

# The Hubble Tension: A Particle Physics Perspective

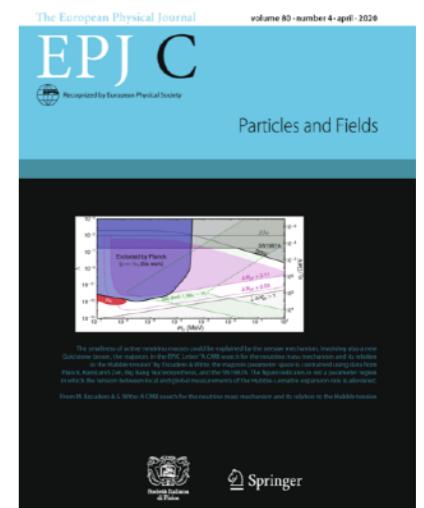
Miguel Escudero Abenza  
[miguel.escudero@tum.de](mailto:miguel.escudero@tum.de)

short review + original work based on:

[ArXiv:1909.04044](https://arxiv.org/abs/1909.04044), EPJC 80 (2020) 4, 294

[ArXiv:2004.01470](https://arxiv.org/abs/2004.01470), NuPhys19 Proceedings

[ArXiv:2103.03249](https://arxiv.org/abs/2103.03249), EPJC 81 (2021) 6, 515



with Sam Witte

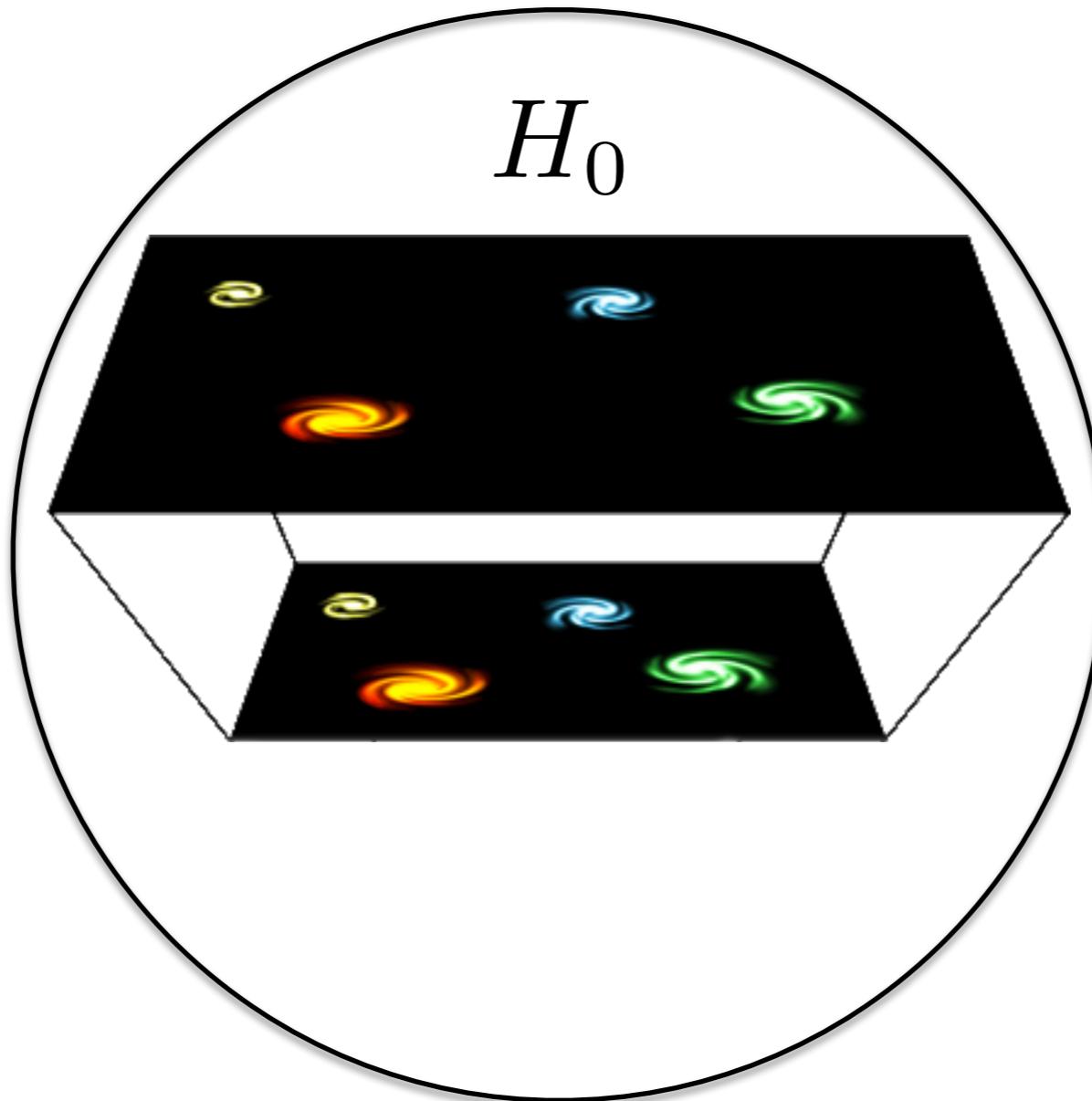


Indian Institute of Technology Mumbai  
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Stiftung / Foundation



Riess *et al.* 2112.04510

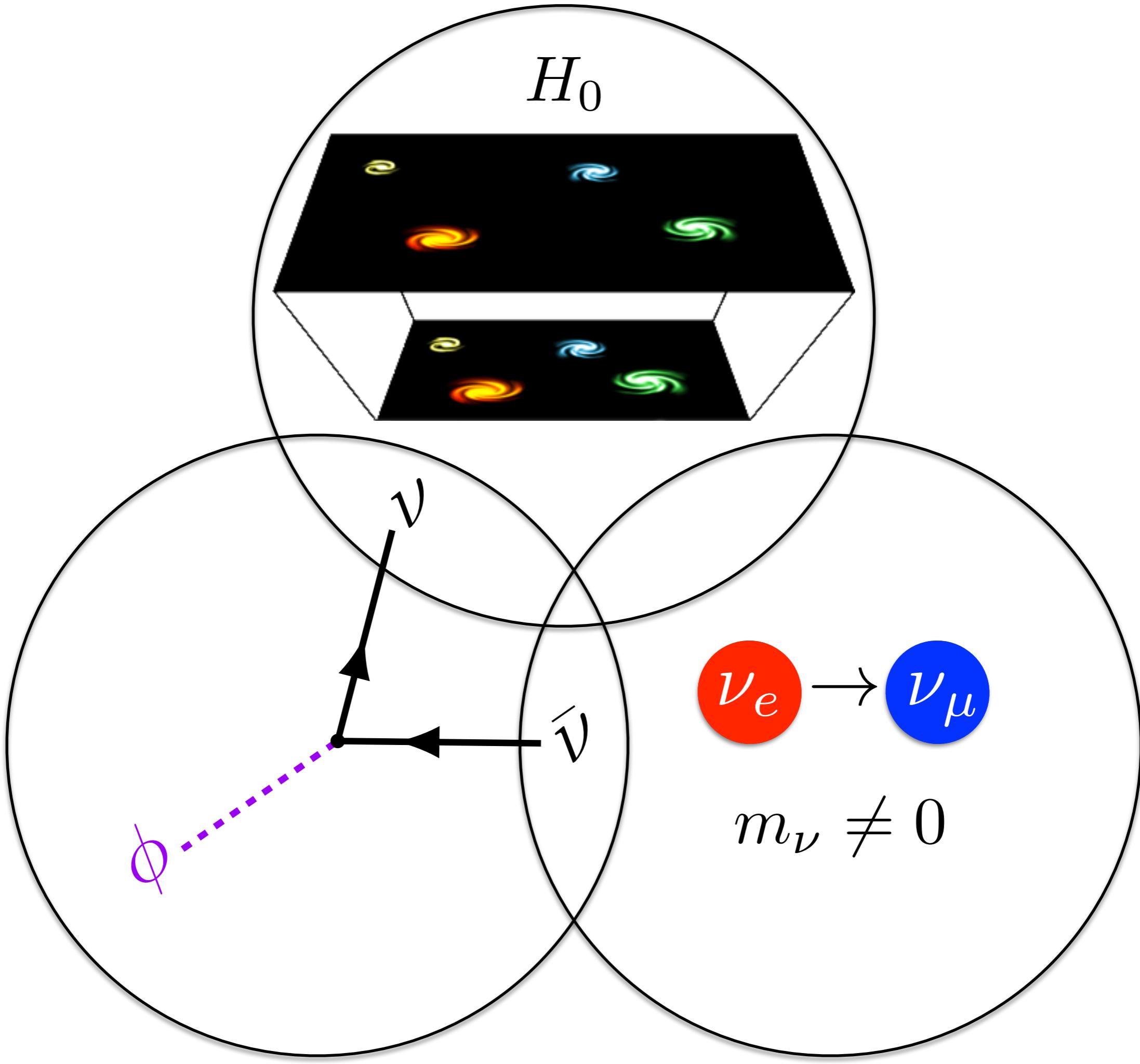
Local Measurements

$$H_0 = 73.04 \pm 1.04 \text{ km/s/Mpc}$$

$\Lambda$ CDM Prediction

$$H_0 = 67.4 \pm 0.5 \text{ km/s/Mpc}$$

5 $\sigma$  tension  
within  $\Lambda$ CDM!



# Outline

## 1) The Hubble Tension

**Observational Evidence**

**Brief review of Models**

## 2) The Majoron as a solution to the $H_0$ tension

**The singlet Majoron model**

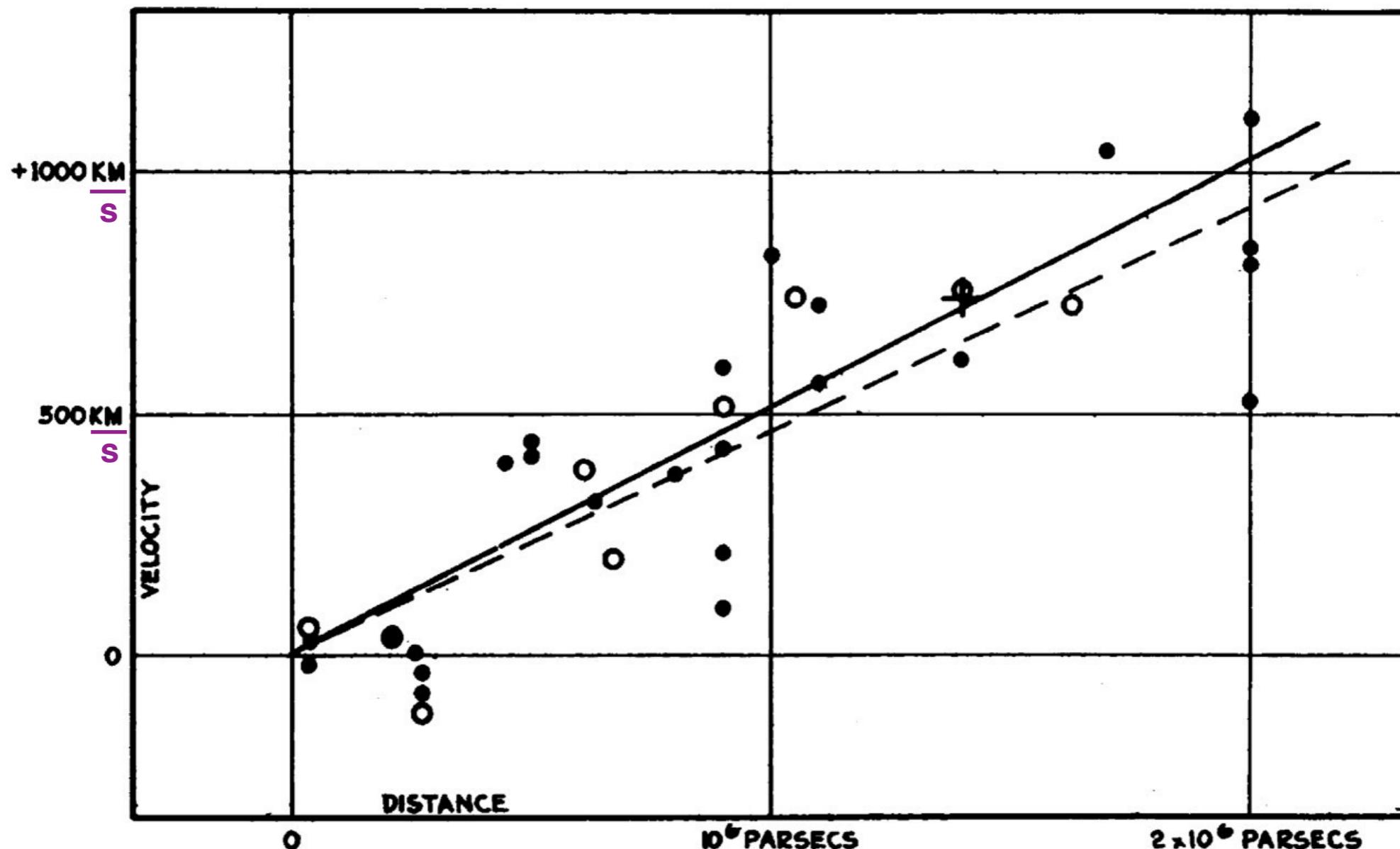
**Majoron Cosmology**

## 3) Conclusions and Outlook

# The Hubble Law

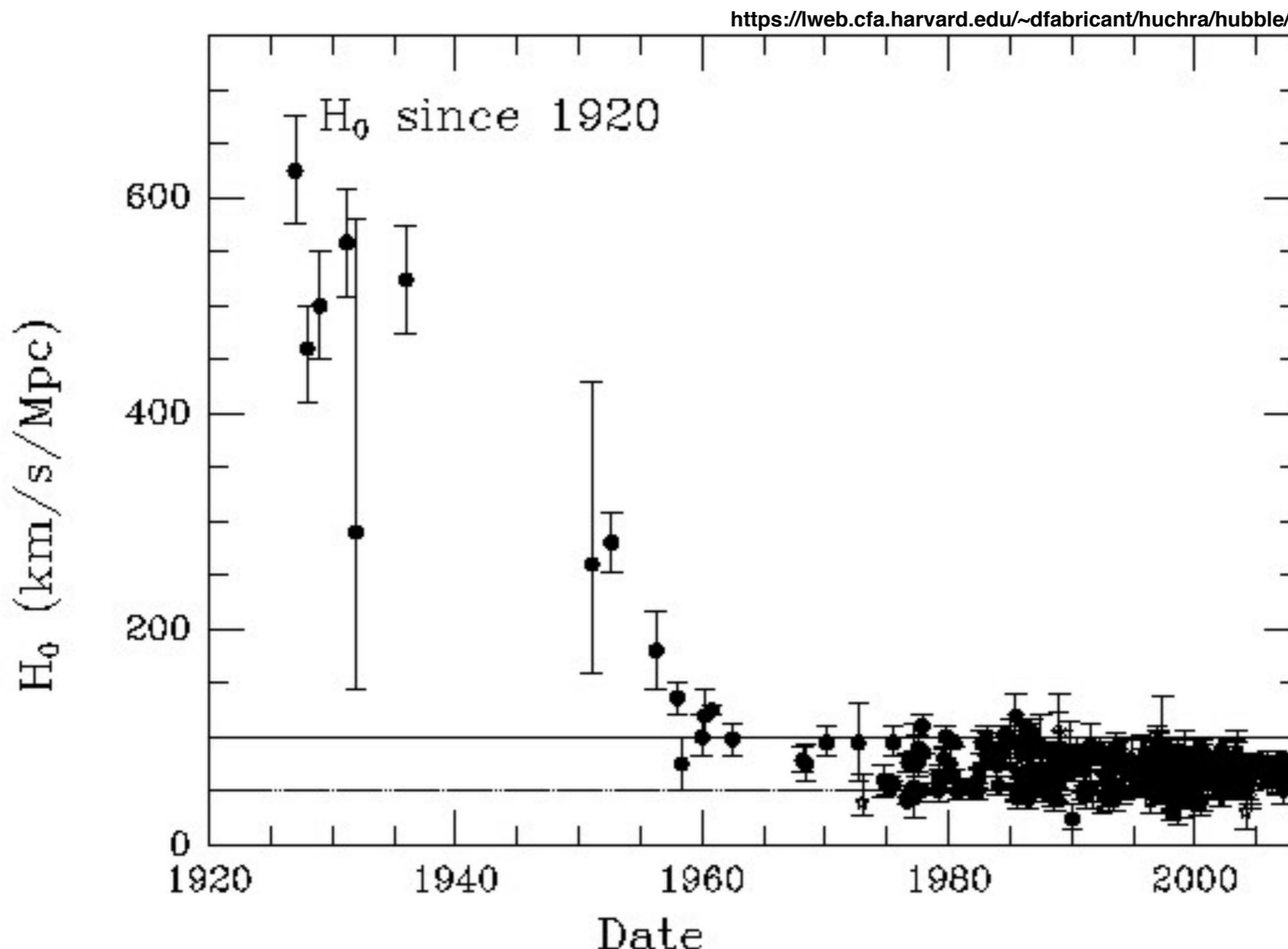
The Universe is expanding!

Hubble (1929):  $v = H_0 d$

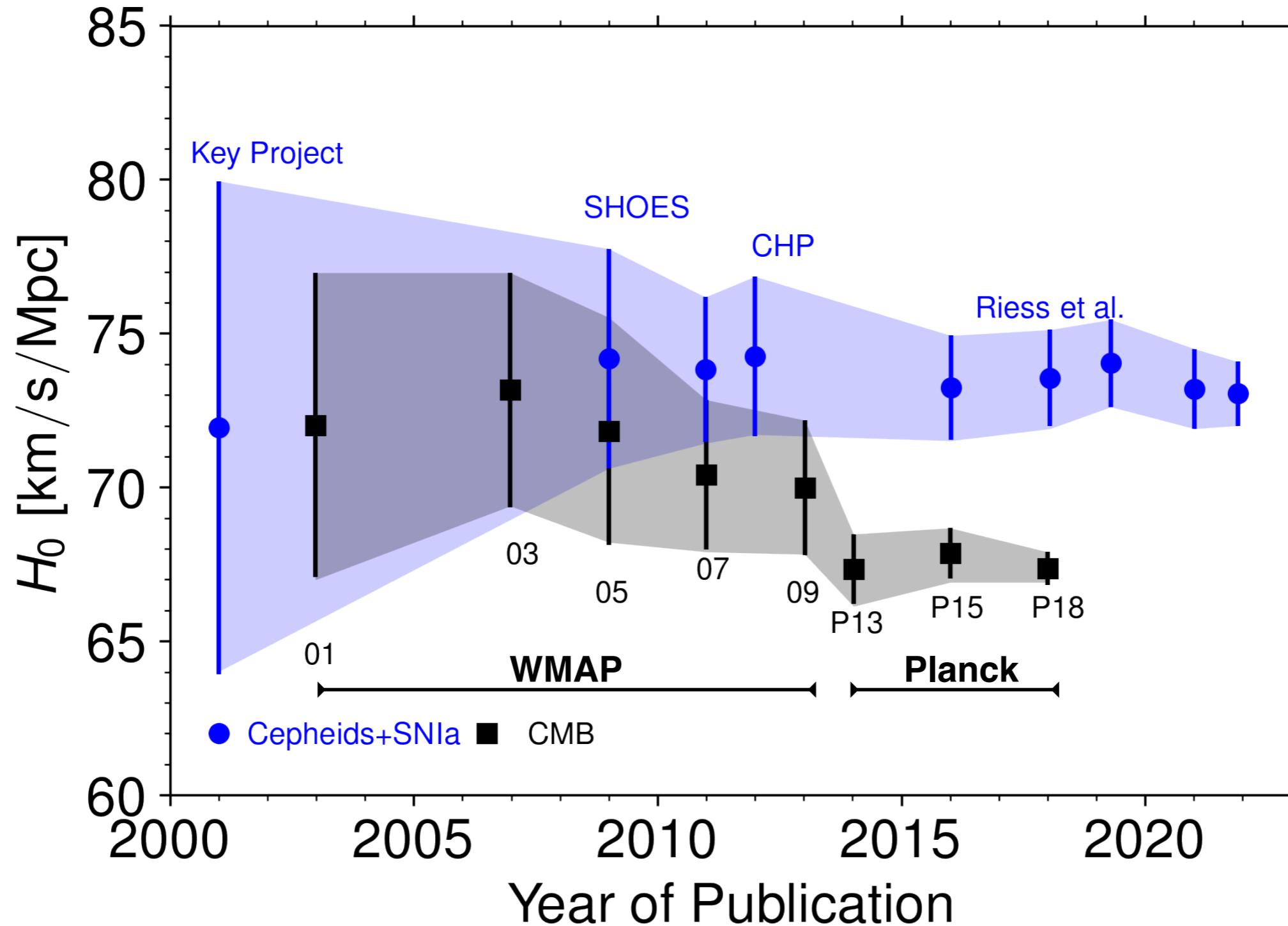


# The Hubble Tension in Perspective

**Hubble law (1929):**  $v = H_0 d$



# The Hubble Tension in Perspective



# The Hubble Tension

- The Hubble Tension:

$$H_0 = 73.04 \pm 1.04 \text{ km/s/Mpc}$$

Riess *et al.* 2112.04510

$$H_0 = 67.4 \pm 0.5 \text{ km/s/Mpc}$$

Planck 2018 1807.06209

**5 $\sigma$  tension within  $\Lambda$ CDM!**

- A pattern has clearly emerged:

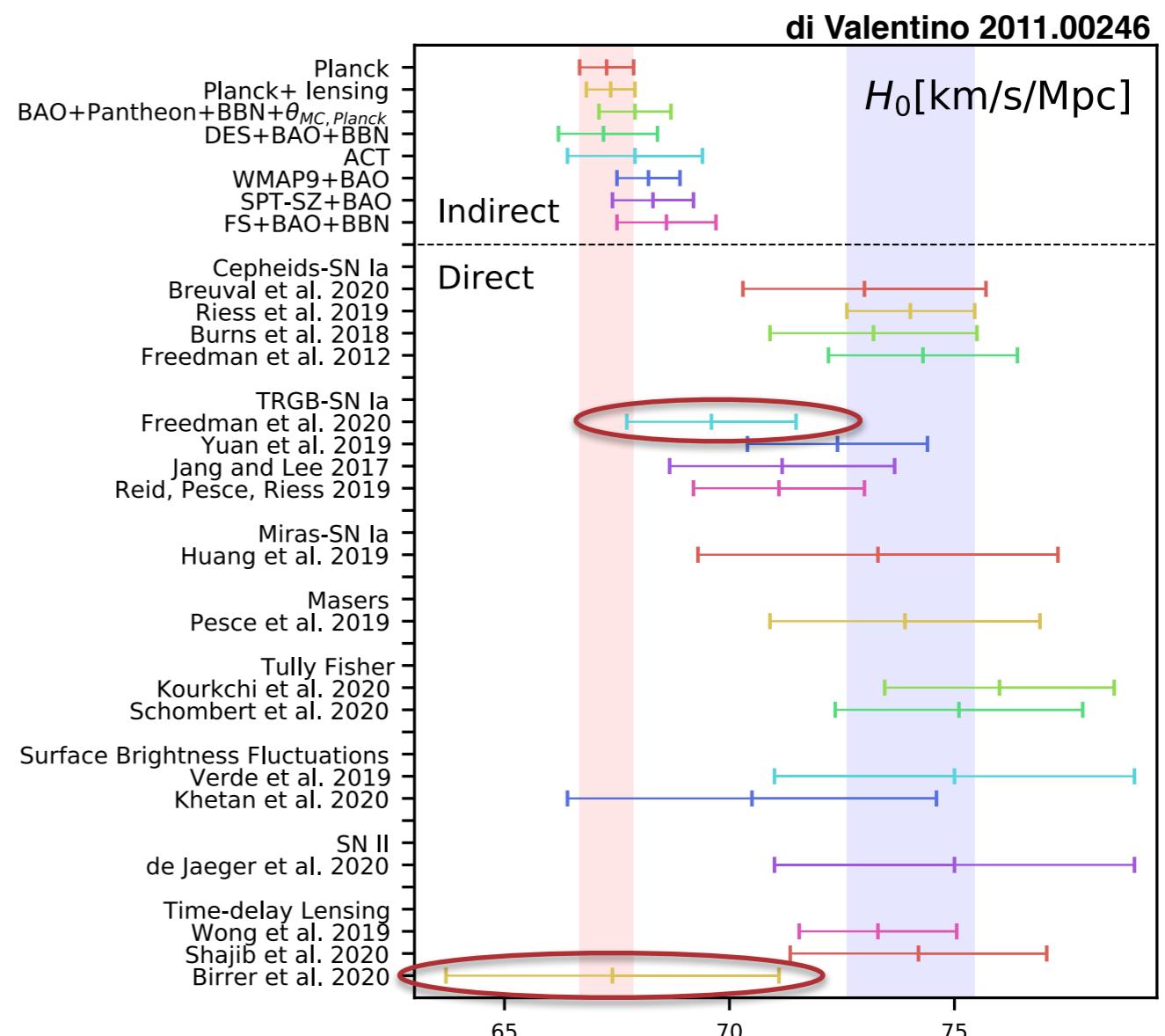
- 4-6  $\sigma$  tension depending upon the datasets included

see Verde, Treu, Riess 1907.10625 for a review

- Baryon Acoustic Oscillations point to small  $H_0$

- Cepheids+Type-Ia SN are among the most precise and they point to  $H_0 \sim (73 \pm 1) \text{ km/s/Mpc}$

- Some direct measurements do point to smaller values, Freedman et al. 20' and Birrer et al. 20'



# The Hubble Tension

- Possible resolutions:

1) Systematics in the CMB data very unlikely

2) Systematics in local measurements none so far

3) New feature of  $\Lambda$ CDM

- Possibilities beyond  $\Lambda$ CDM: See 2103.01183 by di Valentino et al. for a review  
(over 1000 references ...)

1) Late Universe Modifications very unlikely

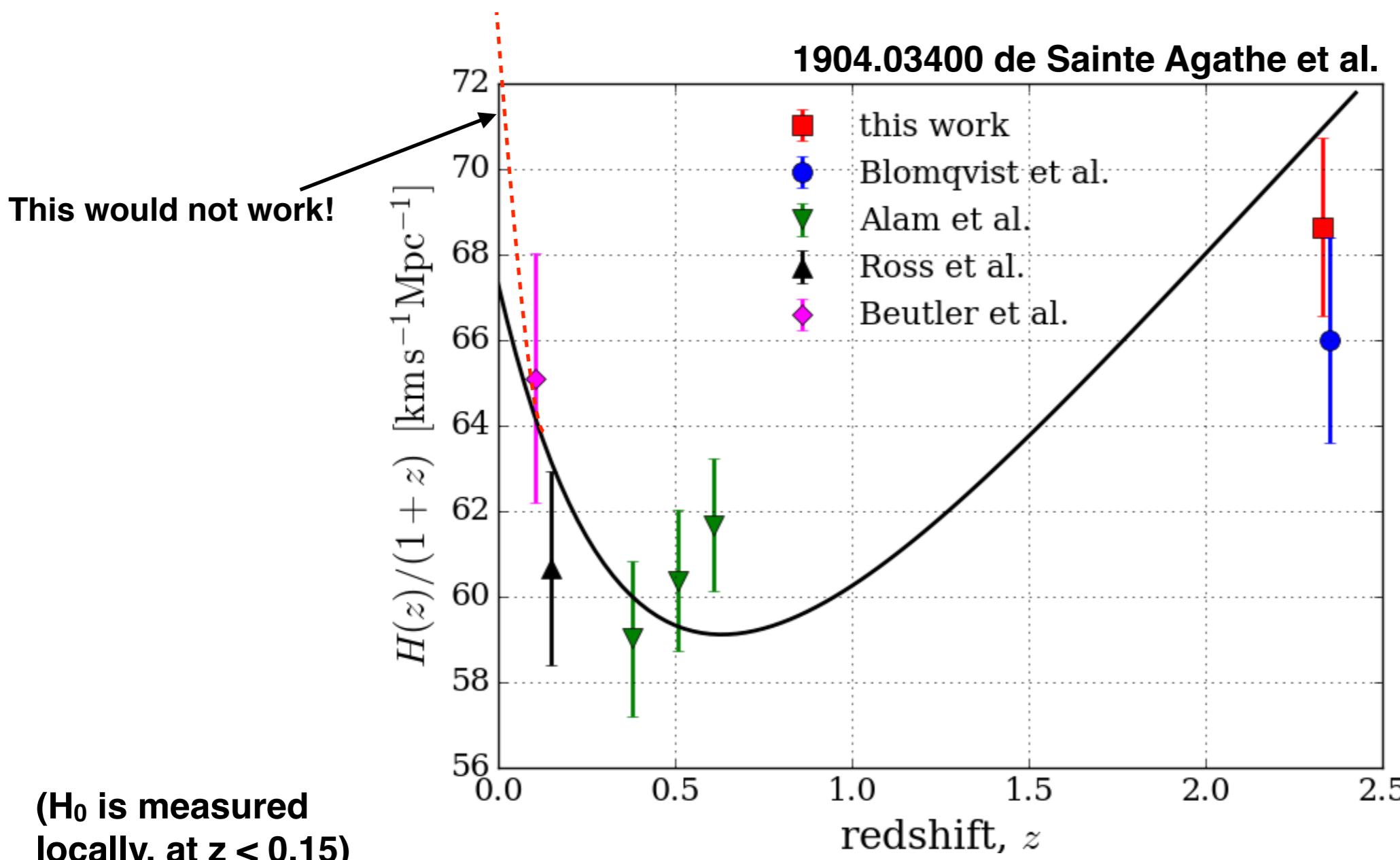
2) Early Universe Modifications hard but doable

# The Hubble Tension: Theory

Why late Universe modifications do not work?

see e.g. 2103.08723 by Efstathiou

Because type Ia SN and Baryon Acoustic Oscillations constrain the expansion history of the Universe at  $z < 2.5$  and they agree with the predictions of  $\Lambda$ CDM



# The Hubble Tension: Theory

## ● Why Early Universe modifications could work?

Because the CMB does not measure  $H_0$  directly!

Planck measures the positions of the peaks:  $\theta_s \equiv r_s/D_M(z_\star)$   
(0.03% precision)

$$r_s = \int_{z_\star}^{\infty} \frac{c_s}{H(z')} dz'$$

**Comoving sound horizon  
(Early Universe)**

$$D_M(z) = \int_0^z \frac{1}{H(z')} dz'$$

**Comoving angular diameter distance  
(Late Universe)**

$H_0$

**Model Building task:**

The game is to make  $r_s$  smaller by ~8% so that  $H_0$  can be the one reported by Riess. But, not spoiling the fit to ultra precise CMB data from Planck!

simplest:

Knox and Millea  
1908.03663

**Enhance the expansion history of the  
Universe prior and close to recombination!**

# Dark Radiation as a solution?



By far the simplest possibility, we have  $\mathcal{O}(10^3)$  models that can do it:

Editors' Suggestion

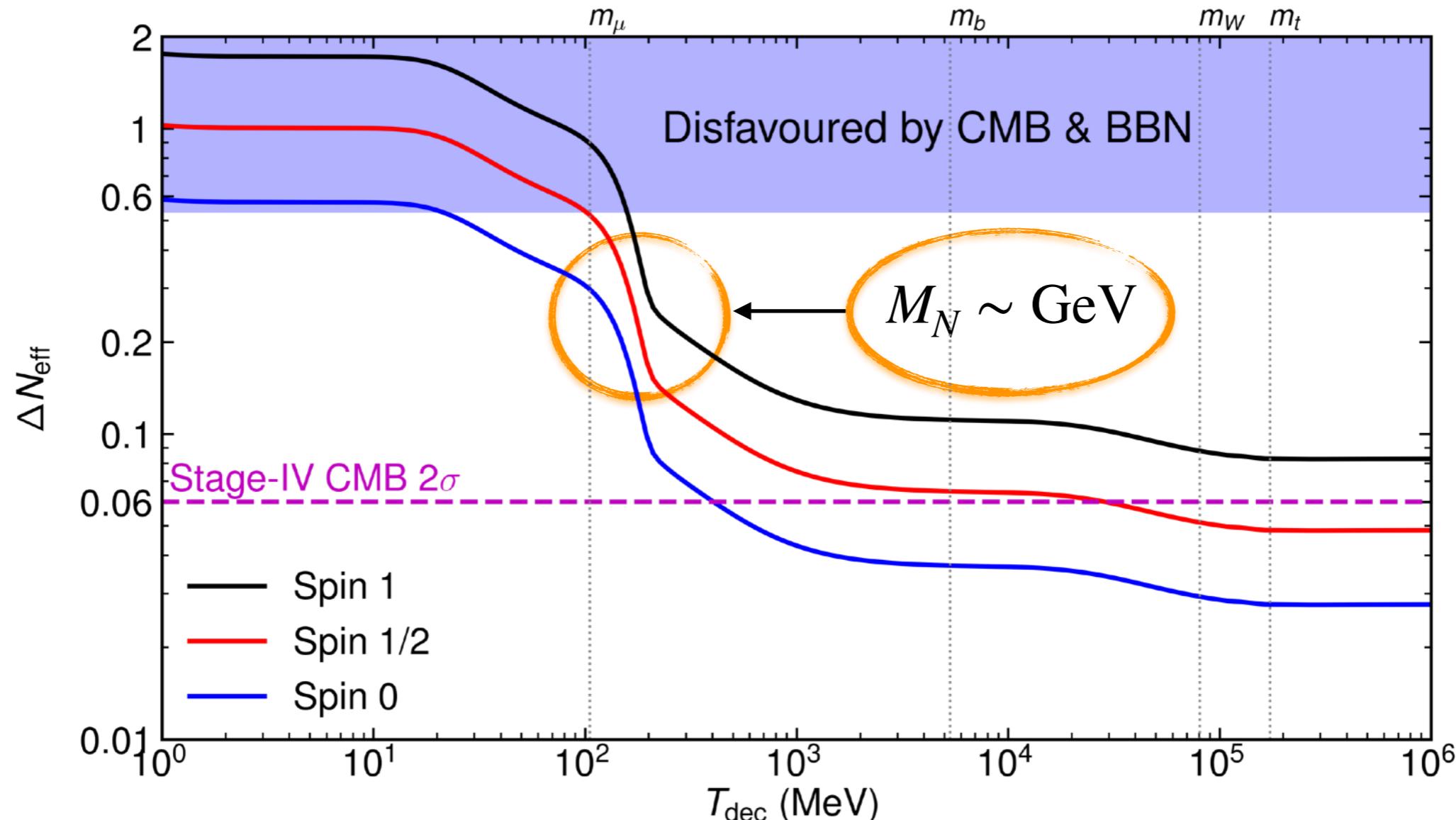
$$\Delta N_{\text{eff}} = N_{\text{eff}} - N_{\text{eff}}^{\text{SM}} > 0 \quad N_{\text{eff}}^{\text{SM}} \simeq 3.04$$

Goldstone Bosons as Fractional Cosmic Neutrinos

Steven Weinberg

Phys. Rev. Lett. **110**, 241301 – Published 10 June 2013

Typically interpreted as additional massless dark radiation as a relic from the Big Bang



# Neff as a solution to the H<sub>0</sub> Tension?

- How large would  $\Delta N_{\text{eff}}$  need to be to solve the tension?

$$H_0 \simeq [67.4 + 6.2 \Delta N_{\text{eff}}] \text{ km/s/Mpc}$$

Vagnozzi 1907.07569

😊  $\Delta N_{\text{eff}} \simeq 1$  would yield the value of  $H_0$  reported by Riess

😐 Problem 1) BBN constraints indicate that:  $\Delta N_{\text{eff}}^{\text{BBN}} < 0.5$  Pisanti et al. 2011.11537

- Constraints are dominated by Helium measurements (that could suffer from systematics)
- In many models  $\Delta N_{\text{eff}}^{\text{CMB}} \neq \Delta N_{\text{eff}}^{\text{BBN}}$

😢 Problem 2) Within the framework of  $\Lambda$ CDM Planck is compatible with  $N_{\text{eff}} \simeq 3$

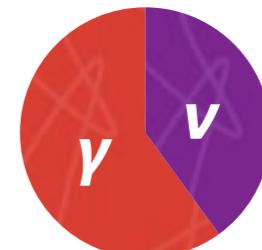
$$N_{\text{eff}}^{\text{CMB+BAO}} = 2.99 \pm 0.17 \quad \text{Planck 2018}$$

Maybe there is an effect that can compensate a large Neff at the level of the CMB fit?

😊 Neutrinos interactions can lead to a relevant impact on the CMB spectra

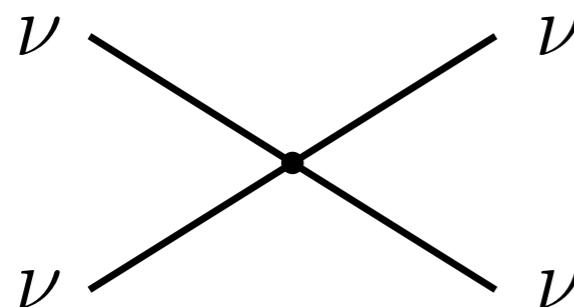
Bashinsky and Seljak astro-ph/0310198

$$\delta G_{\mu\nu} = 8\pi G \delta T_{\mu\nu}$$



# Neutrinos and the Hubble Tension

- **Strong Neutrino Scattering + Extra Radiation** Kreisch, Cyr-Racine, Doré 1902.00543



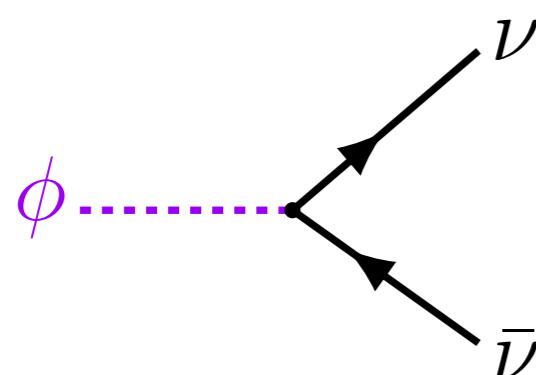
$H_0$  tension solved if TEEE data is ignored 😊

If pol data is included no solution for  $H_0$  😞

Almost excluded by Lab data (Blinov++1905.02727) 😞



- **Light Neutrinophilic Scalar + Dark Radiation** Escudero & Witte 1909.04044



$H_0$  tension from  $4.4\sigma$  to  $2.5\sigma$  😊

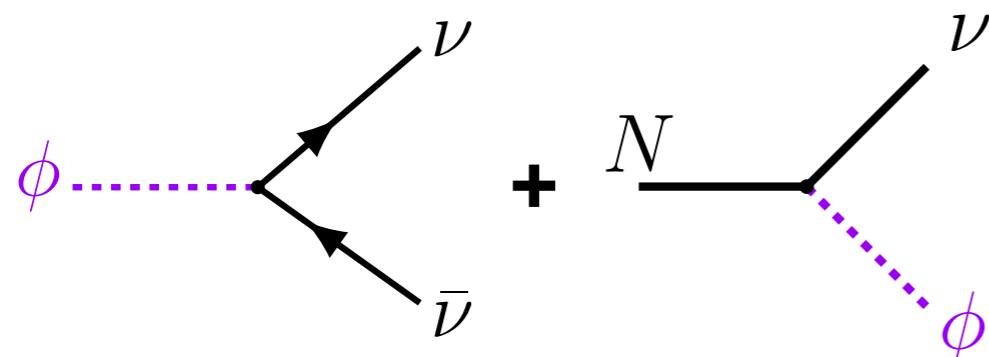
CMB fit is not degraded 😊

Direct connection with Seesaw 😊

Ad hoc  $\Delta N_{\text{eff}} \sim 0.5$  😐



- **Primordial population of light scalars** Escudero & Witte 2103.03249



Sterile neutrinos can source  $\Delta N_{\text{eff}} \sim 0.4$

Sterile neutrinos can lead to Leptogenesis

$H_0$  tension from  $5\sigma$  to  $2.5\sigma$

# The Hubble Tension: Theory

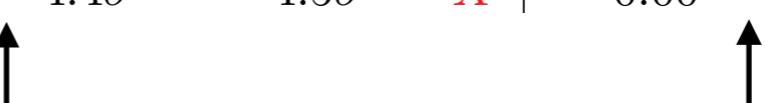
- Hundreds of Models in the market See 2103.01183 by di Valentino et al.

Most of them do not work well. They either lead to a bad CMB fit or do not shift  $H_0$  enough

Schöneberg et al. 2107.10291: *The  $H_0$  Olympics: A fair ranking of proposed models*

Model	$\Delta N_{\text{param}}$	$M_B$	Gaussian Tension	$Q_{\text{DMAP}}$ Tension	$\Delta\chi^2$	$\Delta\text{AIC}$	Finalist		
$\Lambda\text{CDM}$	0	$-19.416 \pm 0.012$	$4.4\sigma$	$4.5\sigma$	X	0.00	0.00	X	X

How large is the Hubble tension?    How good is the CMB fit?  
small values here are better!    negative values are good here!



# The Hubble Tension: Theory

- Hundreds of Models in the market See 2103.01183 by di Valentino et al.

Most of them do not work well. They either lead to a bad CMB fit or do not shift  $H_0$  enough

Schöneberg et al. 2107.10291: *The  $H_0$  Olympics: A fair ranking of proposed models*

best performance:

Model	$\Delta N_{\text{param}}$	$M_B$	Gaussian Tension	$Q_{\text{DMAP}}$ Tension	$\Delta\chi^2$	$\Delta\text{AIC}$		Finalist	
$\Lambda\text{CDM}$	0	$-19.416 \pm 0.012$	$4.4\sigma$	$4.5\sigma$	X	0.00	0.00	X	X
$\Delta N_{\text{ur}}$	1	$-19.395 \pm 0.019$	$3.6\sigma$	$3.9\sigma$	X	-4.60	-2.60	X	X
SIDR	1	$-19.385 \pm 0.024$	$3.2\sigma$	$3.6\sigma$	X	-3.77	-1.77	X	X
DR-DM	2	$-19.413 \pm 0.036$	$3.3\sigma$	$3.4\sigma$	X	-7.82	-3.82	X	X
mixed DR	2	$-19.388 \pm 0.026$	$3.2\sigma$	$3.7\sigma$	X	-6.40	-2.40	X	X
$\text{SI}\nu+\text{DR}$	3	$-19.440 \pm 0.038$	$3.7\sigma$	$3.9\sigma$	X	-3.56	2.44	X	X
Majoron	3	$-19.380 \pm 0.027$	$3.0\sigma$	$2.9\sigma$	✓	-13.74	-7.74	✓	✓ (2)
primordial B	1	$-19.390 \pm 0.018$	$3.5\sigma$	$3.5\sigma$	X	-10.83	-8.83	✓	✓ (3)
varying $m_e$	1	$-19.391 \pm 0.034$	$2.9\sigma$	$3.2\sigma$	X	-9.87	-7.87	✓	✓ (3)
varying $m_e+\Omega_k$	2	$-19.368 \pm 0.048$	$2.0\sigma$	$1.7\sigma$	✓	-16.11	-12.11	✓	✓ (1)
EDE	3	$-19.390 \pm 0.016$	$3.6\sigma$	$1.6\sigma$	✓	-20.80	-14.80	✓	✓ (2)
NEDE	3	$-19.380 \pm 0.021$	$3.2\sigma$	$2.0\sigma$	✓	-17.70	-11.70	✓	✓ (2)
CPL	2	$-19.400 \pm 0.016$	$3.9\sigma$	$4.1\sigma$	X	-4.23	-0.23	X	X
PEDE	0	$-19.349 \pm 0.013$	$2.7\sigma$	$2.0\sigma$	✓	4.76	4.76	X	X
MPEDE	1	$-19.400 \pm 0.022$	$3.6\sigma$	$4.0\sigma$	X	-2.21	-0.21	X	X
DM $\rightarrow$ DR+WDM	2	$-19.410 \pm 0.013$	$4.2\sigma$	$4.4\sigma$	X	-4.18	-0.18	X	X
DM $\rightarrow$ DR	2	$-19.410 \pm 0.011$	$4.3\sigma$	$4.2\sigma$	X	0.11	4.11	X	X

- None of them fully solves the Hubble tension!
- Most of those that can ameliorate the tension are not theoretically well motivated

# The Hubble Tension: Theory

## ● A critical review of the best performing models

Schöneberg et al. 2107.10291: *The  $H_0$  Olympics: A fair ranking of proposed models*

Model	$\Delta N_{\text{param}}$	$M_B$	Gaussian Tension	$Q_{\text{DMAP}}$ Tension	$\Delta\chi^2$	$\Delta\text{AIC}$	Finalist	
Majoron	3	$-19.380 \pm 0.027$	$3.0\sigma$	$2.9\sigma$	✓	-13.74	-7.74	✓ ②
primordial B	1	$-19.390 \pm 0.018$	$3.5\sigma$	$3.5\sigma$	X	-10.83	-8.83	✓ ③
varying $m_e$	1	$-19.391 \pm 0.034$	$2.9\sigma$	$3.2\sigma$	X	-9.87	-7.87	✓ ③
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EDE	3	$-19.390 \pm 0.016$	$3.6\sigma$	$1.6\sigma$	✓	-20.80	-14.80	✓ ②
NEDE	3	$-19.380 \pm 0.021$	$3.2\sigma$	$2.0\sigma$	✓	-17.70	-11.70	✓ ②

## ● Primordial magnetic fields & $m_e(t) + \Omega_k$

The idea here is that recombination happens earlier than in  $\Lambda$ CDM by either

- a) using primordial magnetic fields of  $\sim 1$  nGauss on kpc scales [Jedamzik & Pogosian 2004.09487]
- b) enhancing  $m_e(t)$  at recombination by  $\sim 2\%$  [Hart & Chluba 1912.03986]

😐 Good exercises, not much theoretical motivation for  $m_e(t)$  but maybe yes for B fields.

## ● Early Dark Energy Poulin, Smith, Karwal, Kamionkowski 1811.04083 Agrawal, Cyr-Racine, Pinner, Randall 1904.01016

The idea is that there is an early dark energy component just acting right before recombination

This can be done with a very light scalar field with  $m_\phi \sim 10^{-27}$  eV  
that yields  $f_{\text{EDE}} \sim 10\%$  but with a very particular potential:

$$V_\phi \sim m^2 f^2 [1 - \cos \phi/f]^3 \sim m^2 \phi^6 / f^4$$

😐 Highly unclear where such potential could come from and there is a coincidence problem ...

## ● New Early Dark Energy

Another possibility is to trigger a 1st order phase transition at  $T \sim$  eV [Niedermann & Sloth 1910.10739]

😐 It appears rather involved ... Dark gauge sector, DM, neutrinos, inverse seesaw...

see [Niedermann & Sloth 2112.00759, 2112.00770]

# The Hubble Tension

## 1) Observational evidence

**There is strong observational evidence from Cepheids+SNIa**

**However, it is still just a tension. It needs to be confirmed by other methods**

**We expect significant improvements in ~3-4 years, particularly with upcoming data from Gaia & the James Webb telescope**

## 2) Theoretical modeling

**Despite the strong efforts, we have no perfect model so far**

**Most of the models lack theoretical motivation**

**My personal view as a particle physicist:**

**Exciting opportunity to try to learn about fundamental physics**

Mid Seminar Pause =)

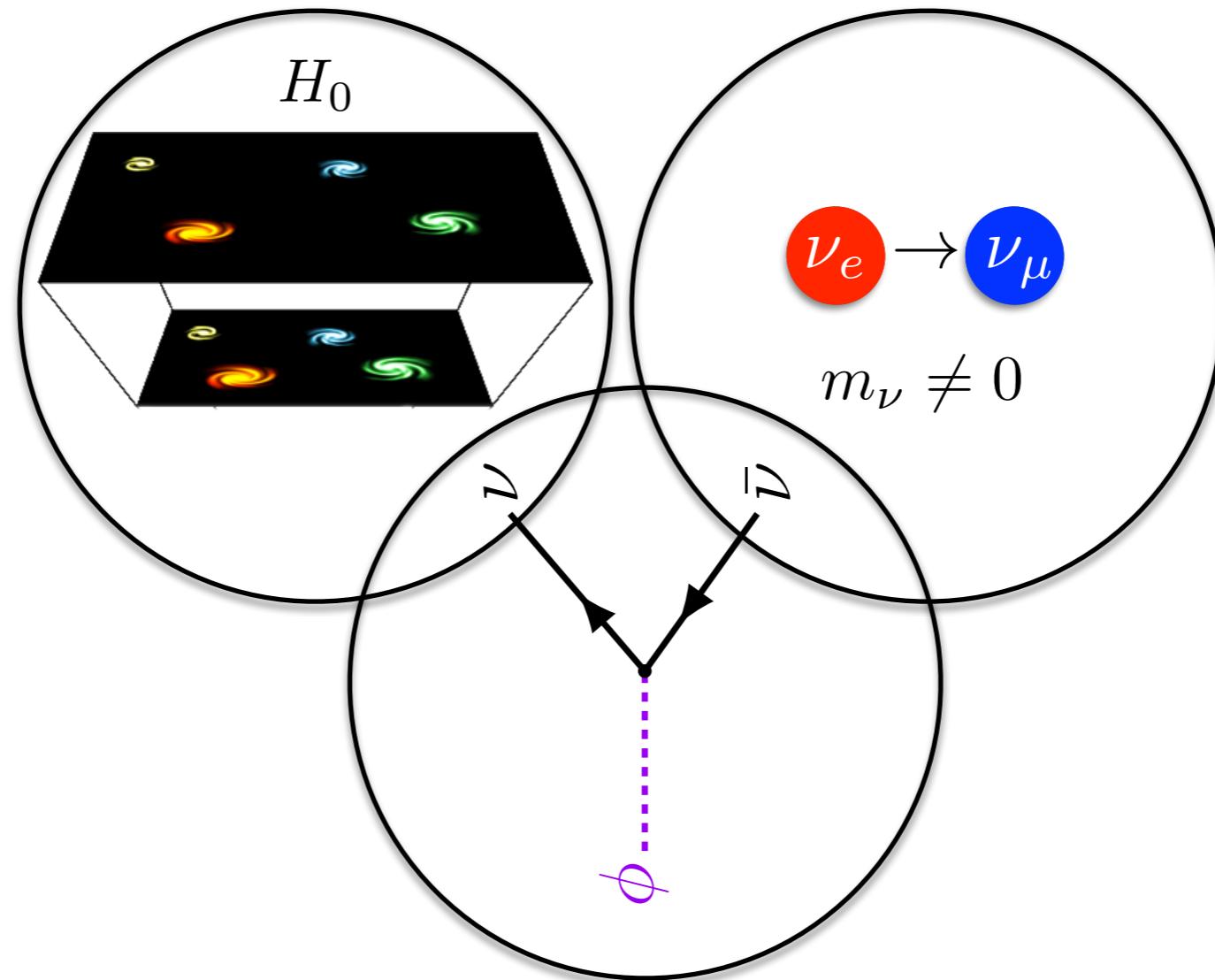
**Questions?**

**Comments?**

**Criticism?**

**All are most welcome!**

# The Idea



**What is the Majoron?**

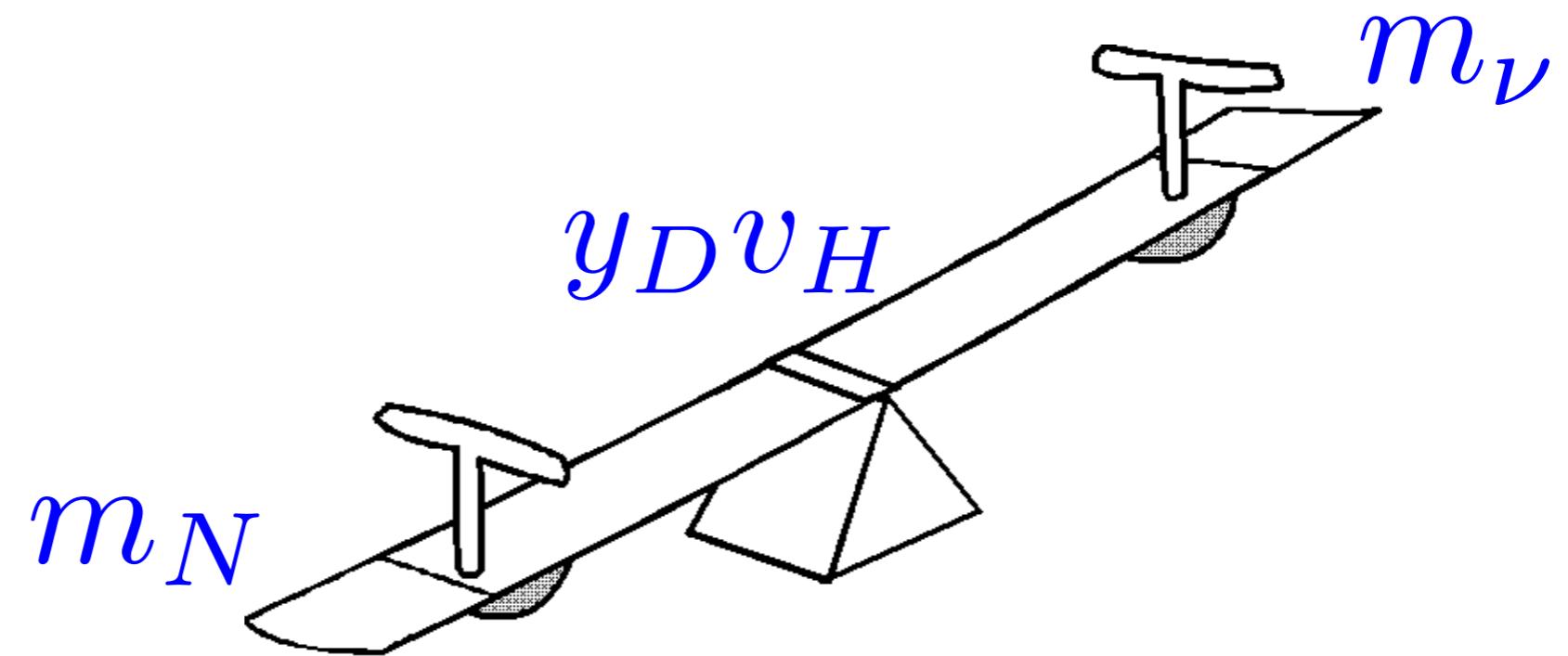
**What are its properties and its cosmology?**

**Why can it address the Hubble tension?**

# The Seesaw Mechanism

Minkowski, Yanagida, Gell-Mann, Ramond, Slansky, Glashow, Mohapatra, Senjanovic, Schechter, Valle

Type-I seesaw



Neutrinos are very light Majorana particles:

$$m_\nu \simeq 0.03 \text{ eV} \left( \frac{y_D}{10^{-6}} \right)^2 \frac{\text{TeV}}{M_N}$$

# The Scenario

## Spontaneously Broken Symmetry Global $U(1)_L$

Chikashige, Mohapatra, Peccei (1981)

**Sterile Neutrinos**  $\mathcal{L} = -\frac{\lambda_{N_{ij}}}{\sqrt{2}} \Phi \bar{N}_{R,i} N_{R,j}^c - h_{\alpha i} \bar{L}_L^\alpha H N_{Ri} + \text{h.c.}, \quad L[\Phi] = 2, \quad L[N] = 1$

SSB:  $\Phi \rightarrow v_L/\sqrt{2} \longrightarrow M_N = \lambda_N v_L \xrightarrow{\text{seesaw}} m_\nu \simeq h^2 v_H^2 / (2M_N)$

**Scalar Sector**  $V_\Phi = -\mu_\Phi^2 \Phi^\dagger \Phi + \lambda_\Phi (\Phi^\dagger \Phi)^2 - \lambda_{\Phi H} (H^\dagger H) (\Phi^\dagger \Phi)$

$\Phi = \frac{v_L + \rho}{\sqrt{2}} e^{i\phi/v_L}$	$\rho \equiv \text{CP-even scalar}$	$m_\rho^2 = 2\lambda_\Phi v_L^2$
	$\phi \equiv \text{Majoron}$	<b>pseudo-Goldstone:</b> $m_\phi \simeq 0$

**Interactions**  $\mathcal{L}_{\text{eff}} = -\frac{\lambda_N}{2} [\rho \bar{N} N - i\phi \bar{N} \gamma_5 N] - \frac{\lambda_{N\nu}}{2} [\rho \bar{N} \nu - i\phi \bar{N} \gamma_5 \nu] + \text{h.c.} - \frac{\lambda_\nu}{2} [\rho \bar{\nu} \nu - i\phi \bar{\nu} \gamma_5 \nu]$

$\lambda_\nu \ll \lambda_{N\nu} \ll \lambda_N$

$\lambda_\nu \simeq |\theta| \lambda_{N\nu} \simeq |\theta|^2 \lambda_N$

$|\theta|^2 \simeq 5 \times 10^{-11} \frac{m_\nu}{0.05 \text{ eV}} \frac{1 \text{ GeV}}{M_N}$

# The Scenario

## Spontaneously Broken Symmetry Global $U(1)_L$

Chikashige, Mohapatra, Peccei (1981)

**The Majoron:**  $\phi$

$$\mathcal{L}_{\text{int}} = i\lambda \phi \bar{\nu} \gamma_5 \nu$$

**Very weakly interacting:**

$$\lambda \simeq 10^{-13} \frac{m_\nu}{0.05 \text{ eV}} \frac{\text{TeV}}{v_L} \quad (\text{seesaw})$$

**Extremely feebly interacting with matter:**  $\lambda_{\phi ee} \sim 10^{-20}$

**Dimension-5 Planck suppressed operators:**

$$m_\phi \sim v_L \sqrt{\frac{v_L}{M_{\text{Pl}}}} \lesssim 0.1 \text{ keV}$$

$$\Delta V = \beta (\Phi^\star \Phi)^2 \frac{\Phi^\star + \Phi}{M_{\text{Pl}}}$$

Rothstein, Babu, Seckel hep-ph/9301213  
Akhmedov, Berezhiani, Mohapatra, Senjanovic hep-ph/9209285

**Key coincidence!!**

**Retain step parameter space**

$$10^{-15} < \lambda < 10^{-3}$$
$$\frac{\phi}{0.1 \text{ eV}} < m_\phi < \text{MeV}$$

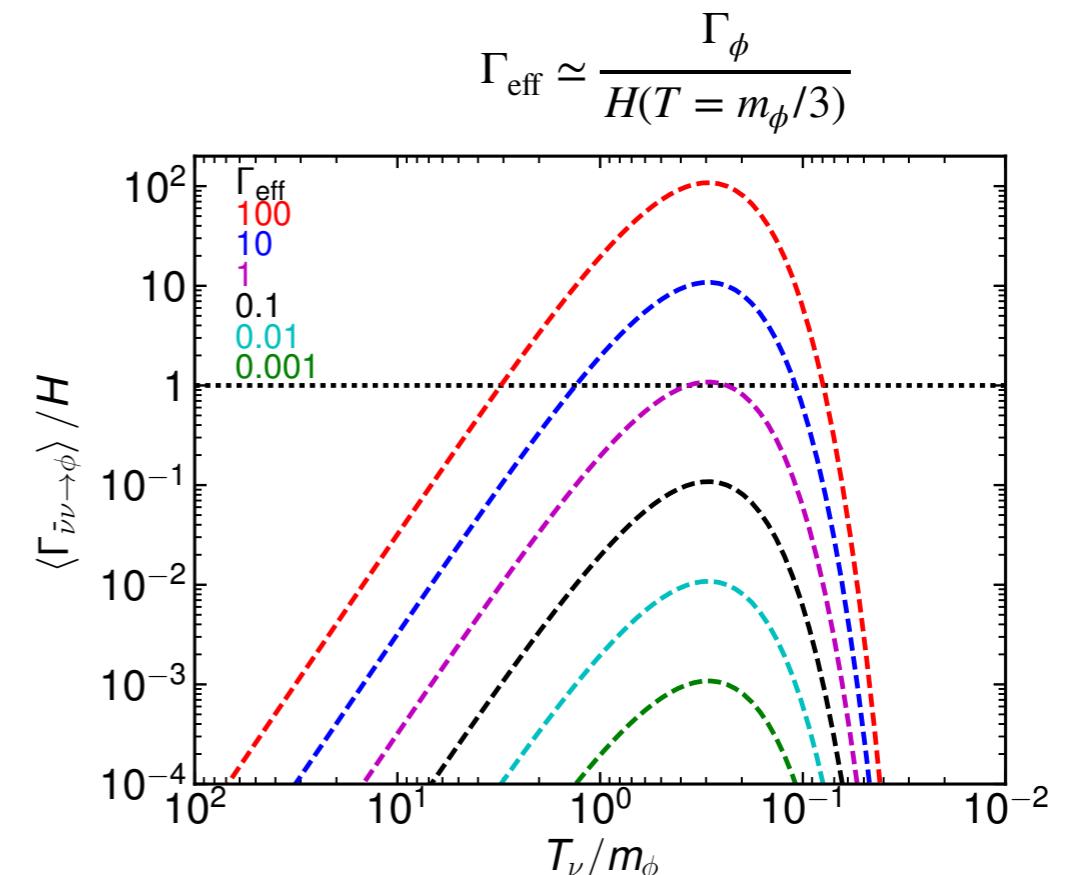
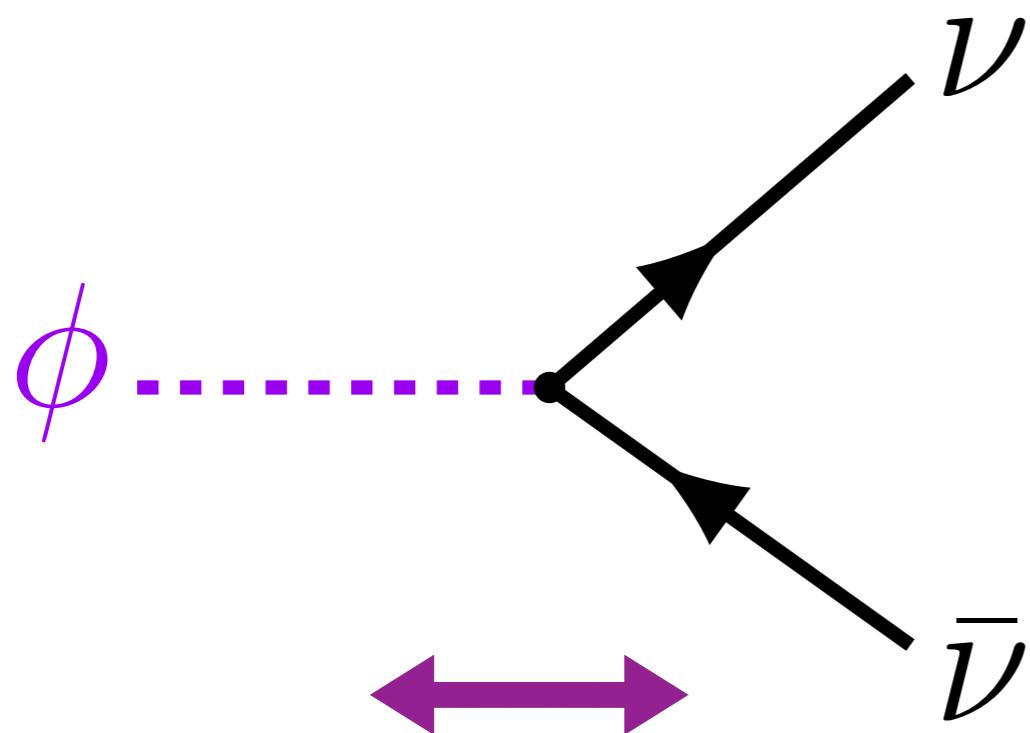
$m_\phi \sim \text{eV}$ ,  $v_L \sim 1 \text{ TeV}$

And assume that  $p_\phi = 0$  at BBN

# Cosmological Implications

Only Relevant Process:

provided  $\Gamma_\phi \geq H(T_\nu = m_\phi/3)$

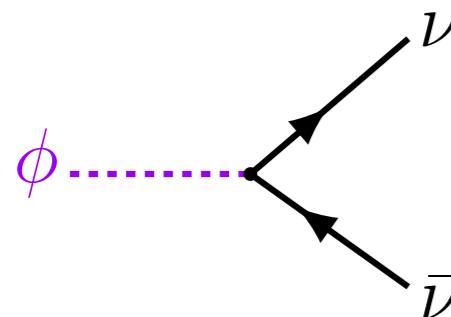


Two main effects:

Chacko, Hall, Okui, Oliver  
hep-ph/0312267

- Non-standard expansion history
- Erase the neutrino anisotropic stress

# Cosmological Analysis



- Non-standard expansion history
- Erase the neutrino anisotropic stress

## ● Background

We solve the Boltzmann equation of the neutrino-majoron system

Escudero 1812.05605 & 2001.04466

$$\begin{aligned} \frac{dT_\phi}{dt} &= \frac{1}{\frac{\partial n_\phi}{\partial \mu_\phi} \frac{\partial \rho_\phi}{\partial T_\phi} - \frac{\partial n_\phi}{\partial T_\phi} \frac{\partial \rho_\phi}{\partial \mu_\phi}} \left[ -3H \left( (p_\phi + \rho_\phi) \frac{\partial n_\phi}{\partial \mu_\phi} - n_\phi \frac{\partial \rho_\phi}{\partial \mu_\phi} \right) + \frac{\partial n_\phi}{\partial \mu_\phi} \frac{\delta \rho_\phi}{\delta t} - \frac{\partial \rho_\phi}{\partial \mu_\phi} \frac{\delta n_\phi}{\delta t} \right] \\ \frac{d\mu_\phi}{dt} &= \frac{-1}{\frac{\partial n_\phi}{\partial \mu_\phi} \frac{\partial \rho_\phi}{\partial T_\phi} - \frac{\partial n_\phi}{\partial T_\phi} \frac{\partial \rho_\phi}{\partial \mu_\phi}} \left[ -3H \left( (p_\phi + \rho_\phi) \frac{\partial n_\phi}{\partial T_\phi} - n_\phi \frac{\partial \rho_\phi}{\partial T_\phi} \right) + \frac{\partial n_\phi}{\partial T_\phi} \frac{\delta \rho_\phi}{\delta t} - \frac{\partial \rho_\phi}{\partial T_\phi} \frac{\delta n_\phi}{\delta t} \right] \\ \frac{dT_\nu}{dt} &= \frac{1}{\frac{\partial n_\nu}{\partial \mu_\nu} \frac{\partial \rho_\nu}{\partial T_\nu} - \frac{\partial n_\nu}{\partial T_\nu} \frac{\partial \rho_\nu}{\partial \mu_\nu}} \left[ -3H \left( (p_\nu + \rho_\nu) \frac{\partial n_\nu}{\partial \mu_\nu} - n_\nu \frac{\partial \rho_\nu}{\partial \mu_\nu} \right) - \frac{\partial n_\nu}{\partial \mu_\nu} \frac{\delta \rho_\nu}{\delta t} + 2 \frac{\partial \rho_\nu}{\partial \mu_\nu} \frac{\delta n_\nu}{\delta t} \right] \\ \frac{d\mu_\nu}{dt} &= \frac{-1}{\frac{\partial n_\nu}{\partial \mu_\nu} \frac{\partial \rho_\nu}{\partial T_\nu} - \frac{\partial n_\nu}{\partial T_\nu} \frac{\partial \rho_\nu}{\partial \mu_\nu}} \left[ -3H \left( (p_\nu + \rho_\nu) \frac{\partial n_\nu}{\partial T_\nu} - n_\nu \frac{\partial \rho_\nu}{\partial T_\nu} \right) - \frac{\partial n_\nu}{\partial T_\nu} \frac{\delta \rho_\nu}{\delta t} + 2 \frac{\partial \rho_\nu}{\partial T_\nu} \frac{\delta n_\nu}{\delta t} \right] \\ \frac{dT_\gamma}{dt} &= -H T_\gamma, \end{aligned}$$

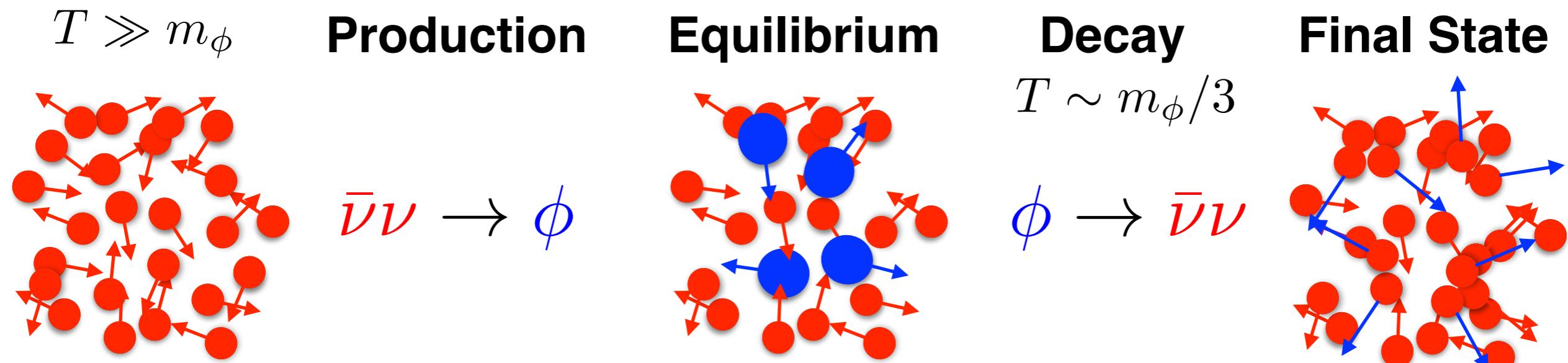
## ● Perturbations

We use the relaxation time approximation to model the effects of interactions in the perturbations:

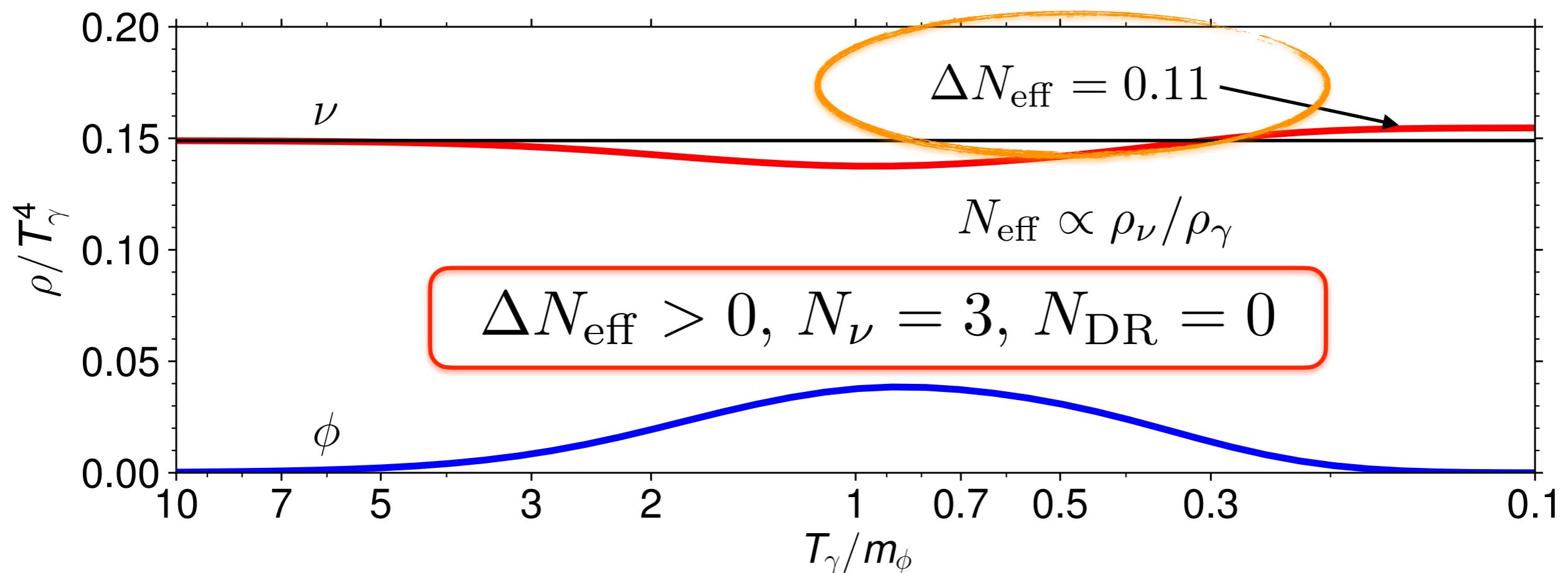
$$\begin{aligned} \dot{\delta}_{\nu\phi} &= -\frac{4}{3}\theta_{\nu\phi} - \frac{2}{3}\dot{h}, \\ \dot{\theta}_{\nu\phi} &= k^2 \left( \frac{1}{4}\delta_{\nu\phi} - \sigma_{\nu\phi} \right), \\ \dot{F}_{\nu\phi 2} &= 2\dot{\sigma}_{\nu\phi} = \frac{8}{15}\theta_{\nu\phi} - \frac{3}{5}kF_{\nu\phi 3} + \frac{4}{15}\dot{h} + \frac{8}{5}\dot{\eta} - 2a\Gamma\sigma_{\nu\phi}, \\ \dot{F}_{\nu\phi \ell} &= \frac{k}{2\ell+1} [\ell F_{\nu\phi (\ell-1)} - (\ell+1)F_{\nu\phi (\ell+1)}] - a\Gamma F_{\nu\phi \ell}, \quad \ell \geq 3. \\ \Gamma &\equiv \frac{1}{n_\nu} \left. \frac{\delta n_\nu}{\delta t} \right|_{\text{forward}} = \frac{\Gamma_\phi}{2} \frac{m_\phi^2}{T_\nu^2} e^{\frac{\mu_\nu}{T_\nu}} K_1 \left( \frac{m_\phi}{T_\nu} \right) \end{aligned}$$

## ● We include in CLASS all of these effects

# Cosmological Implications

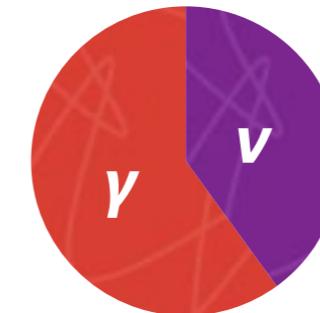


$$\Gamma_\phi \simeq H(T_\nu = m_\phi/3)$$



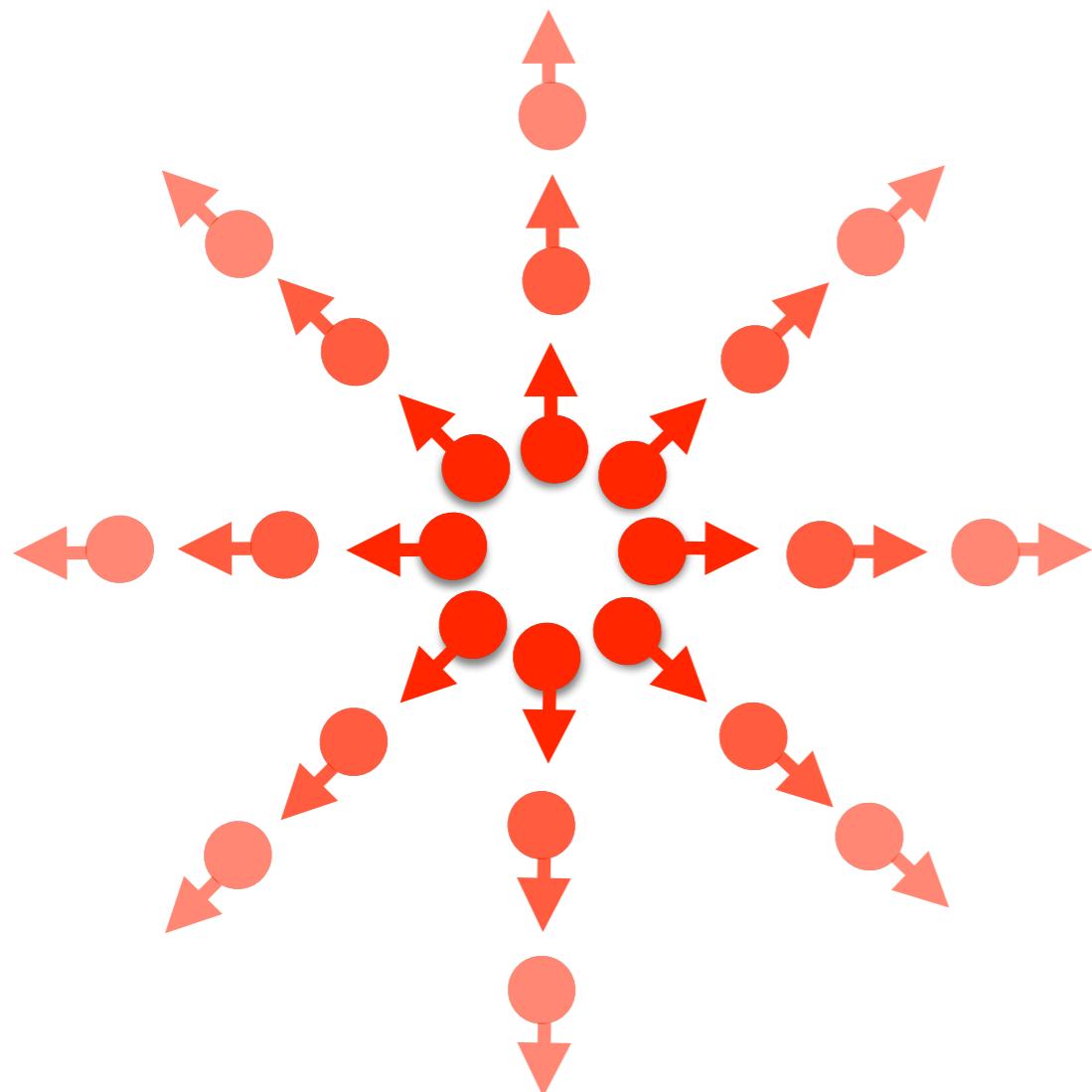
# Neutrino Perturbations

Neutrino perturbations are key:

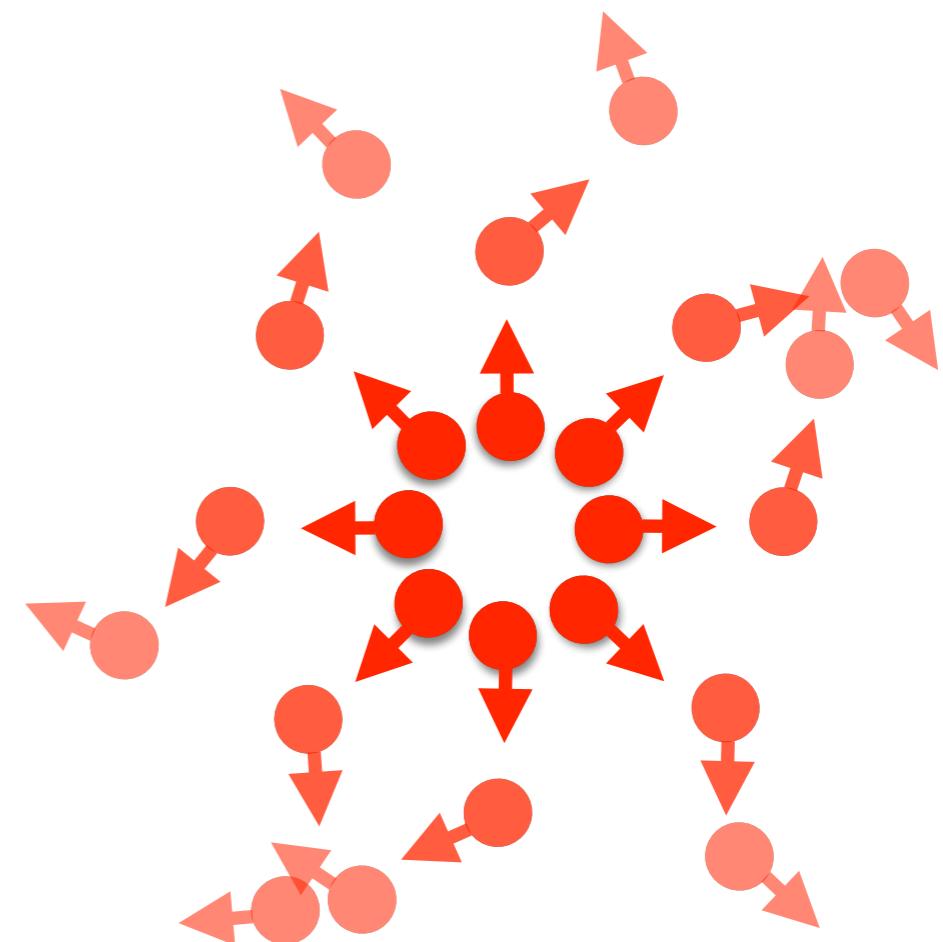


$$\delta G_{\mu\nu} = 8\pi G \delta T_{\mu\nu}$$

Free Streaming Neutrinos  $\sigma_\nu \neq 0$



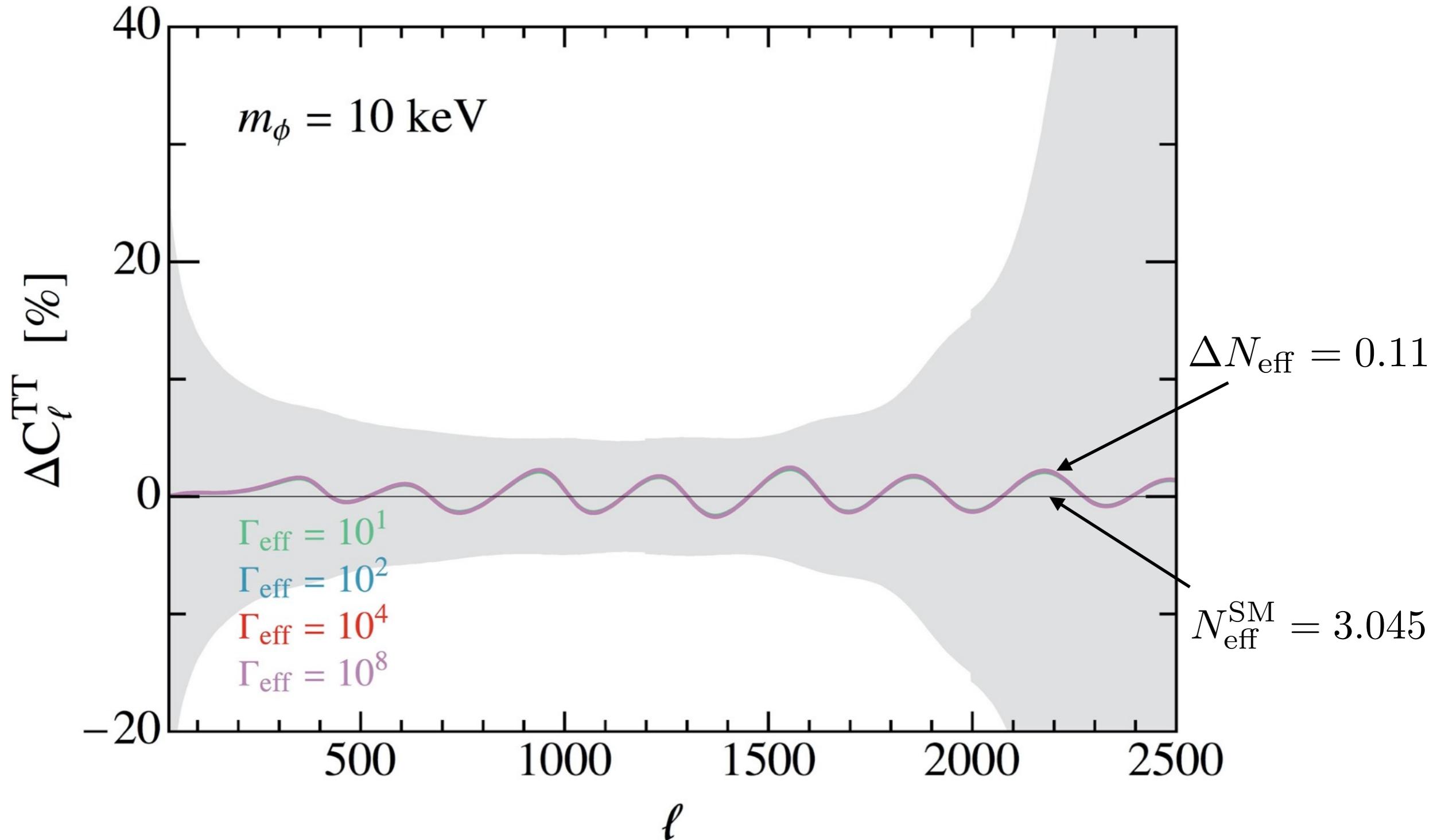
Interacting Neutrinos  $\sigma_\nu \rightarrow 0$



Effect on the CMB is to shift the positions of the peaks! Bashinsky and Seljak  
[astro-ph/0310198](https://arxiv.org/abs/astro-ph/0310198)

# Effects on the CMB

$$\Gamma_{\text{eff}} = \left( \frac{\lambda}{4 \times 10^{-14}} \right)^2 \left( \frac{0.1 \text{ eV}}{m_\phi} \right)$$



# Effects on the CMB

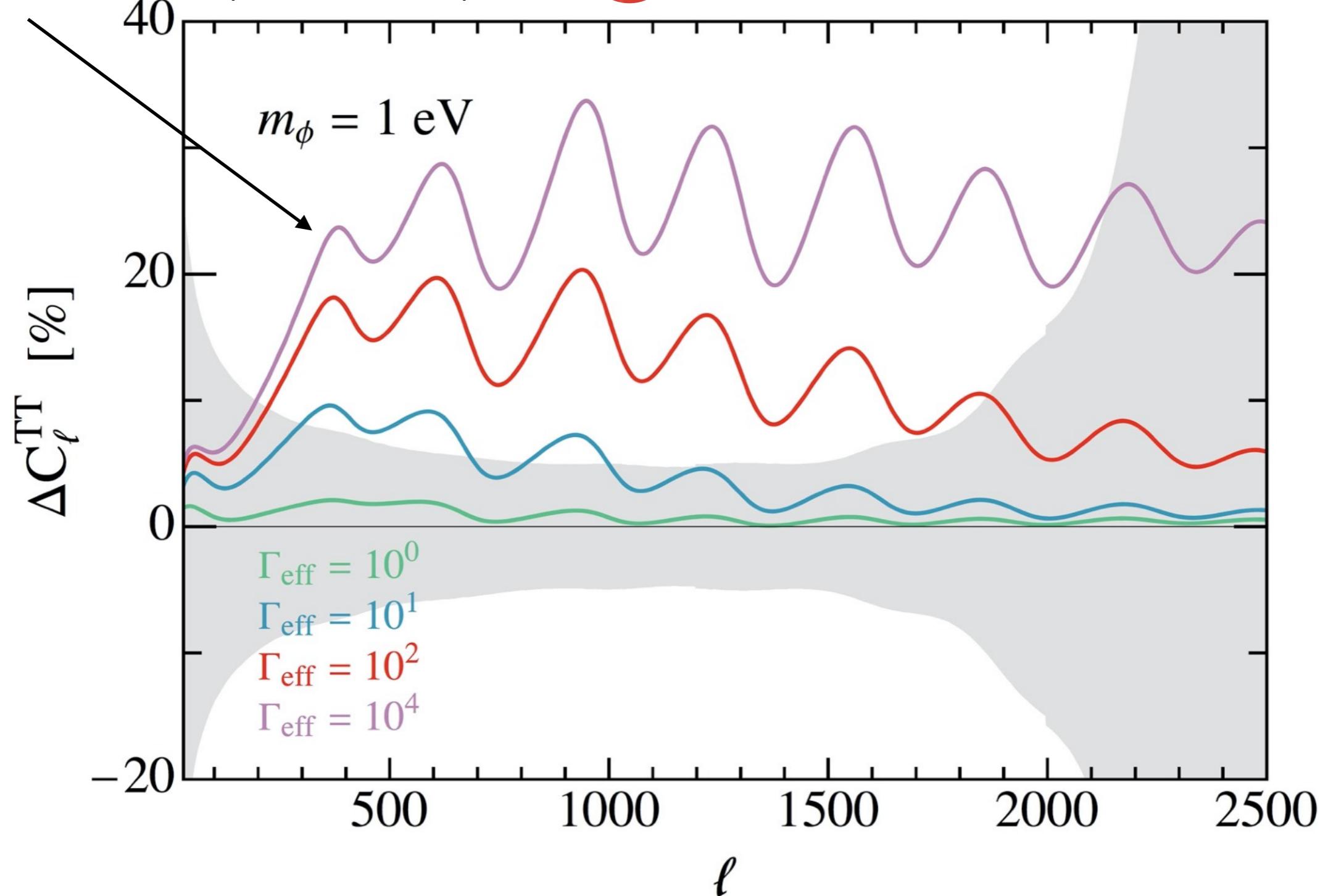
see Bashinsky and Seljak astro-ph/0310198

$$\sigma_\nu \rightarrow 0$$

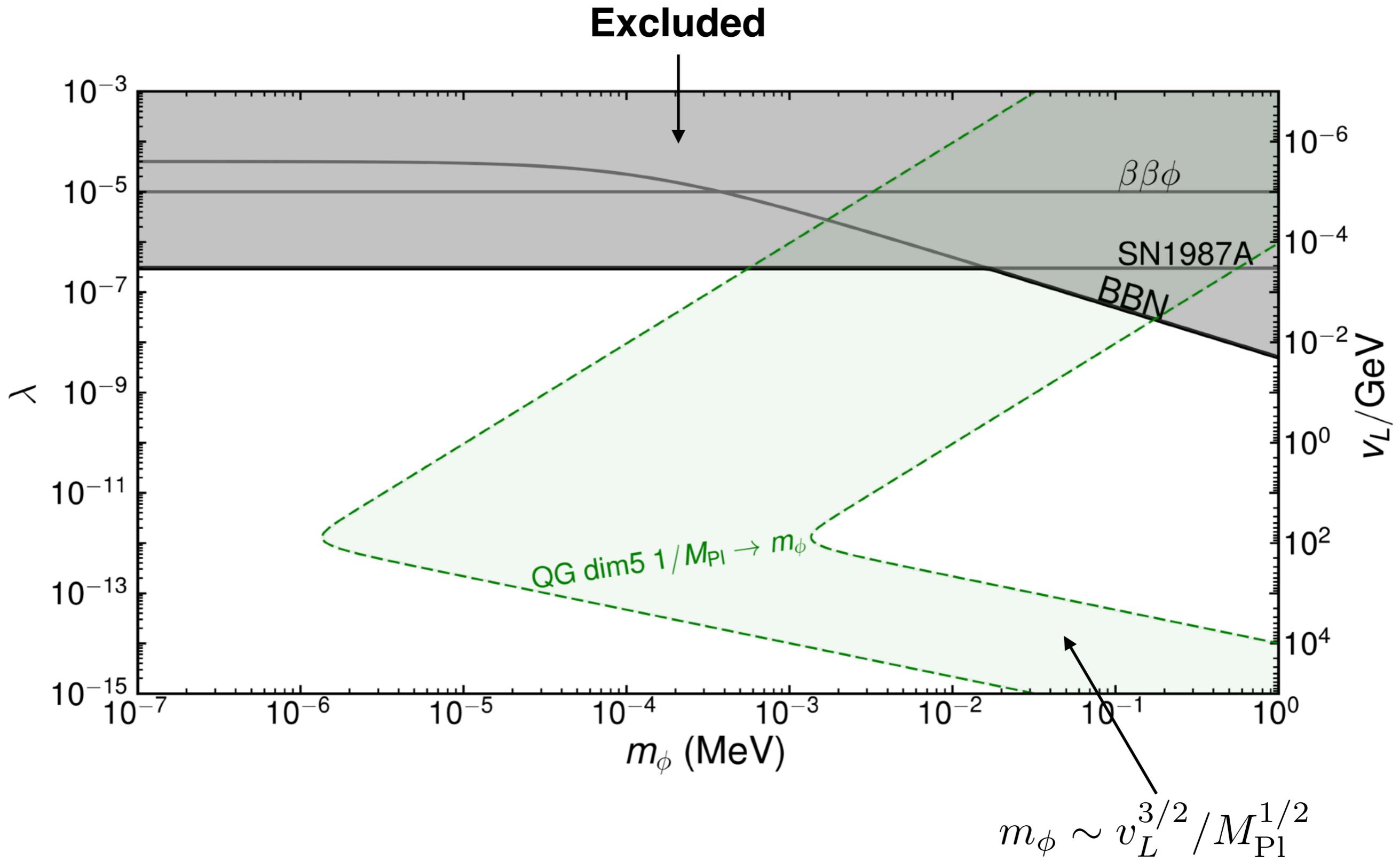
$$\delta G_{\mu\nu} = 8\pi G \delta T_{\mu\nu}$$



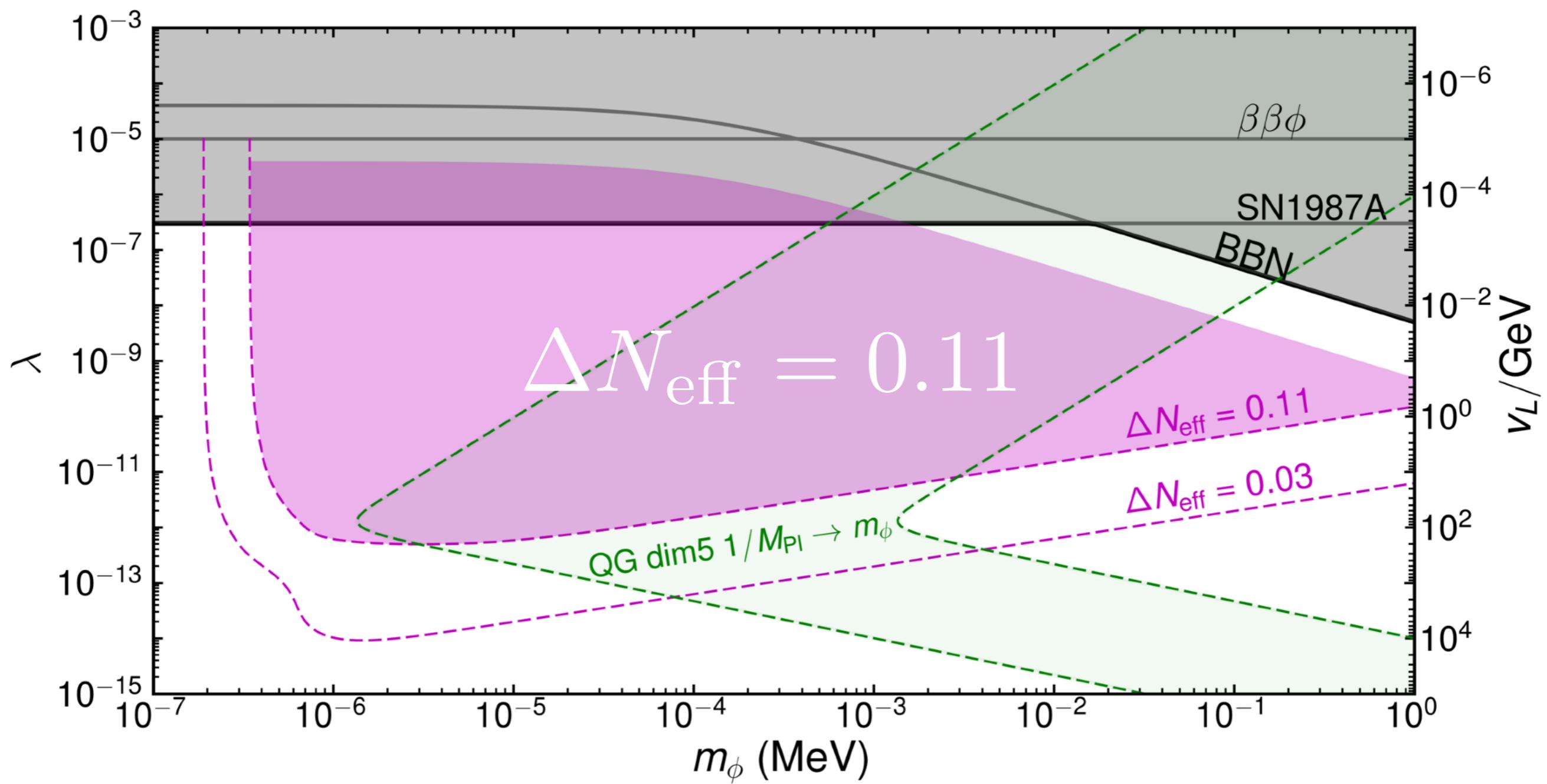
$$\Gamma_{\text{eff}} = \left( \frac{\lambda}{4 \times 10^{-14}} \right)^2 \left( \frac{0.1 \text{ eV}}{m_\phi} \right)$$



# Parameter Space

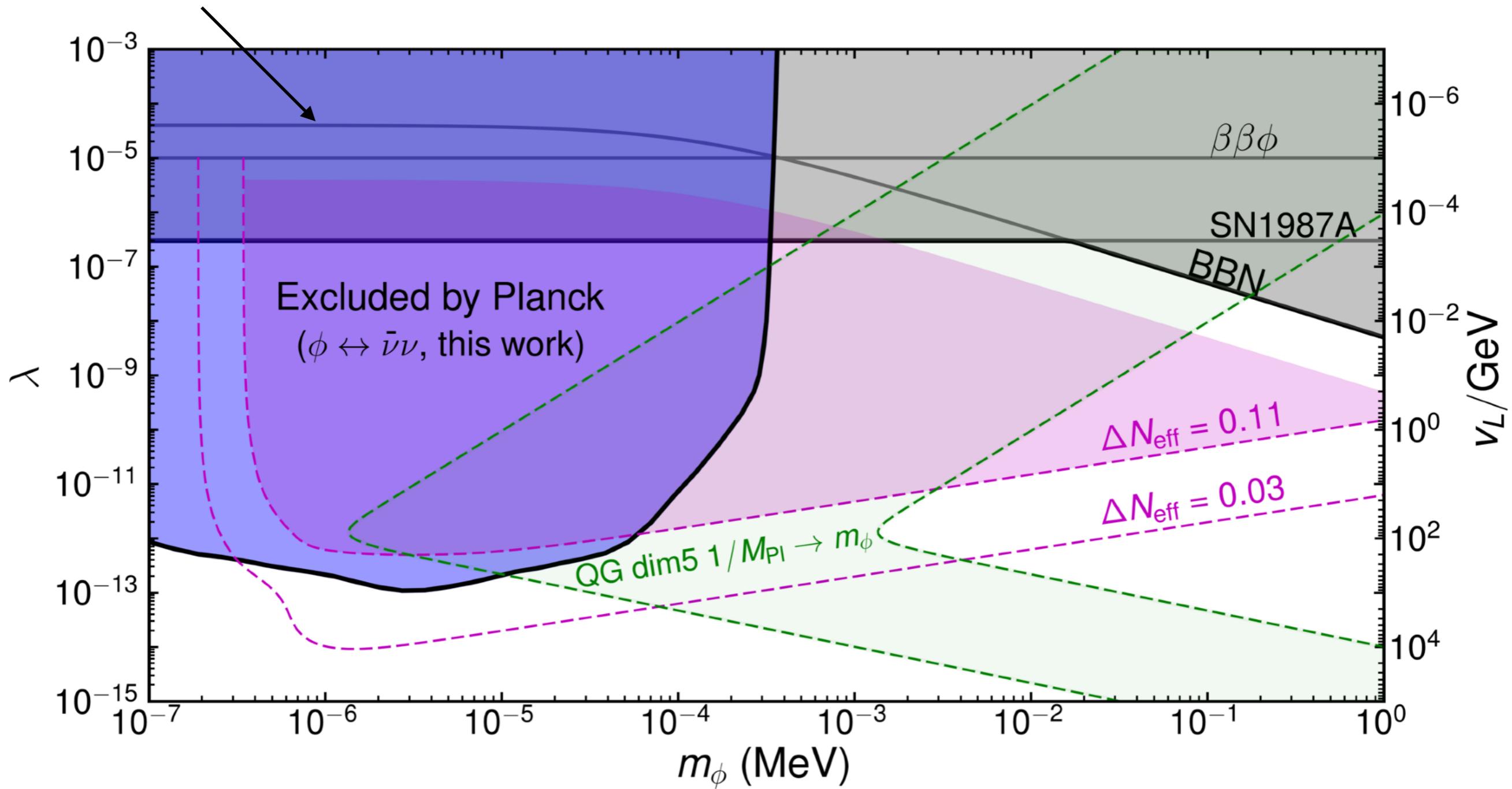


# Parameter Space

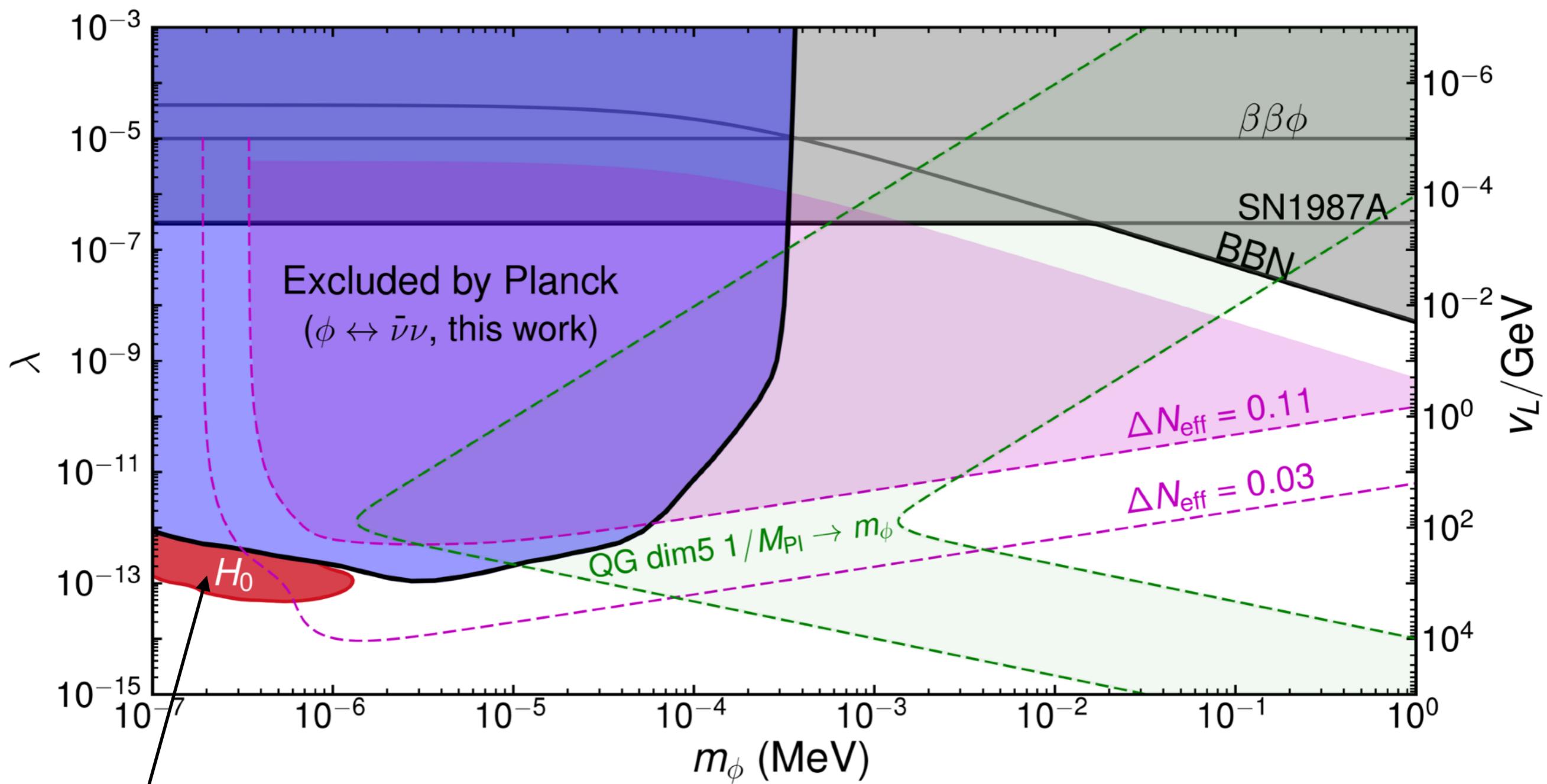


# Parameter Space

Full MCMC to Planck 2018 data

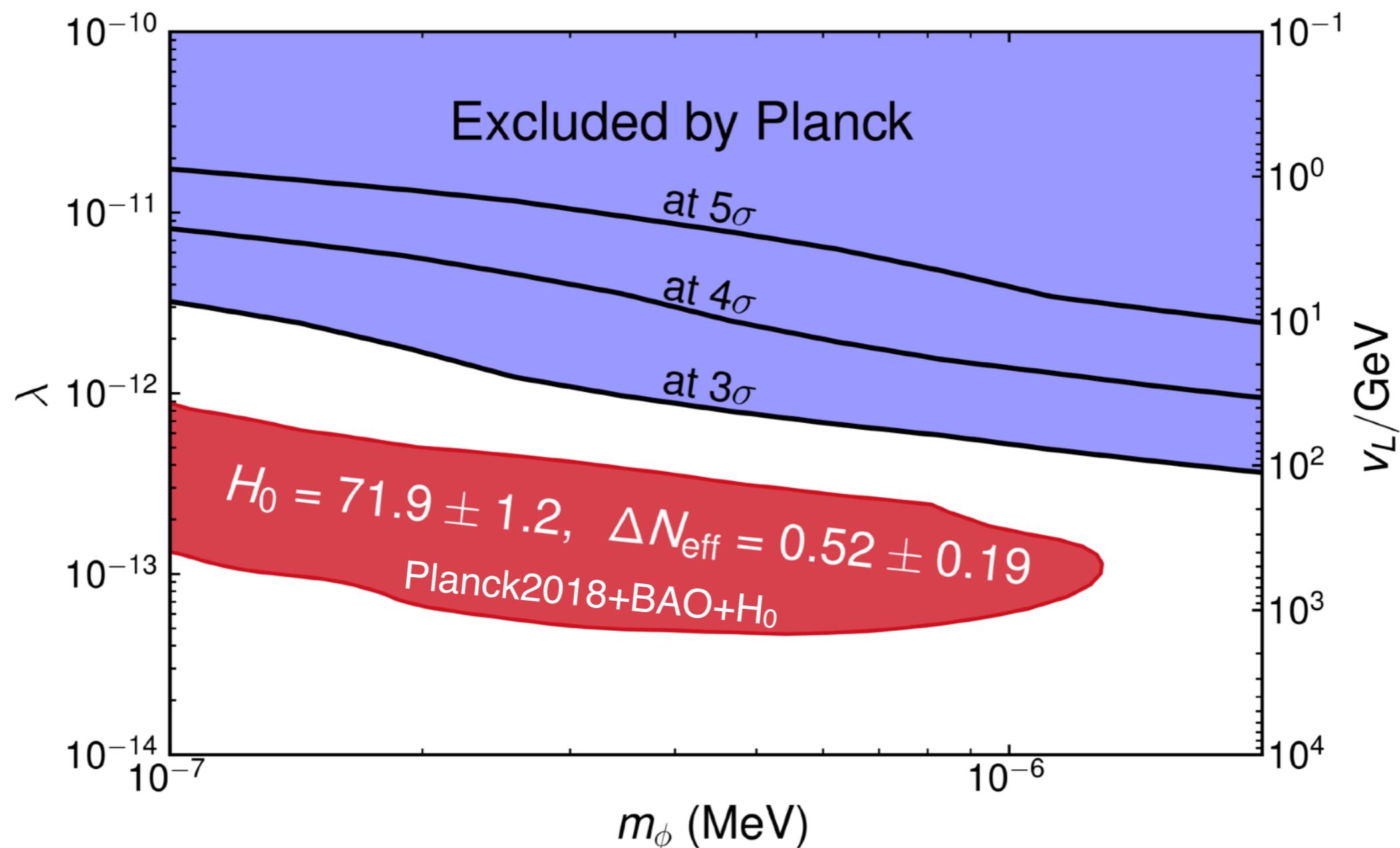


# Parameter Space



**1 $\sigma$  preference when including  $H_0$  in the fit and an additional  $\Delta N_{\text{eff}}$**

# Parameter Space for $H_0$



- Requires a positive  $\Delta N_{\text{eff}} \sim 0.5$
- $H_0$  Thanks to the  $\nu - \phi$  interactions Planck 2018 fit is not degraded wrt  $\Lambda\text{CDM}$
- Very close to the electroweak scale  $v_L \sim (0.1 - 1) \text{ TeV}$

# Summary of Escudero & Witte 19'

- The Majoron and the Hubble tension
  - Planck sets very stringent constraints
  - The CMB-S4 experiment can test large regions of parameter space since  $\sigma(N_{\text{eff}}) \simeq 0.03$

$$m_\phi \sim (0.1 - 1) \text{ eV}$$

- Can reduce the tension if:
  - $v_L \sim (0.1 - 1) \text{ TeV}$
  - $\Delta N_{\text{eff}} \sim 0.5$

😐  $\Delta N_{\text{eff}} \sim 0.5$  is somewhat ad hoc

😊 Now we have a very good reason for it!

# Primordial Majorons

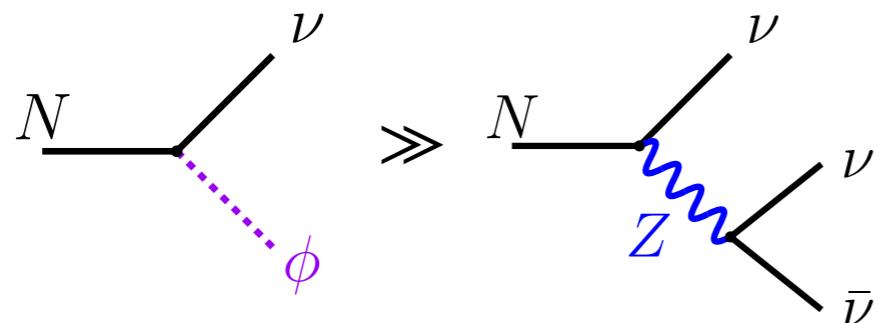
- There are sterile neutrinos in the model  
since  $\nu_L \lesssim 1 \text{ TeV}$  then we can expect  $M_N \sim 1 \text{ GeV}$
- The decays of GeV-scale sterile neutrinos in the early Universe can lead to  $\Delta N_{\text{eff}}^{\text{BBN}} \sim 0.3$  since  $T_d \sim M_N/10$
- Neutrino-Majoron interactions can rise it to  $\Delta N_{\text{eff}}^{\text{CMB}} \sim 0.6$
- These sterile neutrinos can do ARS Leptogenesis!

# Production of Majoron population

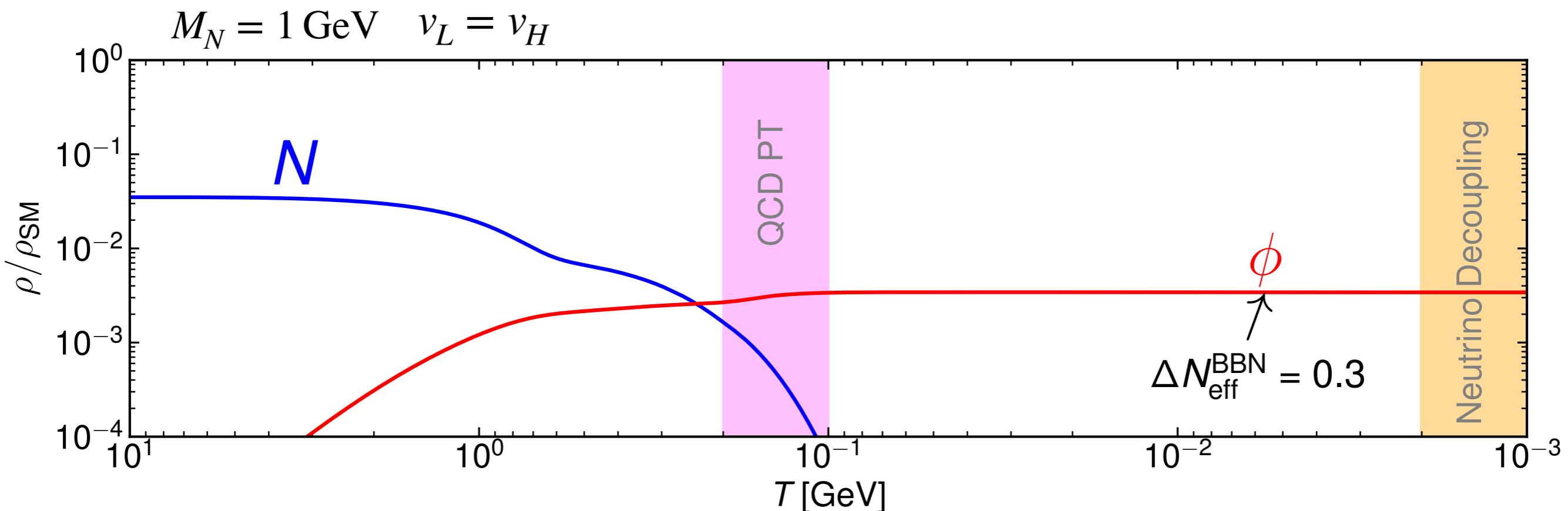
- Sterile neutrinos have masses  $\sim \text{GeV}$  and interact with the majoron

Sterile neutrinos that give mass to the active ones thermalize      (Ghiglieri & Laine 1605.07720)

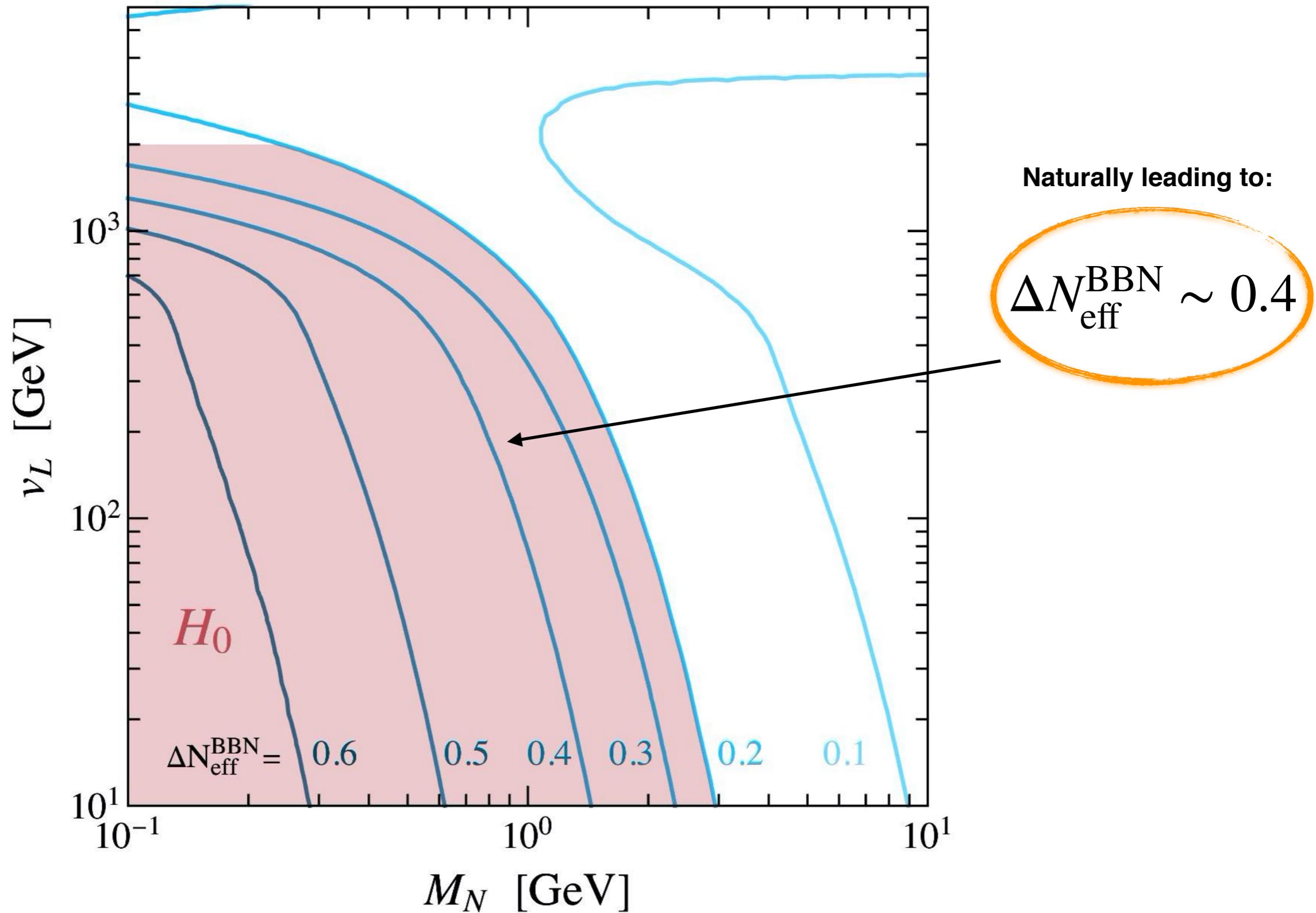
In the majoron model sterile neutrinos have a new decay mode



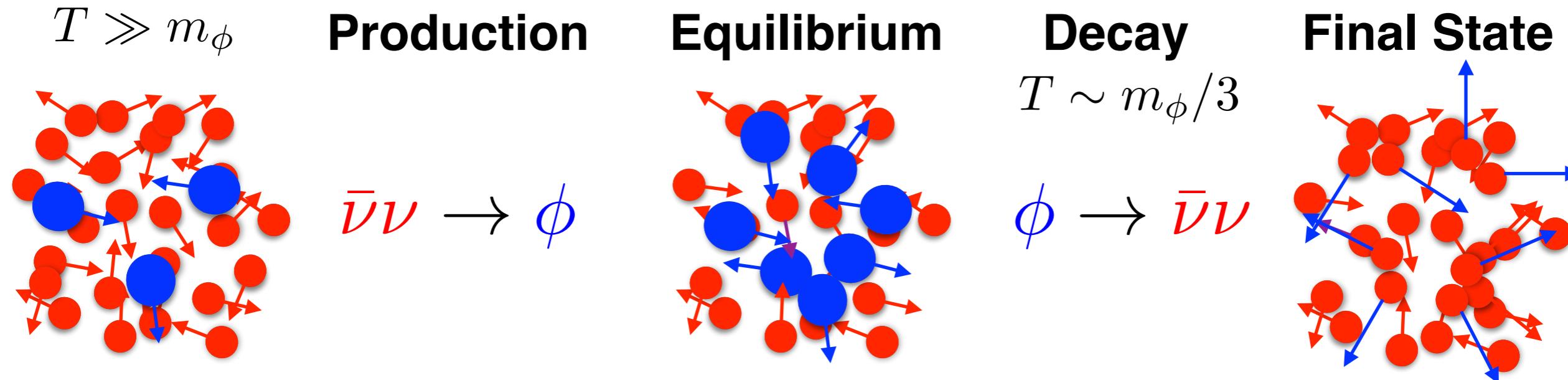
$$\frac{\Gamma(N \rightarrow \nu\phi)}{\Gamma(N \rightarrow \text{SM})} \simeq 4 \times 10^3 \left( \frac{1 \text{ GeV}}{M_N} \right)^2 \left( \frac{1 \text{ TeV}}{v_L} \right)^2$$



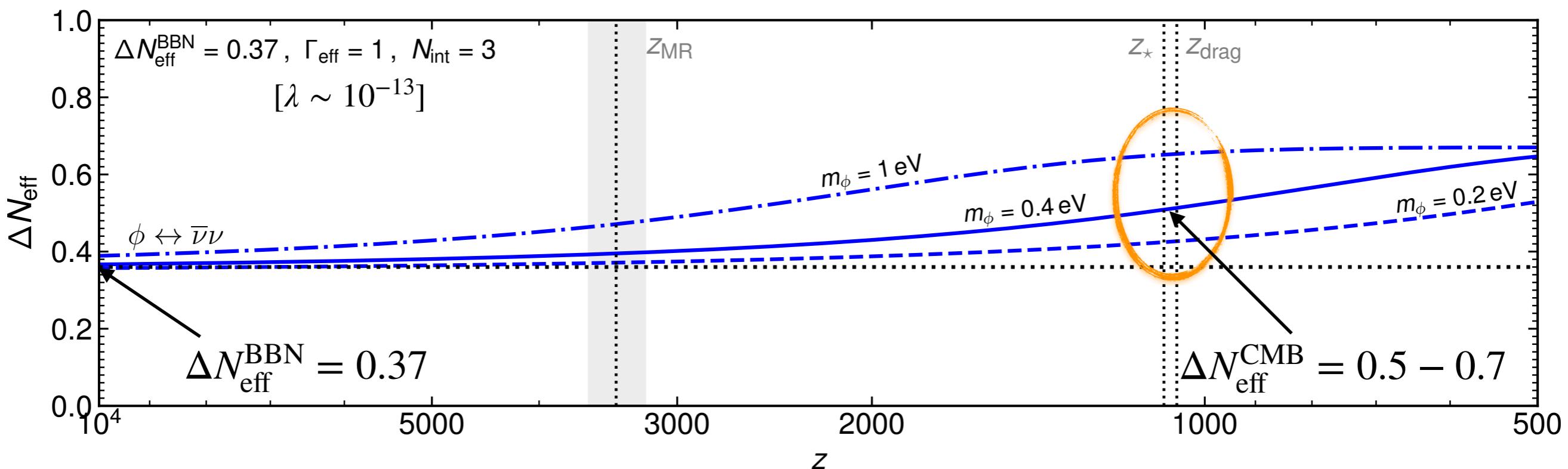
# Parameter Space



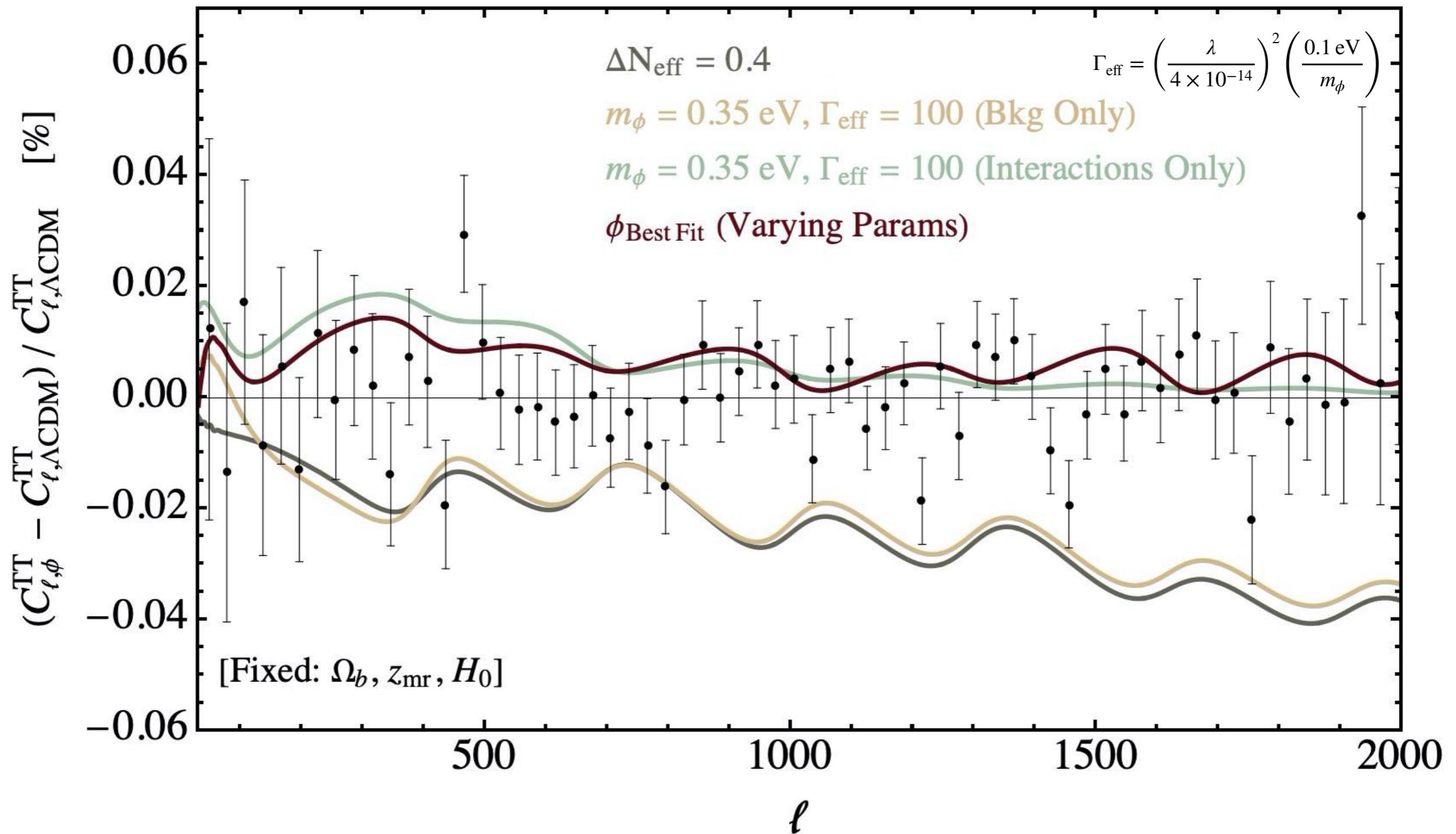
# Cosmological Implications



**The effect is enhanced if there is a primordial population:**



# Effect on the CMB



**Neutrino-Majoron interactions can compensate the enhanced expansion history!**

# Summary of Escudero & Witte 21'

- Sterile Neutrinos can provide just the right primordial majoron population
- A full Planck Legacy data analysis shows that:

for  $\Delta N_{\text{eff}}^{\text{BBN}} = 0.37$

$$H_0 = (70.2 \pm 0.6) \text{ km/s/Mpc}$$

$$\begin{aligned}m_\phi &= (0.1 - 0.8) \text{ eV} \\v_L &= (0.05 - 2) \text{ TeV} \\M_N &\sim \text{GeV}\end{aligned}$$

This makes the tension  $5\sigma \rightarrow 2.5\sigma$  but with a better CMB fit than  $\Lambda$ CDM!

- We argue that in the parameter space of interest these sterile neutrinos can lead to the baryon asymmetry of the Universe via their CP violating oscillations. ARS-Leptogenesis

Akhmedov, Rubakov & Smirnov, hep-ph/9803255  
See also Asaka & Shaposhnikov, hep-ph/0505013

provided  $|\lambda_{\phi H}| < 10^{-7} \frac{v_L}{1 \text{ TeV}} \sqrt{\frac{10^5 \text{ GeV}}{T_c}}$  which requires some fine tuning  
but at least is protected under RGE flow

Our expectations have been confirmed by:

[2109.10908](#) Flood, Porto, Schlesinger, Shuve & Thum  
[2110.14499](#) Fischer, Lindner & van der Woude

# Final Summary

## The Majoron as a solution to the Hubble tension

- The Majoron can substantially relax the tension and can accommodate  $H_0 \simeq 70 \text{ km/s/Mpc}$  while providing a good CMB fit.
- The Majoron is a well motivated particle:
  - It is predicted within the type-I seesaw with a global Lepton number symmetry
  - Its interaction rate with neutrinos is naturally very feebly
  - The Majoron mass could be understood from Planck-scale physics and points to  $m_\phi \sim \text{eV}$
- Parameter space to ameliorate the Hubble tension is well motivated:  $\nu_L \sim \nu_H$
- The sterile neutrinos in the model play a crucial role:
  - By providing by their decays  $\Delta N_{\text{eff}}^{\text{BBN}} \sim 0.3$
  - In addition, they could be responsible for low-scale Leptogenesis

# Outlook

- **Collider tests**  $K \rightarrow \mu N$  (NA62)  
 $\pi \rightarrow e N$  (PIENU)
- **Refined cosmological analysis**  
We are doing a careful cosmological analysis  
Improved collision term: Stefan Sandner, Escudero & Witte 2208.xxxxxx
- **Cosmological tests**  
There are signals for ongoing/upcoming CMB experiments:  
ACT, SPT, Simons Observatory and CMB-S4
- **My main conclusion:**  
Regardless of what happens with the Hubble tension, we will learn about fundamental physics! Probing a well motivated neutrino mass model with  $\Lambda \sim 1$  TeV!

# Acknowledgements

Unterstützt von / Supported by



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**Alexander von Humboldt  
Stiftung / Foundation**

**Sam Witte!**



Munich 2021



# Time for Questions and Comments

**Thank you a lot for the invitation  
and for your attention!**

