{-1}, 14 \text{ TeV}$	Extrap.
$t \rightarrow hq$	5×10^{-4}	LHC $t\bar{t} \rightarrow Wb + hq \rightarrow \ell\nu b + \ell\ell q X$	$3000 \text{ fb}^{-1}, 14 \text{ TeV}$	Extrap.
$t \rightarrow hq$	5×10^{-4}	LHC $t\bar{t} \rightarrow Wb + hq \rightarrow \ell\nu b + \gamma\gamma q$	$300 \text{ fb}^{-1}, 14 \text{ TeV}$	Extrap.
$t \rightarrow hq$	2×10^{-4}	LHC $t\bar{t} \rightarrow Wb + hq \rightarrow \ell\nu b + \gamma\gamma q$	$3000 \text{ fb}^{-1}, 14 \text{ TeV}$	Extrap.

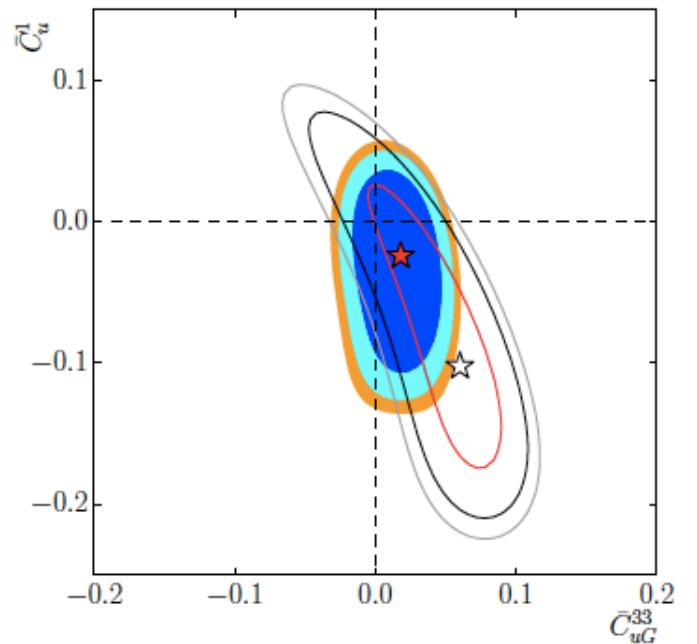
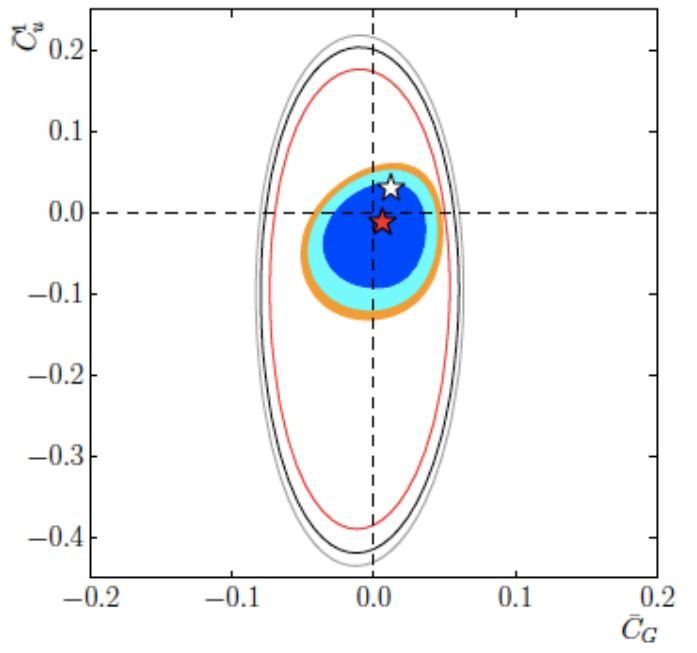
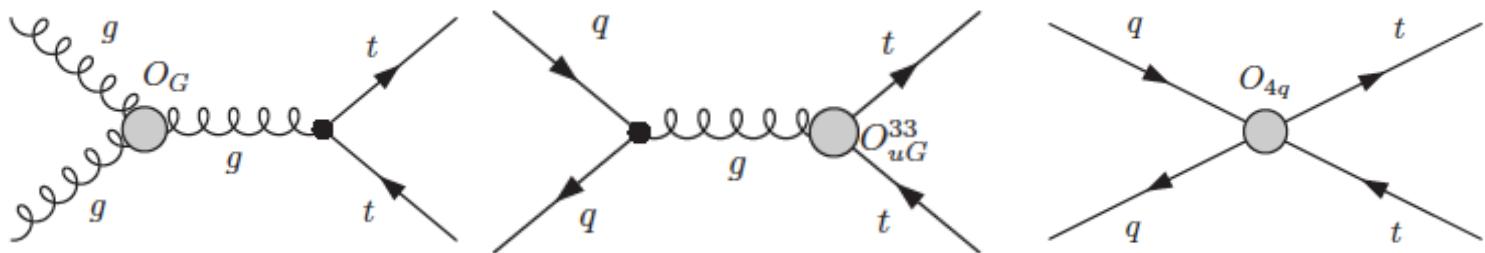
NP through Effective Lagrangian (SMEFT) Anomalous Couplings

$$\mathcal{L} = \mathcal{L}^{SM} + \sum \frac{c_i}{\Lambda^2} \mathcal{O}_i + O\left(\frac{1}{\Lambda^4}\right)$$

TopFitter Collaboration
1512.03360

$$\begin{aligned} \mathcal{L}_{D6} \supset & \frac{C_{uG}}{\Lambda^2} (\bar{q} \sigma^{\mu\nu} T^A u) \tilde{\varphi} G_{\mu\nu}^A + \frac{C_G}{\Lambda^2} f_{ABC} G_\mu^{A\nu} G_\nu^{B\lambda} G_\lambda^{C\mu} + \frac{C_{\varphi G}}{\Lambda^2} (\varphi^\dagger \varphi) G_{\mu\nu}^A G^{A\mu\nu} \\ & + \frac{C_{qq}^{(1)}}{\Lambda^2} (\bar{q} \gamma_\mu q) (\bar{q} \gamma^\mu q) + \frac{C_{qq}^{(3)}}{\Lambda^2} (\bar{q} \gamma_\mu \tau^I q) (\bar{q} \gamma^\mu \tau^I q) + \frac{C_{uu}}{\Lambda^2} (\bar{u} \gamma_\mu u) (\bar{u} \gamma^\mu u) \\ & + \frac{C_{qu}^{(8)}}{\Lambda^2} (\bar{q} \gamma_\mu T^A q) (\bar{u} \gamma^\mu T^A u) + \frac{C_{qd}^{(8)}}{\Lambda^2} (\bar{q} \gamma_\mu T^A q) (\bar{d} \gamma^\mu T^A d) + \frac{C_{ud}^{(8)}}{\Lambda^2} (\bar{u} \gamma_\mu T^A u) (\bar{d} \gamma^\mu T^A d) \end{aligned}$$

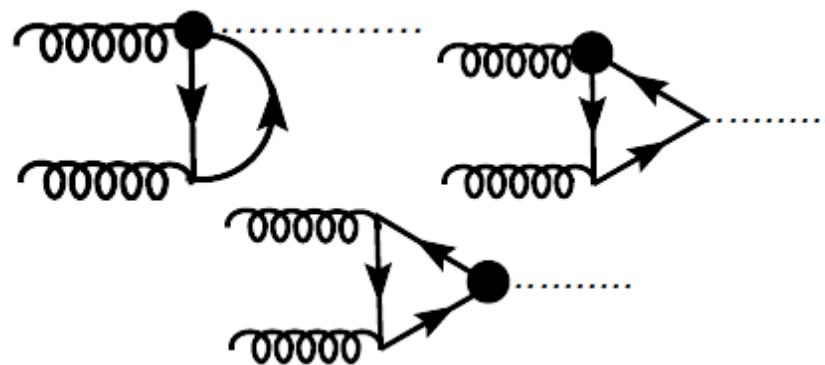
$$C_u^1 = C_{qq}^{(1)1331} + C_{uu}^{1331} + C_{qq}^{(3)1331}$$



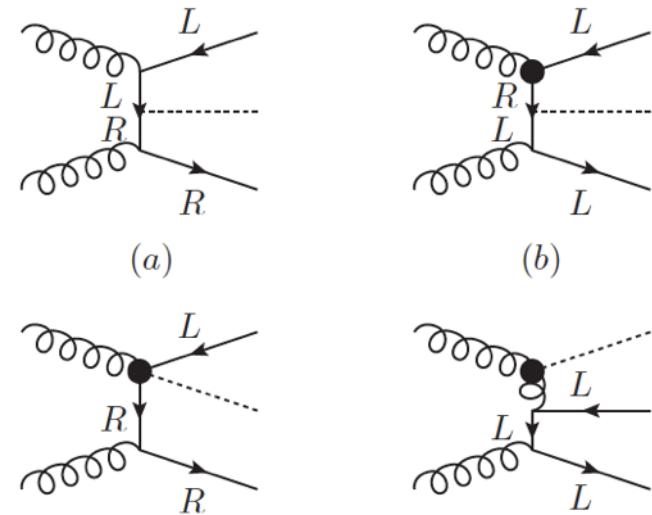
NP through Effective Lagrangian (SMEFT) Anomalous Couplings

$$\mathcal{L} = \mathcal{L}^{SM} + \sum \frac{c_i}{\Lambda^2} \mathcal{O}_i + O\left(\frac{1}{\Lambda^4}\right)$$

$$\begin{aligned} \mathcal{O}_{hg} &= (\bar{Q}_L H) \sigma^{\mu\nu} T^a t_R G_{\mu\nu}^a, & \mathcal{O}_{HG} &= \frac{1}{2} H^\dagger H G_{\mu\nu}^a G_a^{\mu\nu} \\ \mathcal{O}_{Hy} &= H^\dagger H (H \bar{Q}_L) t_R & \mathcal{O}_{H\gamma} &= \frac{1}{2} H^\dagger H F_{\mu\nu} F^{\mu\nu} \\ \mathcal{O}_{Ht} &= H^\dagger D_\mu H \bar{t}_R \gamma^\mu t_R & & \\ \mathcal{O}_{HQ} &= H^\dagger D_\mu H \bar{Q}_L \gamma^\mu Q_L & \mathcal{O}_H &= \partial_\mu (H^\dagger H) \partial^\mu (H^\dagger H) \\ \mathcal{O}_{HQ}^{(3)} &= H^\dagger \sigma^I D_\mu H \bar{Q}_L \sigma^I \gamma^\mu Q_L & & \end{aligned}$$



$$\sigma(gg \rightarrow h) = \sigma(gg \rightarrow h)_{SM} \left(1 + \frac{c_{HG}}{\Lambda^2} \frac{6\pi v^2}{\alpha_s}\right)^2$$

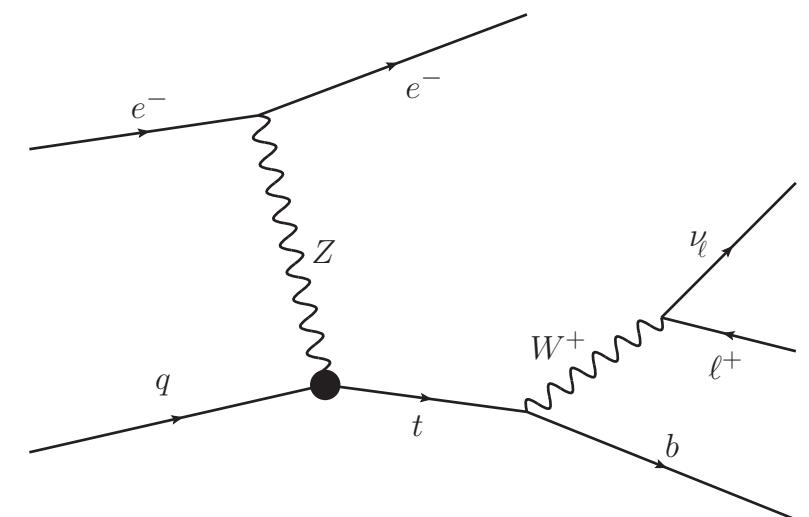
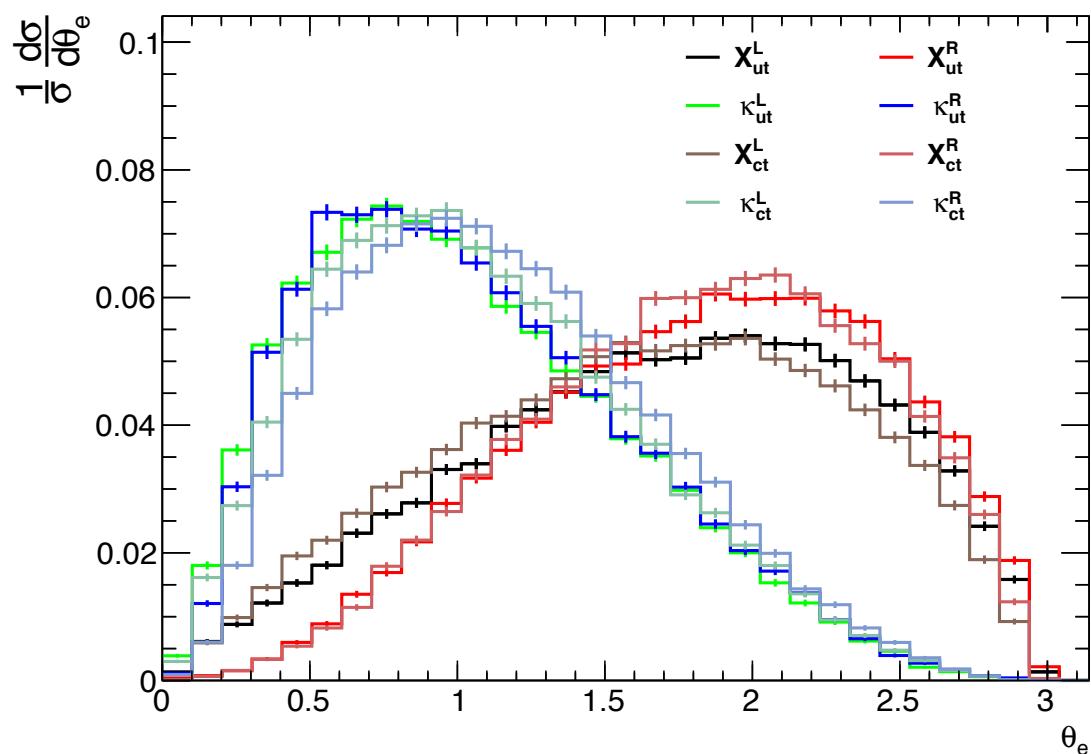


$$\begin{aligned} \mathcal{L}^{h\bar{t}t} &= \bar{t}t \frac{h}{\sqrt{2}} \left(y_t - \left(\frac{3}{2} \Re(c_{Hy}) + y_t c_H \right) \frac{v^2}{\Lambda^2} \right) \\ &= \bar{t}t h \frac{m_t}{v} \left(1 - c_y \frac{v^2}{\Lambda^2} \right), \end{aligned} \quad \sqrt{s} = 14 \text{ TeV}$$

$$\begin{aligned} \frac{\sigma(pp \rightarrow t\bar{t}h)}{\text{fb}} &= 611_{-110}^{+92} + [457_{-91}^{+127} \Re c_{hg} - 49_{-10}^{+15} c_G \\ &\quad + 147_{-32}^{+55} c_{HG} - 67_{-16}^{+23} c_y] \left(\frac{\text{TeV}}{\Lambda}\right)^2 \\ &\quad + [543_{-123}^{+143} (\Re c_{hg})^2 + 1132_{-232}^{+323} c_G^2 \\ &\quad + 85.5_{-21}^{+73} c_{HG}^2 + 2_{-0.5}^{+0.7} c_y^2] \\ &\quad + 233_{-144}^{+81} \Re c_{hg} c_{HG} - 50_{-14}^{+16} \Re c_{hg} c_y \\ &\quad - 3.2_{-8}^{+8} \Re c_{Hy} c_{HG} - 1.2_{-8}^{+8} c_H c_{HG}] \left(\frac{\text{TeV}}{\Lambda}\right)^4, \end{aligned} \quad (18)$$

C. Degrande, et al
JHEP 1207 (2012) 036,
1205.1065

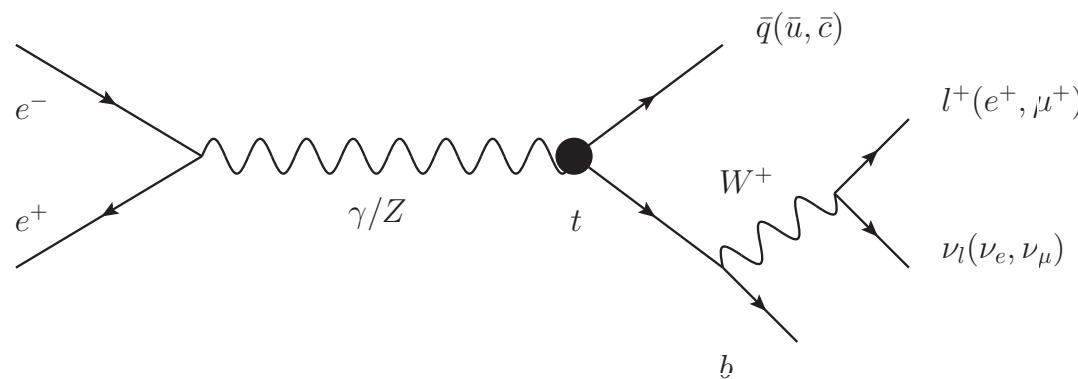
$$\begin{aligned}
 -\mathcal{L}_{\text{tqZ}(\gamma)} = & \frac{g}{2c_W} \bar{q} \gamma^\mu (X_{qt}^L P_L + X_{qt}^R P_R) t Z_\mu + \frac{g}{2c_W} \bar{q} \frac{i\sigma^{\mu\nu} q_\nu}{m_t} (\kappa_{qt}^L P_L + \kappa_{qt}^R P_R) t Z_\mu \\
 & + e \bar{q} \frac{i\sigma^{\mu\nu} q_\nu}{m_t} (\kappa_{qt}^L(\gamma) P_L + \kappa_{qt}^R(\gamma) P_R) t A_\mu + \text{H.c.}
 \end{aligned}$$



The scattered electron as a discriminator

Lorentz structure of the coupling can be probed.

Something quite hard at LHC



$$\begin{aligned}
 -\mathcal{L}_{tqZ(\gamma)} = & \frac{g}{2c_W} \bar{q} \gamma^\mu (X_{qt}^L P_L + X_{qt}^R P_R) t Z_\mu + \frac{g}{2c_W} \bar{q} \frac{i\sigma^{\mu\nu} q_\nu}{m_t} (\kappa_{qt}^L P_L + \kappa_{qt}^R P_R) t Z_\mu \\
 & + e \bar{q} \frac{i\sigma^{\mu\nu} q_\nu}{m_t} (\kappa_{qt}^L(\gamma) P_L + \kappa_{qt}^R(\gamma) P_R) t A_\mu + \text{H.c.}
 \end{aligned}$$

Coupling	$\kappa_{ut}^L(\gamma)$	$\kappa_{ut}^R(\gamma)$	X_{ut}^L	X_{ut}^R	κ_{ut}^L	κ_{ut}^R	$\kappa_{ct}^L(\gamma)$	$\kappa_{ct}^R(\gamma)$	X_{ct}^L	X_{ct}^R	κ_{ct}^L	κ_{ct}^R
σ_{unpol} (fb)	126.66	127.23	53.97	53.88	89.37	89.49	126.84	127.29	53.99	53.91	89.45	89.39
$\sigma(-80\%, +30\%)$ (fb)	156.5	156.3	77.97	78.09	131.8	131.7	156.5	156.3	77.97	78.09	131.8	131.7
$\sigma(+80\%, -30\%)$ (fb)	157.06	157.89	53.63	54.01	89.18	89.61	157.19	157.75	54.02	53.78	89.50	89.59

We studied the signal (1j + 1b-jet + 1 lepton + missing energy)
against the SM background.

Major Backgrounds

	cross section (pb)
1. $e^+e^- \rightarrow WW \rightarrow 2\ell 2\nu$	10.99
2. $e^+e^- \rightarrow ZZ \rightarrow 2\ell 2\nu + 2\ell 2j$	0.83
3. $e^+e^- \rightarrow Z \rightarrow 2j, 2b$	0.75
4. $e^+e^- \rightarrow 2e\gamma,$	14.79
5. $e^+e^- \rightarrow \mu^+\mu^- h.$	0.01

Process	N _{simulated}	$\sigma_{-8, +3}[fb]$	N _e
$\kappa_{ul}^L(\gamma)$	10000	156.5	3130
$\kappa_{ul}^R(\gamma)$	10000	156.3	3120
X_{ul}^L	10000	77.97	1559
X_{ul}^R	10000	78.09	1560
κ_{ul}^L	9500	131.8	2630
κ_{ul}^R	10000	131.7	2630
$e^-e^+ \rightarrow WW \rightarrow b\nu_l 2j$ 4f_WW_semileptonic	279897	10992.9	21985
$e^-e^+ \rightarrow ZZ \rightarrow 2l2j + 2\nu_l 2j$ 4f_ZZ_semileptonic	535103	856.927	1713
$e^-e^+ \rightarrow Z \rightarrow 2j + 2b$ 2f_Z_hadronic	476642	78046.5	15609
$e^-e^+ \rightarrow \mu^+(e^+)\mu^-(e^-)h$ higgs_ffh_Plhh	30126	10.651	213

signal

background

before after

263400	118134
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21985832	3533
1713854	1439

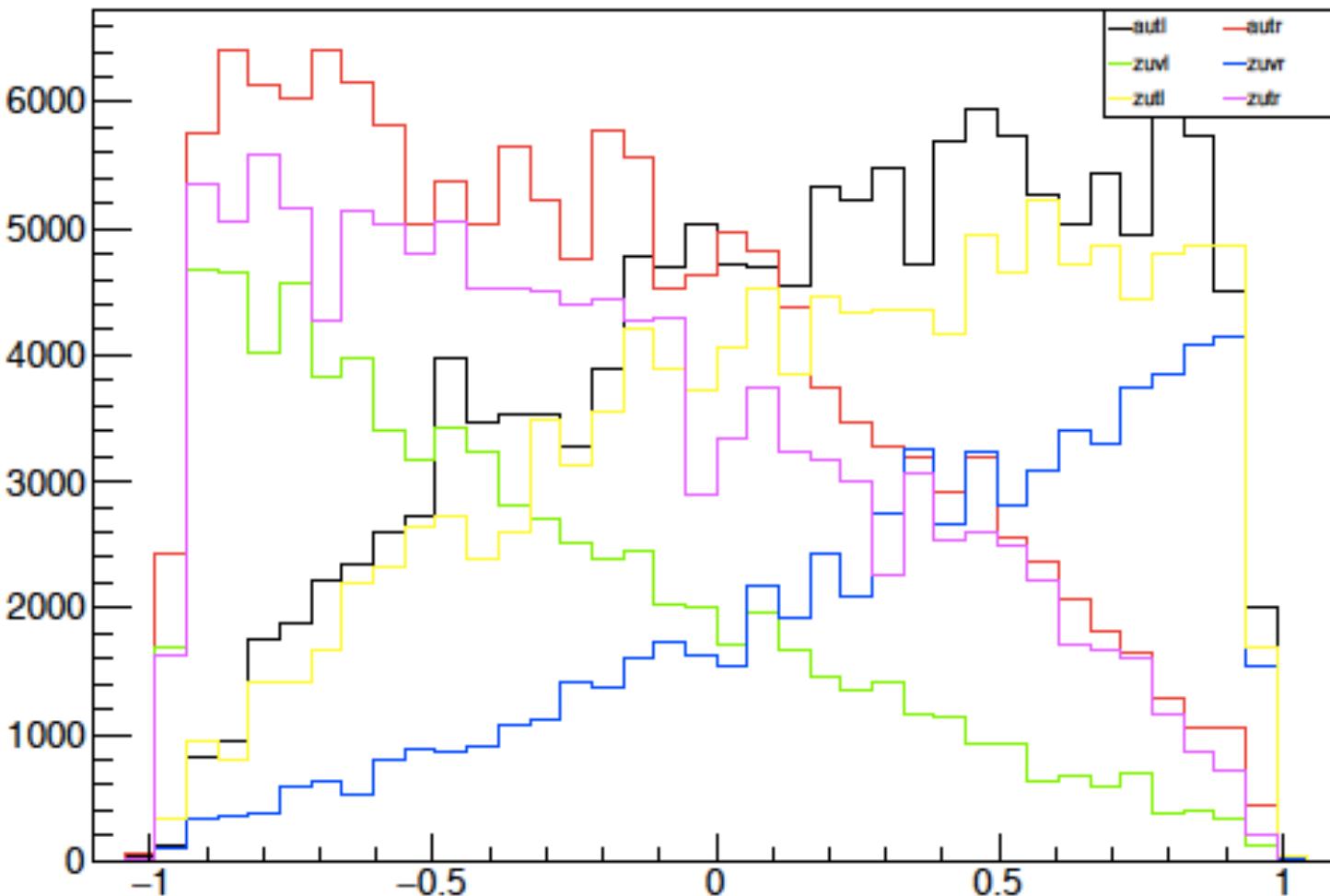
156092928	20
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21302	139
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$0 < m_t < 240$	$180 < M_{lj} < 270$	$M_{bj}/[85, 95]$	$ p_\nu > 20$	$\cos\theta_\mu < .95, \cos\theta_\nu > -.95$
176719	176344	142540	141789	138408
180088	179557	145046	144358	141607
90195	89899	75085	74757	73369
87757	87460	68328	67907	66735
151223	150862	122615	121886	119480
148952	148557	120558	120005	118134
18790	18511	3905	3533	3533
3802	3535	3215	1867	1439
2116	2116	41	41	20
243	238	237	168	139

Kinematic Selections to improve the signal significance.

80% left-polarised electron beam
30% right-polarised positron beam

_jet_Cos_th_zutr_maj_bkg

angular distribution of the light jet
is sensitive to the type of coupling

potential to distinguish the
Lorentz structure of the coupling

Summary

Apart from probing resonant production of new physics particle, precise measurement of top quark couplings can provide information of physics beyond the Standard Model.

Precise knowledge of the top quark couplings are essential to extract Higgs coupling information.

LHC producing plenty of top quark pairs, can perform precision measurements including rare top decays.

Other colliders like electron-proton collider, and the ILC can complement the LHC studies, and have the potential to provide additional informations like the Lorentz structure of the couplings, which are difficult to probe at the LHC.

Thank you